Thermodynamics of Aqueous Reciprocal Salt Systems. I. Relationships between the Thermodynamic Behaviour of Molten and Aqueous Mixtures

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For high temperature reciprocal reactions of the type:

$$AX_{(1)} + BY_{(1)} = AY_{(1)} + BX_{(1)}$$

(all components being in the pure liquid state), where A,B stand for the cations and X,Y for the anions, the change in standard Gibbs energy is ΔG_{ex}° . This energy parameter enters the expression for the activity coefficients in a mixture of the four salts according to the equation by Flood, Førland and Grjotheim. The results presented in this paper demonstrate that ΔG_{ex}° may be considered to be a main contribution to the activity terms in concentrated solutions. Based on calculated activity coefficients by means of Pitzer's equation, the relative contributions of ΔG_{ex}° and of hydration effects are discussed. A criterion is proposed to estimate the predominant effect.

Introduction

Unlike the numerous investigations of reciprocal salt pairs in their molten state, 1,2 the systematic work on these systems in aqueous solutions has not essentially been continued since the early works of van't Hoff, Brønsted 4,5 and Jänecke. The treatment of the thermodynamic properties of mixtures of salt solutions without common ions gives rise to the most elaborate equations within the framework of the recent methods of the specific ion interaction approach. Usually not all of the needed interaction coefficients are available and extrapolations toward higher concentrations are doubtful.

Therefore it seems worthwhile to search for some simple relationships between the behaviour of aqueous and molten mixtures as a basis for the

Relations for Molten Salts

It is well-known that molten salt mixtures without common ions show a stronger non-ideality than the corresponding common ion mixtures. For simple reciprocal salt mixtures, like NaCl + KF, the deviations can be explained by pure electrostatic interactions, the so-called reciprocal Coulomb effect.⁸ According to this, the stable salt pair is characterized by the ion combinations: small cation-anion and large cation-anion (NaF + KCl in the given example).

More generally Flood, Førland and Grjotheim⁹ have shown that the thermodynamic mixing properties of a system A⁺,B⁺//X⁻,Y⁻ can be cal-

development of extrapolation prosedures or appropriate model equations. It is the aim of this paper, on the basis of published experimental data on aqueous reciprocal salt mixtures, to look for a correlation with the standard Gibbs energy of the corresponding reciprocal exchange reactions.

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culated in a first approximation from the standard Gibbs energy ΔG_{ex}° of the exchange reaction (I).

$$AX(l) + BY(l) \rightarrow AY(l) + BX(l)$$
 (I)

The activity coefficients γ_{ij} of the salt components AX, BY, AY and BX are related to ΔG_{ex}° by the equations (2a, 2b).

$$\begin{split} &\ln\gamma_{AX} = X_B X_Y (\Delta G_{ex}^{\circ}/RT), \\ &\ln\gamma_{BX} = X_A X_Y (\Delta G_{ex}^{\circ}/RT) \end{split} \tag{2a}$$

$$\begin{split} &\ln\!\gamma_{\text{AY}} = -X_{\text{B}} X_{\text{X}} (\Delta G_{\text{ex}}^{\circ} / \! RT), \\ &\ln\!\gamma_{\text{BX}} = -X_{\text{A}} X_{\text{Y}} (\Delta G_{\text{ex}}^{\circ} / \! RT) \end{split} \tag{2b}$$

The excess Gibbs energy of mixing $\Delta_m G^E$ for the mixtures AX-BY and AY-BX is given by the relations (3a, 3b).

$$\Delta_{m}G^{E}(AX/BY) = \Delta G_{ex}^{o}(X_{A}X_{B}X_{Y} + X_{A}X_{B}X_{Y}) (3a)$$

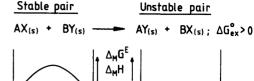
$$\Delta_{m}G^{E}(AY/BX) = -\Delta G_{ex}^{\circ}(X_{A}X_{B}X_{X} + X_{A}X_{B}X_{Y})$$
(3b)

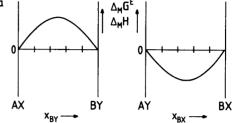
X, represents the ionic fraction of the ion i as defined by the Temkin model.8

It has been shown that Equations (2a, 2b) or (3a, 3b), respectively, can be derived as zero order approximations from a quasi-lattice model⁸ and also from the conformal ionic solution theory. In the case of strictly regular common ion subsystems and if $\Delta G_{ex}^{\circ} > 0$, the composition dependence of the activity coefficients and the excess Gibbs energy of mixing is of the type shown in Fig. 1. The mixtures of the stable pairs exhibit positive deviations that is increasing activity coefficients and $\Delta_m G^E$ or $\Delta_m H > 0$. We find just the opposite situation for the unstable pairs. $\Delta_m G^E$ and $\Delta_m H$ give identical curves, since for regular solutions the excess entropy of mixing $\Delta_m S^E$ is zero.

Relation to Aqueous Solutions

As already emphasized above, 11 both molten salts and aqueous electrolyte solutions represent ionic liquids, the properties of which are governed by Coulombic forces. This should be reflected also in related aspects of the thermodynamics of mixing, especially for the mixtures of reciprocal salt pairs, where the largest changes of electrostatic energy occur. On the other hand the presence of





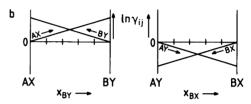


Fig. 1. General pattern of the composition dependence of some thermodynamic quantities. a) Dependence of the excess Gibbs energy of mixing $\Delta_m G^E$ and enthalpy of mixing $\Delta_m H$ on mole fractions x_{BY} , x_{BX} for binary mixtures of the stable pair components (left side) and instable pair components (right side).

b) Dependence of the logarithmic values of the activity coefficients on mole fractions x_{BY} , x_{BX} for the same mixtures.

water will modify the ion-ion interaction due to specific ion hydration.

For the discussion of solution data we refer to ΔG_{ex}° of the exchange reaction in the solid state (Reaction II) at 298.15 K, because most data are available for this temperature

$$AX(s) + BY(s) \rightarrow AY(s) + BX(s)$$
 (II)

 ΔG_{ex}° has been calculated from standard Gibbs energies of formation and solution using references¹²⁻¹⁵ as data sources. The difference between ΔG_{ex}° values, calculated for one and the same reaction, applying various standard data sets, never exceeded 4 kJ/mol.

Enthalpies of Mixing at Constant Ionic Strength

Up till now the enthalpy of mixing has been published for only eight systems of reciprocal pairs.

Table 1. Enthalpies of the mixing of reciprocal salt pairs $\Delta_m H(J/kg H_2O)$ at constant ionic strength I at 298.15 K with $y_A = y_B = 0.5$ (y_A, y_B ionic strength fraction defined as (I_A/I , where I_A ionic strength of salt A).

lonic strength mol/kg H₂O	Stable pair	Unstable pair	Ref.	ΔG _{ex} kJ/mol
1	LiCl - NaBr +116	LiBr – NaCl +65	16	11.5
l	LiCl – KBr +1.5	LiBr – KCl –133	16	14.8
l	NaCl – KBr +5	NaBr – KCI –78	16	6.5
	NaCl – KNO₃ +331	NaNo ₃ – KCI –419	16	2.2
I 3	MgCl ₂ - CaBr ₂ +6 +78	MgBr² – CaCl₂ 16	17	0.9
 	NaCl – Li ₂ SO ₄ +19.1 +405 +1551	Na ₂ SO ₄ – LiCl +64.4 +56.5 -862	18	26.0
 	NaCl – MgSO₄ +60.7 +687 +1958	Na ₂ SO ₄ - MgCl ₂ +206 +913 +1713	19	41.2
1 3 5	+182 +1199 +3027	+180 +1010 +1966		11.5

The reported results are summarized in Table 1. The ΔG_{ex}° in the fifth column refers to the conversion of the stable into the unstable salt pair. Thereby Reaction (II) was formulated on the basis of equivalents for the salts of a higher valence type.

If there exists a relationship with ΔG_{ex}° of the exchange reaction; $\Delta_m H$, for the stable pairs should be positive and negative for the unstable pairs. Indeed, all mixtures of stable pairs possess endothermic enthalpies of mixing. On the other hand, not all $\Delta_m H$ values of the unstable pairs are of negative sign. But, there is a clear tendency for $\Delta_m H$ to be exothermic or less endothermic. In the case of the chargeasymmetric mixtures (the last three systems in Table 1) the situation becomes more complicated because, by keeping the total ionic strength constant, solutions with different molalities have to be mixed. However, at higher concentrations also for these mixtures $\Delta_m H$ on the unstable side is less endothermic or tends toward becoming exothermic as in the example of

Na₂SO₄-LiCl. The authors of the original papers (see ref. Table 1) discussed their results in terms of Young's cross-square rule, which predicts that the sum of the $\Delta_m H$ values of the four binary common ion mictures should be equal to the sum of $\Delta_m H$ of the two reciprocal mixtures, or in symbols $\Sigma \square = \Sigma X$. In this connection it is interesting to note that this rule can also be applied to reciprocal molten mixtures. This is demonstrated in Table 2 for the system Na+,K+//Cl-,Br- based on the data given by Kleppa & Toguri.21 Compared with the analogous aqueous mixtures, the difference between $\Sigma \square$ and X is larger for the molten system, but also the greater uncertainty of measurements at high temperatures must be born in mind.

E.M.F. Measurements

Schwabe et al.²² investigated the influence of high concentrations of perchlorates on the activity coefficients of various salts without a common ion

Table 2. Enthalpies of mixing $ΔH_m$ in the system Na⁺,K⁺//Cl⁻,Br⁻ in the anhydrous molten state and as one molal aqueous solutions, Σ□ represents the sum $ΔH_m$ of all common ion mixtures, ΣX the sum of the two reciprocal mixtures.

Salt pairs	Melts	One molal
·	(1086 ± 2 K)*	solutions**
	J/mol	(298.15 K)
		J/kg H₂O
NaCl-KCl	- 546	-40
NaBr-KBr	- 565	-39
NaCl-NaBr	+ 105	+ 3.3
KCI-KBr	+ 67	+ 3.3
Σ□	- 939	-72.4
NaCl-KBr	+1035	+ 5.1
NaBr-KCI	-2109	-78
ΣΧ	-1074	-72.9

^{*}data from 21, **data from16.

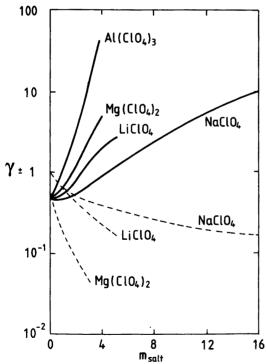


Fig. 2. Dependence of the mean ionic activity coefficient of CdCl₂ and TIF on the molality of various perchlorates²². The molalities of CdCl₂ and TIF are both 0.01 mol/kg H₂O, —— CdCl₂, ---- TIF.

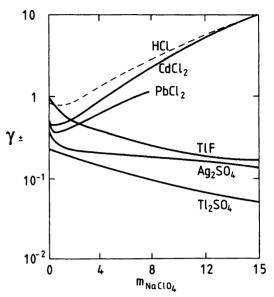


Fig. 3. The dependence of the mean ionic activity coefficient of various salts (m = 0.01) on the molality of NaClO₄.²²

by means of e.m.f. measurements with appropriate combinations of amalgam electrodes and electrodes of the second kind. Their results were only presented graphically, as shown in Figs. 2 and 3. Fig. 2 represents the mean ionic activity coefficient of CdCl, and TlF dependent on the molality of different perchlorates. The concentration of CdCl2 and TlF was kept constant at 0.01 mol/kg H₂O. The most striking feature is the fact that the addition of the perchlorates has an opposite effect on the activity coefficients of these two salts. Whereas the coefficient for CdCl₂ is increased in the order NaClO₄ < LiClO₄ < Mg(ClO₄)₂ < Al(ClO₄)₃, the coefficient of TlF decreases in the same order. In general this increase of $\gamma_+(CdCl_2)$ in the given order is explained by the growing hydration abilities of the cations within the series $Na^+ < Li^+ < Mg^{2+} < Al^{3+}$ or by cation-cation repulsion interactions as suggested by Kelm and Schwabe.23 Apart from a remark on a possible occurrence of ion association in the case of Tl+, the authors gave no satisfactory explanation of the decrease of $\gamma_{\pm}(TlF)$.

However, the different behaviour of $CdCl_2$ and TIF correlates well with the values of ΔG_{ex}° of the corresponding exchange reactions, as summarized in Table 3. Below the chemical formula in

Table 3. Standard Gibbs energies of exchange reactions $\Delta G_{\rm ex}^{\circ}$ and the standard Gibbs energies of solution $\Delta_{\rm e}G^{\circ}$, which have been taken or calculated from ref. ¹²⁻¹⁵.

	Exchange Reactions						ΔG _{ex} kJ/mol
TIF -11.0	+	NaClO₄ -15.9	\rightarrow	TICIO ₄ + 6.6*	+	NaF + 1.25	- 34.7
TIF -11.0	+	LiCIO ₄	\rightarrow	TICIO ₄ + 6.6*	+	LiF +13.8	
TIF -11.0	+	½Mg(ClO₄)₂ -72.2	\rightarrow	TICIO ₄ + 6.6*	+	½MgF₂ +20.1	-109.9
½CdCl ₂ + 2.0	+	NaClO₄ -15.9	\rightarrow	½Cd(ClO₄)₂ **	+	NaCl - 9.0	>+15
½CdCl ₂ + 2.0	+	¹ 2Mg(ClO₄)₂ −72.2	\rightarrow	½Cd(ClO ₄) ₂	+	½MgCl₂ 63.0	>+12
½PbCl₂ +13.6	+	NaClO₄ 15.9	→	½Pb(ClO₄)₂ ***	+	NaCl - 9.0	>+28
½Ag₂SO₄ +14.1	+	NaClO₄ -15.9	\rightarrow	AgClO₄ −19.4	+	½Na₂SO₄ + 0.5	+ 17.1
½Tl₂SO₄ +11.0	+	NaClO₄ 15.9	\rightarrow	TICIO ₄ + 6.6*	+	1Ω2SO₄ + 0.5	- 12.0
NaCl - 9.0	+	½Mg(ClO₄)₂ -72.2	→	NaClO₄ -15.9	+	½MgCl₂ −63.0	- 2.3
NaCl - 9.0	+	LiClO₄	\rightarrow	NaClO₄ -15.9	+	LiCI -41.5	
NaCl - 9.0	+	½Ba(ClO₄)₂ -23.0	\rightarrow	NaClO₄ -15.9	+	1 BaCl₂ - 6.1	- 10.0

^{*}Calculated from solubility²⁸ and extrapolation of the activity coefficients given by R. A. Robinson.³⁴

Table 3 the standard Gibbs energies of solution $\Delta_s G^{\circ}(298)$ of the corresponding salts are given, from which ΔG_{ex}° was calculated by Equation (4).

$$\Delta G_{ex}^{\circ} = \Delta_{s} G^{\circ}(AX) + \Delta_{s} G^{\circ}(BY) - \Delta_{s} G^{\circ}(AY) - \Delta_{s} G^{\circ}(BX)$$
(4)

We find negative values for the reactions of TlF, which become numerically larger when going from NaClO₄ to Mg(ClO₄)₂. According to Equation (2a) this indicates a decrease of $\gamma_{\pm}(\text{TlF})$ in the same order as obtained experimentally.

Unfortunately, for crystalline anhydrous cadmium perchlorate no standard data are available. Taking into account that ΔG for the formation of a stable hydrate from the anhydrous salt must be negative (Reaction III),

$$Cd(ClO_4)_2(s) + 6H_2O(l) \rightarrow Cd(ClO_4)_2 \cdot 6H_2O(s)$$
(III)

 $\Delta_s G^\circ$ for the anhydrous cadmium perchlorate will be even more negative than the value of the hydrate given in Table 3.

For the exchange reactions of $CdCl_2$ positive values of ΔG_{ex}° have been estimated. Therefore, both the influence of the exchange reaction and that of the hydration effect of the cations Na^+ and Mg^{2+} are directed toward an increase in $\gamma_{\pm}(CdCl_2)$.

Likewise the curves of the activity coefficients of PbCl₂, Ag₂SO₄ and Tl₂SO₄, shown in Fig. 4, can be interpreted on the basis of the sign and the relative magnitude of ΔG_{ex}^{o} given in Table 3. For PbCl₂ almost the same applies as in the case of

^{**} Δ_s G°(Cd(ClO₄)₂· 6H₂O) = -38 kJ/mol estimated from saturated solution data with m_s=4.666; γ_{\pm} =65.335 and aH₂O=0.379, which is the water activity of a MgI₂ solution³⁵ of the same concentration.

^{***} $\Delta_sG^\circ(Pb(ClO_4)_2 \cdot 3H_2O) = -42$ kJ/mol calculated from saturated solution data given in ref.³⁷.

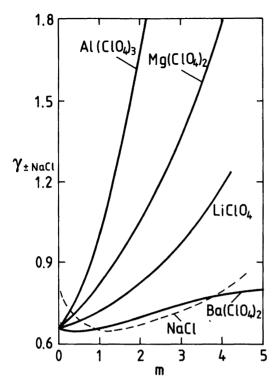


Fig. 4. The dependence of the mean ionic activity coefficient of NaCl (m = 1.0/kg H₂O) on the molality of four perchlorates.²⁴

CdCl₂, which gives rise to a similar dependence of $\gamma \pm (PbCl_2)$ and $\gamma \pm (CdCl_2)$ on the content of NaClO₄. The ΔG_{ex}° of Ag₂SO₄ and Tl₂SO₄ in Table 3 are of opposite sign, but their absolute values are relatively small. Therefore the positive ΔG_{ex}° of Ag₂SO₄ cannot overcompensate the general effect of the increasing ionic strength (Debye-Hückel term), which results in a decreasing curve for $\gamma \pm (Ag_2SO_4)$. Corresponding with the negative sign of ΔG_{ex}° the curve of Tl₂SO₄ shows a stronger drop at high contents of NaClO₄.

Later, measurements of the activity coefficient of NaCl in the presence of the same perchlorates were published²⁴ using sodium ion-conducting glass electrodes (Fig. 4). Again ΔG_{ex}° of the exchange reactions has small absolute values and hydration of the cations (Na⁺, Li⁺, Mg²⁺, Ba²⁺) becomes the dominating factor reflected in an increase of $\gamma \pm$ (NaCl).

Influence of Hetero-ionic Salt Additions on Solubility

The background of investigations of the influence of hetero-ionic salt additions on the solubility was in most cases a test of the validity of the Debye-Hückel-Onsager equation. Therefore with few exceptions only measurements with slightly soluble salts and with electrolyte concentrations below one molal are reported. The applicability of the published solubility data for our purpose is further restricted by the fact that for a lot of salt pairs $\Delta G_{\rm ex}^{\rm o}$ could not be calculated for reason of lacking data (especially LiClO₄, acetates, iodates, bromates, chromates). In spite of this, it seems that some solubility data are of interest to discuss from the reciprocal reaction approach.

Bozorth²⁵ determined the influence of a number of salt additions on the solubility of KClO₄. From these data the variation of the logarithm of

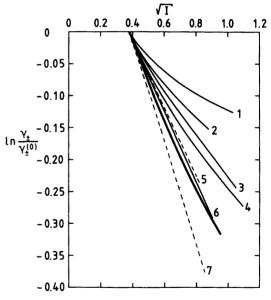


Fig. 5. Variation of the relative mean ionic activity coefficient of KClO₄ as determined from solubility measurements²⁵ at 298.1 K: thick line – theoretical ionic strength's dependence according to Equation (5), continuous lines – non-common salt additions (1 BaCl₂, 2 NaCl, 3 Ba(NO₃)₂, 4 Na₂SO₄, 6 NaNO₃), dotted lines – common ion salt additions (5 KCl, NaClO₄, K₂SO₄, 7 KNO₃). $\gamma_{\pm}^{(0)} =$ activity coefficient of the pure KClO₄ solution.

Table 4. Standard Gibbs energies of exchange reactions ΔG_{ex}° and standard Gibbs energies of solution $\Delta_s G^{\circ}$ components. Values below the chemical formula denote $\Delta_s G^{\circ}$, which have been taken or calculated from ref. ¹²⁻¹⁵.

	Exchange Reactions					ΔG _{ex} kJ/mol	
KClO₄ +11.3	+	NaCi - 9.0	\rightarrow	NaClO₄ 15.9	+	KCL - 5.2	+23.4
KClO₄ +11.3	+	NaNO₃ - 6.2	\rightarrow	NaClO₄ 15.9	+	KNO₃ + 0.7	+20.3
KClO₄ +11.3	+	½Na₂SO₄ + 0.6	\rightarrow	½K₂SO₄ + 5.0	+	NaClO₄ 15.9	+22.8
KClO₄ +11.3	+	½BaCl₂ - 8.2	\rightarrow	KCI - 5.2	+	½Ba(ClO₄)₂ -23.0	+31.3
KCIO₄ +11.3	+	½Ba(NO ₃) ₂ + 6.5	\rightarrow	KNO ₃ + 0.7	+	¹ / ₂ Ba(ClO ₄)₂ −23.0	+40.1
½Ba(NO₃)₂ + 6.5	+	NaBr -17.1	\rightarrow	½BaBr₂ -18.2	+	NaNO ₃ 6.2	$+13.8$ ${\Delta H_{ex}^{\circ} = }$ $+10.5$
½Ba(NO ₃) ₂ + 6.5	+	⅓FeCl₃ -21.3	\rightarrow	½BaCl₂ - 8.2	+	$\frac{1}{3}$ Fe(NO ₃) ₃	$ \begin{cases} \Delta H_{ex}^{\circ} = \\ +15.5 \end{cases} $
KI -11.7	+	NaOH -42.3	\rightarrow	KOH -65.3	+	NaI -30.6	+41.9
½CaSO₄ +12.8	+	NaCl - 9.0	\rightarrow	½CaCl₂ −32.6	+	$\frac{1}{2}$ Na ₂ SO ₄ + 0.6	+35.8
½CaSO₄ +12.8	+	LiNO₃ -14.6	\rightarrow	$\frac{1}{2}$ Ca(NO ₃) ₂ -16.1	+	½Li ₂ SO₄ - 5.0	+19.3
½CaSO₄ +12.8	+	NaNO ₃ - 6.2	\rightarrow	½Ca(NO ₃) ₂ -16.1	+	$\frac{1}{2}$ Na ₂ SO ₄ + 0.6	+22.1
½Ca(OH)₂ +14.4	+	NaCl - 9.0	\rightarrow	½CaCl₂ −32.6	+	NaOH -42.3	+80.3
½Ca(OH) ₂ +14.4	+	NaNO ₃ - 6.2	\rightarrow	$\frac{1}{2}$ Ca(NO ₃) ₂ -16.1	+	NaOH -42.3	+66.6

the relative activity coefficient has been plotted against the square root of the ionic strength (Fig. 5). The thick line represents the theoretical change of the extended Debye-Hückel term given by Pitzer²⁶ (Equation 5).

$$ln\gamma_{\pm} = -A\{\sqrt{I/(1+1.2\sqrt{I})} + (2/1.2)ln(1+1.2\sqrt{I})\}$$
(5)

Except for the curves of KNO₅ and NaNO₃ (which are explained afterwards), the curves for common ion salt additions follow the theoretical one more closely than those for salts without a common ion. This confirms the greater non-ideality of non-common ion mixtures for aqueous

solutions as well, if other compensating effects are absent. In agreement with the positive $\Delta G_{\rm ex}^{\rm o}$ in Table 4 all curves of the hetero-ionic additions are shifted in a positive direction. In the case of NaNO₃ this positive shift occasionally results in a line near to the theoretical one, because the common ion analogous curve of KNO₃ is situated below the Debye-Hückel curve. The stronger hydration of sodium ions cannot be considered as an explanation for the larger activity coefficient of KClO₄ in the presence of the hetero-ionic sodium salts, because the effect of NaClO₄ as a homo-ionic salt is the same as for KCl.

An investigation of a more soluble salt has been carried out by Åkerløf.²⁷ He determined the

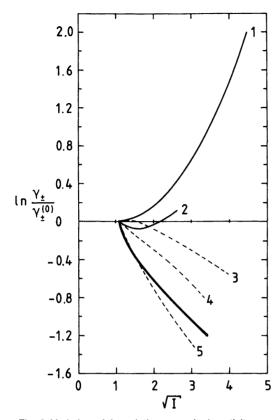


Fig. 6. Variation of the relative mean ionic activity coefficient of Ba(NO₃)₂ as determined from solubility measurements²⁷ at 298.1 K, thick line – theoretical dependence according to Eq. (5), continuous lines – non-common salt additions (1 FeCl₃, 2 NaBr), dotted lines – common ion salt additions (3 Al(NO₃)₃, 4 BaBr₂, 5 NaNO₃), $\gamma_{\pm}^{(0)}$ – activity coefficient of the pure saturated Ba(NO₃)₂ solution.

effect of various salts on the solubility of $Ba(NO_3)_2$ up to ionic strengths of 21 molal. In Fig. 6 the activity coefficients of $Ba(NO_3)_2$ have been plotted in the same manner as before. The hetero-ionic additions are FeCl₃ and NaBr. The enthalpies of the corresponding exchange reactions are positive (see Table 4). This should also be true for ΔG_{ex}° of both reactions because the reaction entropies are generally small as is evidenced by the reaction of $Ba(NO_3)_2$ with NaBr (Table 4). As expected, the reciprocal salt effect becomes more distinct at the higher salt concentrations, so that the positive ΔG_{ex}° values cause not only a relative positive shift, but an absolute

increase of the activity coefficient. On the other hand all salts with a common ion have a decreasing effect on $\gamma \pm (Ba(NO_3)_2)$, although the hydration properties of the cations are similar.

The plot in Fig. 7 is based on solubility determinations of KI in the presence of NaOH or KOH, respectively²⁸. Both hydroxides enhance the activity coefficient of KI due to their strong hydration. From this point of view KOH should give the largest salting-out effect on KI. $\Delta_sG^\circ(KOH) = -65.3$ kJ/mol, whereas $\Delta_sG^\circ(NaOH)$ is only -42.3 kJ/mol). As can be seen from Fig. 7 the reverse is obtained, again in agreement with ΔG_{ex}° of the reaction of NaOH with KI (Table 4), which has a large positive value.

More recently determinations²⁹⁻³¹ of the influence of NaNO₃, NaCl and LiNO₃ on the solubility of CaSO₄ (anhydrite) and Ca(OH)₂ have been performed at enhanced temperatures (T \geq 125 °C) and up to salt concentrations of 6 molal. At a given ionic strength the solubility of CaSO₄ decreases in the order NaNO₃ \approx LiNO₃ > NaCl. Similarly, higher solubilities of Ca(OH)₂

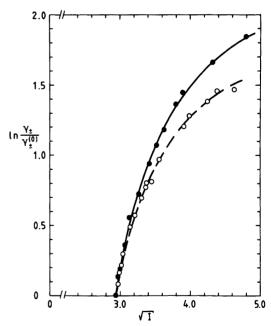


Fig. 7. Dependence of the relative mean ionic activity coefficient of KI on the addition of NaOH (●) and KOH (○) from solubility measurements²³ at 293 K.

in NaNO₃ than in NaCl solutions have been reported³¹. This behaviour is also consistent with the ΔG_{ex}^{o} values given in the last part of Table 4. In the reactions with NaCl, ΔG_{ex}^{o} is more positive, which gives a larger salting-out effect. The exchange reactions of NaNO₃ and LiNO₃ with CaSO₄ have approximately equal values for ΔG_{ex}^{o} .

Activity Coefficients at Constant Ionic Strength

Considering charge-symmetrical systems and mixing at a constant total ionic strength, the contribution of the Debye-Hückel term remains constant and variations of the activity coefficients will be caused only by specific ion-ion and ionwater interactions. If these interactions are dictated by ΔG_{ex}° of the corresponding exchange reaction, a plot of $\ln\gamma_{\pm}$ against the ionic strength fraction of one salt component in the mixture should give the same pattern as shown in Fig. 1 for the molten salts.

Unfortunately, up to now no direct determinations of activity coefficients have been performed for charge-symmetrical reciprocal salt pairs at constant ionic strength, for instance by means of measurements with ion-selective electrodes. Even osmotic coefficients have been determined only for the systems Na⁺,K⁺//Cl⁻,NO₃^{-,26} and Li⁺,K⁺//Cl⁻,NO₃^{-,28} Under these circumstances the application of Pitzer's equations²⁶ seems to be the most reliable way of providing some information about the behaviour of the activity coefficients of a large number of reciprocal systems of constant ionic strength.

For a binary 1-1 electrolyte mixture of AX and BY the dependence of the activity coefficient of AX on the ionic strength fraction y_B of BY is given by Equations (6a-c),

$$\begin{split} &\ln\!\gamma_{\pm}(AX) = \ln\!\gamma^{\circ}_{\pm}(AX) \, + \\ &y_{B}m\{B_{MY} + B_{NX} - 2B_{MX} + \theta_{MN} + \theta_{XY} \, + \, m[B_{MY}' \, + \\ &B_{NX}' - 2B_{MX}' + 2(C_{MY} + C_{NX} - 2C_{MX}) \, + \, \psi_{MNX} + \psi_{MXY}]\} \\ &+ \, y_{B}^{2}m^{2}\{B_{NY}' - B_{MY}' + B_{MX}' - B_{NX}' \, + \\ &C_{NY} - C_{MY} + C_{MX} - C_{NX} \, + \, (1/2)[\psi_{MNX} + \psi_{NXY}] \, - \\ &\psi_{MNX} - \psi_{MXY}\} \end{split} \label{eq:local_equation_for_matrix} \tag{6a}$$

$$B_{ij} = \beta_{ij}^{(0)} + \frac{\beta_{ij}^{(1)}}{2m} \left[1 - (1 + 2\sqrt{m}) \exp(-2\sqrt{m}) \right]$$
(6b)

$$B'_{ij} = \frac{\beta_{ij}^{(1)}}{2m^2} \left[(1 + 2\sqrt{m} + 2 \text{ m}) \exp(-2\sqrt{m}) - 1 \right]$$
 (6c)

wherein m represents the total molality, $\gamma_{\pm}^{(0)}$ the activity coefficient of the pure binary solution, $\beta_{ij}^{(0)}$, $\beta_{ij}^{(1)}$, c_{ij} are constants characterizing the pure binary electrolyte solutions and θ_{ij} , ψ_{ijk} are the socalled mixing parameters, which have to be evaluated from the ternary systems with a common ion. Appropriate replacements of the indices in the Equations (6a–c) yield the activity coefficient of BY.

The advantage of the Pitzer equations compared to other treatments, based on the specific ionic interaction approach, is a smaller number of adjustable parameters and an enhanced predictive power. As has been pointed out, ²⁶ in most cases of simple electrolyte mixtures the activity coefficients are described fairly well at moderate concentrations (m < 3 mol/kgH₂O), even if the mixing parameters are not included.

Using the coefficients tabulated by Pitzer, 26 we calculated the non-common ion trace activity coefficients of all components of 54 reciprocal systems. In order not to exceed the concentration range, within which Pitzer's parameter had been established, a total molality of one was chosen. All systems are listed in Table 5. Again, the stable pairs are arranged on the left-hand side. The last column contains the $\Delta G_{\text{ex}}^{\text{o}}$ values of the conversion of the stable pair into the unstable under standard conditions. The systems are arranged according to falling values of ΔG_{ev}° . The arrow behind each component (e.g. AX) indicates, whether its trace activity coefficient in the solution of the other non-common ion component (BY) is larger (\uparrow) or smaller (\downarrow) than the activity coefficient of the component (AX) in its own, pure aqueous solution.

Thus, the change of the activity coefficients will agree with the sign of ΔG_{ex}° , if the arrows of the stable pair are both directed towards the top and those of the instable pair towards the bottom. As can be seen from Table 5, this is valid for the systems with the largest values of ΔG_{ex}° . Calculations of the full ionic strength fractions dependence of these systems revealed for $\ln\gamma_{\pm}$ the same pattern with crossed, nearly straight lines as shown in Fig. 1 for the molten salt mixtures. With decreasing values of ΔG_{ex}° the differences in the hydration ability becomes more and more impor-

Table 5. Direction of the variation of the activity coefficients of mixing at a total ionic strength of one molal as calculated from Pitzer's equation. ΔG_{ex}° represents the standard Gibbs energy of the exchange reaction converting AX+BY into AY+BX, values calculated from ref. 12, arrow \uparrow (\downarrow) behind component AX (BY, AY, BX) denotes a larger (smaller) value of the trace activity coefficient of AX (BY, AY, BX) in a solution of BY (AX, BX, AY) than in its own pure solution; \star – direction of the activity coefficient variation is opposite to predictions of Eq. (7a, 7b), \bullet – prediction of Eq. (7a, 7b) is uncertain.

AX + BY				AY + BX		
NaF	↑	CsI ↑	Nal	. CsF	91.5	
Nal	†	LiOH T	NaOH	Lil	82.3	
NaBi	r 🛉	LiOH 1	NaOH	LiBr	74.3	
	!	•			Y	
KNO	• !	LiOH ↑	KOH .	LiNO₃	73.5	
NaC	' <u> </u>	LiOH ↑	NaOH .	LiCI	67.6	
NaF	Ţ	CsNO₃ ↑	NaNO₃ .	, CsF	↓ 67.2	
NaF	Ĩ	CsCl ↑	NaCl ,	CsF	↓ 61.2	
Linc)₃ ↓	★ KI ↓	Lil ,	, KNO₃	↑ 50.7	
NaF	1	KI ↑	Nal ,	Į KF	↓ 47.1	
LiCI	Ĺ	● Csl ↑	Lil	CsCl	↑ 45.1	
KF	Ť	Csl 1	● KI	CsF	44.4	
LiOH	. ∤	NaNO₃ ↑	LiNO ₃	NaOH	43.5	
NaO		KI T	Nal .	KOH	41.9	
NaF	'' <u> </u>	KBr ↑	NaBr .	KF	40.1	
	. !	!	· · · · · · · · · · · · · · · · · · ·			
Linc	' 3 ↓	★ Nal	Lil KD::	NaNO₃	38.8	
KF		CsBR ↑	KBr .	CsF	37.3	
Linc)₃ ↓	★ KBr ↓	LiBr	, KNO₃	↑ 35.7	
NaF	Î	KNO₃ ↑	NaNO₃ .	, KF	↓ 35.2	
NaO	н ↓	KBr ↑	NaBr ,	Į ко н	↓ 34.9	
NaF	†	KCI ↑	NaCl ,	Į KF	32.2	
KF	İ	CsNO₃ ↑	KNO ₃	CsF	32.0	
LiNC). Ĭ	★ NaBr	LiBr	NaNO ₃	↑ 30.7	
NaC		Csl ↑	Nal	CsCl	↑ 30.3	
NaO			· · · · · · · · · · · · · · · · · · ·	KOH	29.9	
	п ↓	KNO₃ ↑	★ NaNO ₃		•	
LiCI	_ ↓	KI ↑	Lil ,	KCI	29.7	
NaN	O₂ ↓	KNO₃ ↑	NaNO₃ ,	KNO ₂	29.45	
KF	1	CsCl ↑	★ KCI ,	CsF	↓ 29.0	
NaO	н 🗼	KCI ↑	★ NaCl	ļ ко н	↓ 26.9	
NaN	O₂	★ KCI ↓	NaCi ,	★ KNO₂	↑ 26.4	
Linc), [NaNO₃ ↑	LiNO ₃	★ NaNO₂	↑ 24.8	
NaN		Csl	Nal	CsNO ₃	↑ 24.3	
LiNC		NaCl ↑	LiCl	NaNO ₃	↑ 24.0	
LiCI	·3	CsBr ↑	LiBr	CsCl	22.9	
Linc	, †	★ KCI	LiCI	KNO ₃	21.0	
LiBr	′ 3 ∤	Csl	Lil	CsBr	19.4	
	. ∳		· · · · · · · · · · · · · · · · · · ·		I .	
NaC	, Ť	CsBr ↑	NaBr ,	CsCl	↑ 16.2	
KCI	Ţ	Csl ↑	KI ,	★ CsCl	↑ 15.3	
LiCI	ļ	Nal ↑	NaC l	Lil	↓ 14.8	
LiCI	\downarrow	KBr ↑	LiBr	Į KCI	↑ 14.7	
NaC	l 🕇	KI ↑	Nal ,	Į KCI	↑ 12.8	
KNO) _a	★ Csl ↓	KI ,	CsNO ₃	12.4	
NaN		★ KI Ŭ	Nal	KNO₃ Č	↑ 11.9	
KCI		CsBr ↑	KBr	CsCl	8.2	
LiBr	*	Nal 1	Lil	NaBr	↑ 8.0	
KBr	*	Csl 1	KI ,	● CsBr	↑ 7.1	
	†					
LiCI	, ∳	NaBr ↑	LiBr	NaCl	↑ 6.7	
NaC		KBr ↑	NaBr	KCI	↑ 6.45	
NaC	•	CsNO₃ ↑	NaNO ₃	CsCl	↓ 6.0	
NaF		★ KNO ₂ ↑	★ NaNO₂	, KF	↓ 5.75	
NaF		KOH ↓	NaOH	, KF	↑ 5.3	
NaN		● KBr ↓	NaBr ,	KNO ₃	↑ 4.9	
NaC		KNO₃ ↑	NaNO ₃	KCI	3.0	
KCI	Ψ	CsNO₃ ↑	KNO ₃	CsCl	2.9	

tant, so that γ_{\pm} decreases (\downarrow) for the stronger hydrating salt and increases (\uparrow) for the other.

Looking for a more quantitative representation of these tendencies we tried to find a correlation with the relationship (7a, 7b) written here for the case of a stable pair.

$$\begin{aligned} & \ln \gamma_{\pm}(AX) \approx \Delta G_{\text{ex}}^{\circ} + (\Delta_{s} G_{\text{AX}}^{\circ} - \Delta_{s} G_{\text{BY}}^{\circ}) & (7a) \\ & \ln \gamma_{\pm}(BY) \approx \Delta G_{\text{ex}}^{\circ} + (\Delta_{s} G_{\text{BY}}^{\circ} - \Delta_{s} G_{\text{AX}}^{\circ}) & (7a) \end{aligned}$$

This relationship involves the difference of the standard Gibbs energies of solutions of the two salts to account for varying hydration abilities. For the corresponding unstable pair the negative value of ΔG_{ex}° has to be inserted and the indices must be substituted by AY and BX.

The direction of the activity coefficient change predicted by Equations (7a, 7b) agrees with the calculations using Pitzer's equation in 174 cases, however, for 30 salts it fails (marked with asterisks in Table 5). In eight cases (marked with black dots) the directon of change of lny according to Equations (7a, 7b) is uncertain, because the value is zero within the limits of uncetainty of the standard values. It should be emphasized that almost all the salts, which are marked by asterisks, belong to nitrate-containing systems. Simple binary mixtures of nitrates with common ions, like KCl-KNO₃, 38 exhibit already a peculiar behavior. Presently it is difficult to decide for which of these systems the calculations by means of the Pitzer equation may have failed. Only for three systems (Na+,K+//Cl-,Br-; $Na^{+}, K^{+}//Cl^{-}, NO_{3}^{-}; Li^{+}, Na^{+}//Cl^{-}, NO_{3}^{-})$ are all mixing parameters available and from detailed calculations of these systems it follows that the mixing parameters are of greater importance for the reciprocal mixtures than for the common ion mixtures. On the other hand the results calculated by us for the system Li⁺,K⁺//Cl⁻,NO₃ are close to those given by Scatchard³³ derived from a thorough analysis of freezing point measurements.

Conclusion

Reliable thermodynamic data of reciprocal salt systems in aqueous solutions are scarce, especially in concentrated solutions. In spite of this, the data from very different origins and sources, which have been discussed here, show clearly that the thermodynamic behaviour of mixed aqueous solutions of reciprocal salt pairs is related to the Gibbs energy of the corresponding exchange reactions ΔG_{ex}^{o} referring to the pure components. In this respect a parallelism exists to the corresponding molten salt systems. But in aqueous solutions besides the exchange reaction also the differences in the hydration abilities of the ions of the two salts must be considered. As a measure of the latter the differences of the standard Gibbs energies of solution have been proved to be useful.

In applications of the Conformal Ionic Solution Theory to molten mixtures of reciprocal salt pairs, the complete second order expression is uaually used, which means that besides the reaction term $\Delta G_{\rm ex}^{\circ}$ the mixing terms of the binary common ion subsystems are included. Similarly the addition of suitable binary mixing terms could be a way to account for the contribution of hydration within aqueous systems. However, in order to verify such an expression, more experimental data on aqueous reciprocal salt systems are required. To improve this situation, it is planned to perform solubility measurements in our next work.

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