## Conformation and Vibrational Spectroscopic Study of Fluorocyclohexane

S. D. CHRISTIAN, J. GRUNDNES, P. KLÆBOE, E. TØRNENG and T. WOLDBÆK

<sup>a</sup> Department of Chemistry, University of Trondheim, NLHT, N-7000 Trondheim, Norway and

<sup>b</sup> Department of Chemistry, University of Oslo, Oslo 3, Norway

The IR spectra of fluorocyclohexane as a vapour, liquid and as a solid at low temperatures were recorded in the region  $4000-50 \text{ cm}^{-1}$ . High pressure IR spectra of the pure sample (0-40 kbar) and of CS<sub>2</sub> solutions (0-10 kbar) in a diamond anvil cell were obtained. Raman spectra of the liquid and of the amorphous and crystalline solids at various temperatures were recorded. Fluorocyclohexane as a vapour and liquid and in the plastic solid state contained a mixture of molecules in the equatorial and axial conformations. At ca. 180 K a reversible transition between the plastic phase and an anisotropic crystal, containing the e-conformer took place, although a small amount of the a-conformer persisted in these experiments.

Compression of the liquid produced the plastic, isotropic solid at relatively low pressures (0,5-1) kbar), but at ca. 7 kbar an anisotropic crystal with strongly enhanced e-bands was formed. The a-bands gradually disappeared at still higher pressure. With increased pressure, solutions of fluorocyclohexane in  $CS_2$  showed a shift in equilibrium towards the a-conformer. In thiourea clathrates fluorocyclohexane did not (as guest molecules) exist in a preferred conformation.

A normal coordinate analysis was performed for both conformers, using general valence force fields analogous to those for the *trans*-1,4-dihalocyclohexanes. Tentative assignments of the fundamental frequencies belonging to the *e*- and *a*-conformers are presented, based upon the observed spectra and the results of the force constant calculations.

Chloro, bromo and iodocyclohexane have been studied in great detail by a variety of physical methods. In the vapour phase, in solution and in the liquid state the equatorial conformers are invariably in highest abundance, and the compounds all crystallize in the e-conformer at low tempera-

tures2-5 and under high pressures.4

The conformational equilibrium in fluorocyclohexane has been studied by electron diffraction,<sup>6</sup> microwave,<sup>7,8</sup> NMR<sup>9,10</sup> and <sup>13</sup>C NMR <sup>11,12</sup> spectroscopy. The energy difference, 1080±120 J/mol (vapour),<sup>8</sup> is close to the value determined in solution.<sup>9,10</sup> Therefore, the equatorial conformer is more abundant in these phases, but the axial conformer is slightly more stable relative to the equatorial form than in chloro, bromo and iodocyclohexane.

Earlier vibrational studies of fluorocyclohexane led to erroneous <sup>2</sup> or misleading <sup>5</sup> conclusions regarding the conformers since no simplification of the spectra was detected after solidification. This failure was probably caused by insufficient <sup>2</sup> or too rapid <sup>5</sup> cooling of the liquid. From analogies with the other halocyclohexanes, Rey-Lafon *et al.*<sup>5</sup> attempted to attribute several IR and Raman bands to the *e*- or *a*-conformers. More recently, they assigned the fundamentals on the basis of force constant calculations <sup>13</sup> leading to various revisions of their earlier <sup>5</sup> results.

We have recently made quite thorough investigations of the vibrational spectra and the conformations of various trans-1,4-dihalocyclohexanes <sup>14,15</sup> and made normal coordinate analyses on these compounds by the overlay technique. <sup>16</sup> The force fields are now being tested on other substituted cyclohexanes, including fluorocyclohexane. A new and thorough experimental study of the vibrational spectra of fluorocyclohexane has been performed. Particular emphasis has been placed on investigations of the low temperature and the high pressure solid phases. These studies provide important clues for the spectral interpretations.

## **EXPERIMENTAL**

The sample of fluorocyclohexane was prepared by adding hydrofluoric acid to cyclohexene at low temperatures, 5,10 and was purified by fractionation in a spinning band column of 20 theoretical plates (m.p. 12 °C). Weak impurity bands first present at 720 and 648 cm<sup>-1</sup> were not present in samples purified by further distillation, and no impurity peaks were detected by gas chromatographic analysis.

The IR spectra were recorded on a variety of instruments, including a fast scan Fourier transform spectrometer from Bruker (IFS 114c) in the region 4000 – 50 cm<sup>-1</sup>, a Perkin-Elmer model 225 spectrometer (4000–200 cm<sup>-1</sup>) and a Hitachi-Perkin-Elmer FIS-3 spectrometer (400–100 cm<sup>-1</sup>). Far IR vapour spectra were recorded with an RIIC Fourier spectrometer model 520, equipped with a light pipe gas cell of optical path ca. 6 m. The Raman spectra were recorded with a modified <sup>17</sup> Cary 81 spectrometer, excited by a CRL model 52 G argon ion laser, using the 4880 and 5145 Å lines.

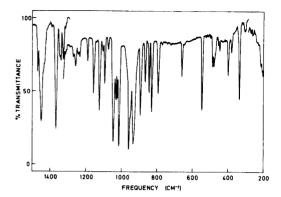
Conventional IR cells for vapour (1 m and 10 cm path), liquid and solutions were employed having windows of KBr, CsI and polyethylene. Cryostats cooled by liquid nitrogen with windows of CsI and polyethylene were used for the IR measurements, and a cooled copper plate was employed for the Raman studies. The temperatures were measured with iron-constantan thermocouples.

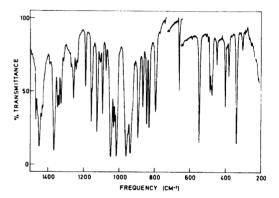
The high pressure solids and compressed CS<sub>2</sub> solutions of fluorocyclohexane were studied in a diamond anvil cell with type II diamonds. In the compressed CS<sub>2</sub> solutions the pressure was estimated by an internal standard of methanol.<sup>18,19</sup>

The various high pressure solid phases were carefully inspected with a polarization microscope. The earlier high pressure spectra were recorded with the PE-225 spectrometer. However, much better data at higher resolution and including the far IR region <sup>20</sup> were obtained with the fast scan Fourier spectrometer due to the multiplex advantage. IR Nujol mull spectra were recorded of fluorocyclohexane—thiourea clathrates.

## **RESULTS**

The IR spectra of fluorocyclohexane in the vapour and liquid states have been reported.<sup>5</sup> Therefore, we have restricted our attention mostly to the solid state spectra. IR spectra of the amorphous (90 K), plastic (190 K) and anisotropic (160 K) solids in the region 1500–200 cm<sup>-1</sup> are shown in Fig. 1, whereas the detailed features in the 900–780 cm<sup>-1</sup> region are given in Fig. 2. High pressure IR spectra of the plastic and anisotropic phases are presented





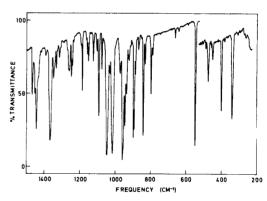


Fig. 1. Infrared spectra of fluorocyclohexane as an amorphous solid at 90 K (upper curve), as a plastic crystal at 190 K (middle curve) and as an anisotropic crystal at 160 K (lower curve) in the region  $1500-200 \text{ cm}^{-1}$ .

in Fig. 3, while the Raman spectra of the liquid (296 K) and the anisotropic solid (90 K) are given in Fig. 4. IR spectra of the 845 and 830 cm<sup>-1</sup> bands at various temperatures between 170 and 183 K

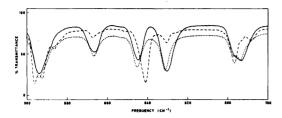


Fig. 2. Infrared spectra of fluorocyclohexane in the region 900-780 cm<sup>-1</sup>; solid line, amorphous solid at 90 K; dashed line, plastic crystal at 190 K; dashed-dotted line, anisotropic crystal at 160 K.

are given in Fig. 5. The far-IR spectrum (440-50 cm<sup>-1</sup>) of fluorocyclohexane in cyclohexane solution is shown in Fig. 6 and spectra of the plastic and anisotropic crystals, recorded in a far-IR cryostat at 90 K are shown in Fig. 7. The wave numbers of the observed IR and Raman bands are listed in Table 1, but for the sake of brevity bands outside the fundamental regions 3000-2800 and 1500-100 cm<sup>-1</sup> are omitted.

The existence of a plastic (cubic, isotropic) crystal for fluorocyclohexane at temperatures below the melting point has been known for a long time.<sup>2</sup> Since earlier attempts to obtain the low temperature anisotropic phase failed <sup>2,5</sup> we report below in some detail the spectral observations at low temperatures and at high pressures.

Infrared spectra at low temperatures. When fluorocyclohexane vapour was deposited on the CsI window at 90 K, no simplification of the spectrum occurred, an amorphous solid being formed (Fig. 1). Heating the sample promoted crystallization and

the intensity of many bands was strongly reduced. When the temperature passed ca. 180 K, however, these bands reappeared, but after slow cooling of the sample, the simplified spectrum was again recorded. Apparently the transition was observed between the plastic phase of fluorocyclohexane and the ordered, anisotropic phase in which one (or mainly one) conformer is present. The transition temperature (180 K) was determined with the spectrometer focused at the 830 cm<sup>-1</sup> band, with alternative heating and cooling of the sample. With the type of cryostat used here, the temperature accuracy is supposed to be about  $\pm 10$  K.

In the spectrum of the anisotropic crystals, weak residual bands persisted (Figs. 1, 2, 6). The intensity of these bands was quite reproducible, and attempts to make pure "one-conformer crystals", by keeping the temperature just below the transition temperature or cycling through this temperature, were not successful. Similar observations are not uncommon in this type of experiment. We do not know, however, if this is due to incomplete conversion of the high temperature phase or to the presence of a small fraction of one conformer in the host lattice of the other.

When the plastic crystal was quenched to liquid nitrogen temperature, only small spectral changes were observed, and a conversion to anisotropic crystals did not take place at this low temperature.

Raman spectra at low temperature. In the Raman experiments the fluorocyclohexane vapour was deposited on a copper finger at 90 K. In some cases the deposit had a glassy appearance, and attempts to promote crystallization by annealing were not successful, in contrast to what was observed with

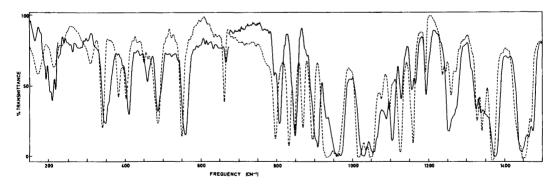


Fig. 3. Infrared spectra of fluorocyclohexane at ambient temperature in the diamond anvil cell; solid line, ca. 40 kbar pressure, anisotropic crystal; dashed line ca. 2 kbar pressure, plastic crystal; 1500-700 cm<sup>-1</sup>, res. 2 cm<sup>-1</sup>, 200 scans; 700-200 cm<sup>-1</sup>, res. 4 cm<sup>-1</sup>, 500 scans; 200-100 cm<sup>-1</sup>, res. 4 cm<sup>-1</sup>, 500 scans.

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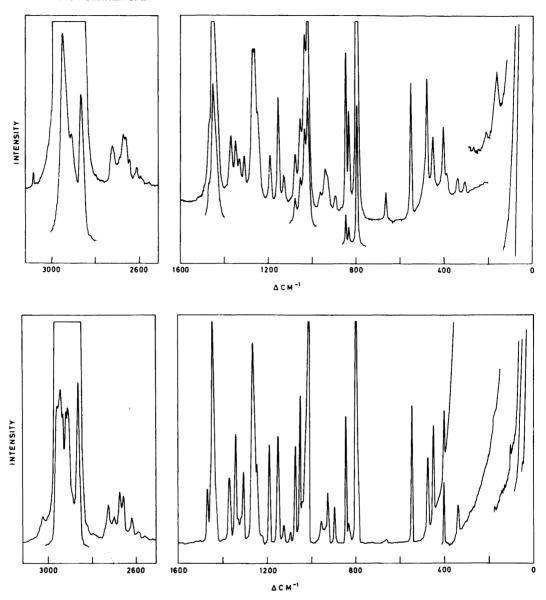


Fig. 4. Raman spectra of fluorocyclohexane as a liquid (upper curve) and as an anisotropic crystal at 90 K (lower curve).

the infrared cryostat. Fortunately, a frosty deposit was formed directly from the vapour in other experiments, and a simplified spectrum was recorded. Furthermore, a sharp and pronounced change in absorption took place at *ca.* 180 K, and above this temperature the spectrum resembled that of the liquid. Below 180 K the bands which showed

strongly reduced intensity corresponded with those which nearly vanished in the infrared spectrum. Undoubtedly, the phase transition from the plastic crystal to an ordered anisotropic phase was observed in these Raman experiments.

The early attempts <sup>2</sup> to obtain anisotropic crystals of fluorocyclohexane apparently failed because

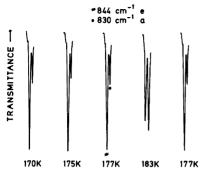


Fig. 5. The IR bands 844 and 830 cm<sup>-1</sup> recorded at various temperatures in succession from 170 K to 183 K and back to 177 K.

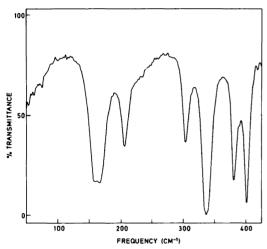


Fig. 6. Far infrared spectrum of fluorocyclohexane dissolved in cyclohexane (20 % solution), 0.2 mm cell thickness, 12  $\mu$ m beamsplitter, 200 scans, 2 cm<sup>-1</sup> resolution.

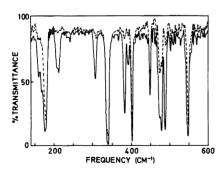


Fig. 7. Far infrared spectra of fluorocyclohexane as an amorphous solid at 90 K (solid line) and as an anisotropic crystal at 90 K (dotted line), 3.5  $\mu$ m beamsplitter, 280 scans, 2 cm<sup>-1</sup> resolution.

temperatures below 200 K were not attainable. It is not clear why the later efforts <sup>5</sup> were unsuccessful. However, the present investigations have shown that too rapid cooling of the plastic phase may preclude detection of the "one-conformer" crystal.

From earlier experience, e.g. with halopropenes, we have concluded that compounds with conformational equilibria often crystallize more readily in a Raman than in an IR cryostat, probably because of the much thicker sample in the former. For fluorocyclohexane the situation was opposite, since we found that if amorphous solids were formed at low temperature (90 K) they were not converted to crystals at any available temperature. In some experiments it could be seen that an amorphous droplet formed on the cold finger simultaneously with the crystalline solid, and the laser beam could be focused on the different regions. For fluorocyclohexane, the thin layer of amorphous sample on the CsI window (IR) obviously crystallized much easier than the thick deposit on a Cu-plate employed in Raman.

Infrared spectra at high pressures. When fluorocyclohexane was compressed in the diamond anvil cell a phase transition leading to the plastic solid took place at rather low pressure. This phase change was difficult to observe under the polarization microscope and might, in fact, be overlooked. On releasing the pressure, the melting process, however, was easily observed.

We have demonstrated <sup>19</sup> that when a gasket is used, it is not possible directly to relate pressure in the diamond anvil cell to the length of the spring which applies force to the diamond faces. Fortunately, pressure-sensitive bands of the compound under investigation can often be used to infer the actual pressure of the sample.<sup>19-21</sup>

The 865 cm<sup>-1</sup> band in liquid fluorocyclohexane shifted less than 1 cm<sup>-1</sup> over the range of pressures from ambient up to the pressure at which the plastic phase first appeared. A shift of this magnitude corresponds to a pressure of less than 1 kbar, probably close to 0.5 kbar. When higher pressures were applied, the phase transition between the plastic and the anisotropic phases occurred at a pressure of about 7 kbar. Inspection in the polarization microscope suggested that complete conversion had occurred from the transparent to the strongly coloured (in polarized light) anisotropic crystals. The IR spectrum of this phase was radically different from that of the plastic phase. Generally, the bands were shifted to higher wave number, as is

Table 1. Infrared and Raman spectral data<sup>a</sup> for fluorocyclohexane.

Vapour	Liquid		Solid					Assignments	
IR	IR	Raman	IR			Raman		б	a
			Low temp. 90 K	High pressure ∼40 kbar	Mod. pressure ~2 kbar°	Low temperature 90 K <sup>b</sup>	190 K°		
$\frac{2959}{2953}$	2940 vs	2947 vs P						·	a
2946	! !	2078 m D						Γ ;	. ;
2910 s	2910 s	$\begin{array}{c} 2910 \text{ s.P} \\ 2910 \text{ vw} \end{array}$						$\begin{cases} v_{2}, v_{3}, \\ v_{2}, v_{3}, \\ v_{4}, v_{29} \end{cases}$	$\begin{cases} v_{28} \\ v_{2}, v_{3}, \\ v_{4}, v_{29} \end{cases}$
$\frac{2870}{2863}$ 8 A	2863 s	2866 s P						$\begin{cases} {}^{V}5, {}^{V}6, \\ {}^{V}7, {}^{V}30, \\ \vdots \end{cases}$	$\begin{cases} v_5, v_6, \\ v_7, v_{30}, \\ v_{10}, v_{30}, \\ v_{10}, v_{30}, \\ v_{10}, v_{10}, \\$
1460 s	1470 m sh 1456 s sh	1470 m D	1468 m 1457 m	1475 s 1465 s	1471 s	1469 w	1470 w sh	v31 v32 v8	(731
1454 s 1444 m	1451 s 1440 m	1450 vs D	1447 s	1446 s	1450  vs $1438  s sh$	1445 vs \\ 1438 sh?	$\frac{1449 \text{ vs}}{1442 \text{ sh}?}$	v <sub>9</sub> , v <sub>33</sub>	$\begin{cases} v_8, v_{32} \\ v_2, v_{32} \end{cases}$
	1433 w sh 1375 w sh	1432 m sh	1435 w sh 1375 m	1427 m sh 1409 vw	1426 m sh 1395 vw	1431 sh	1432 sh	V <sub>10</sub> V <sub>34</sub>	v <sub>10</sub>
$\frac{1371}{1373}$ s	1368 vs	1371 m D	1366 s	1375 vs	1369 vs	1369 w	1369 w	V <sub>11</sub> , V <sub>35</sub>	V34
1351 w 1340 w	1347 w 1339 w	1349 m D	1356 m sh *	1356 m sh	1347 m sh	1344 w	1348 w	V <sub>12</sub> , V <sub>36</sub>	V <sub>11</sub> , V <sub>35</sub>
1332 w	1328 w 1310 vw	1332 w P 1309 w D	1332 vw 1314 vw	1338 m 1326 m	1329 m 1316 vw sh	* 1308 w	1332 vw 1309 w	V <sub>13</sub>	v12, v13, v36 v37
1769.	1270 vw sh	1271 s	1270 vw sh	1274 w sh	1273 w	1268 s	1270 s	comb.	V <sub>14</sub>
1260 m A $1254$	1258 m	1262 s D	1263 w $1257 w$	1267 m sh	1259 m	*	1263 s	comb.	ν38

	v <sub>15</sub>		V39 V40	V <sub>16</sub>	<sup>7</sup> 41		V <sub>17</sub> , V <sub>42</sub>	ν18				v <sub>19</sub>	<i>y</i> 43		<sup>y</sup> 20, <sup>y</sup> 44
	ν <sub>38</sub> ν <sub>15</sub> comb.	V39	V <sub>16</sub>		V40 V41	V <sub>17</sub> , V <sub>42</sub>		V <sub>18</sub>	$v_{22} + v_{27}$	ν19	2xv <sub>24</sub>		ν <sub>43</sub>	<sup>7</sup> 20, <sup>7</sup> 44	$\frac{2xv_{46}}{v_{23}+v_{46}}$
	1248 w sh	1192 w	1155 m	1128 w	1076 w	1053 m	1032 m	1017 vs		958 vw sh		937	927 m	892 w	
	1248 w sh	1191 m	1154 m	*	1074 w	$1054 \mathrm{m}$ $1042 \mathrm{vw  sh} $ $\left. 1053 \mathrm{m} \right.$	*	1016 vs		956 w		*	926 m	894 w	
	1246 w 1238 w	1193 w	1160 s 1155 w sh	1126 s	1108 vw sh 1098 m 1077 w	1050 vs	1036 m	1017 vs		sv 096		935 vs		s 968	870 m
	1255 s 1201 vw sh	1193 w	1166 w 1157 w	1128 m	1104 m 1089 w	1065  m sh $1054  vs$		1030 vs		964 vs		933 w		$907 \mathrm{s}$ $903 \mathrm{m sh}$	891 w sh 882 vw sh
	1247 w 1241 vw	1187 m	* 1152 m	*	1104 w \ 1093 m \ 1075 vw	1046 vs	*	$1022 \mathrm{m} \left\{ 1014 \mathrm{vs} \right\}$	ma 0/6	958 vs	946 m	*	926  vw $922  vw$	896 m 892 m	886 w 878 vw *
	1250 m D	1193 m D	1154 s P	1129 m P	1077 w D	1054 m D	1033 s D	1019 vs D		962 w P		940 m P	933 m D	893 w P	
rued.	1243 vw 1235 vw	1190 vw	1157 m 1153 w	1126 m	$     \begin{array}{c}       1095 \text{ w} \\       1089 \text{ w} \\       1074 \text{ vw}   \end{array} $	1049 vs	1031  m $1024  vw$	, 1016 vs		962 vs	948 sh	938 vs	924 sh	892 m	876 vvw 865 m
Table 1. Continued.	1248 vw 1243 vw	$\frac{1195}{1187}$ w B		1133 1133 1135 1135	1100 w	$1066 \\ 1065 \\ 1065 \\ 1058$	$1033 \atop 1027 $ m B	1022 1019 vs C 1013	920	971 971 964	<del>1</del> 6	962) 954\s C 946	925 w	896 m $898$	867 w

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Continued.
1
Table

	V <sub>21</sub>	V <sub>22</sub>	745	V <sub>23</sub>		V46 V24			747	v <sub>2</sub> s		$\frac{2xv_{27}}{v_{26}}$	8 , ,
V <sub>21</sub>		V <sub>22</sub>	745		V <sub>23</sub>		<sup>V</sup> 24 V46	$v_{27} + v_{48}$ $v_{25}$			V26, V47	V <sub>48</sub>	V27
845 m	831 m	s 797 s		662 vw	549 s	1	4//s 450 m	401 m					
843 m	*	s 66 <i>L</i>	785 vw sh	*	547 s	* "	470 m	397 m		*	337	* 222 w *	*
849 m	833 s	798 s		663 m	552 s'	488 m	460 SII 451 vw	404 m		383 m	341 m	309 w	172 w bd
849 s	840 vw sh	$\begin{cases} 822 \text{ vw sh} \\ 808 \text{ s} \end{cases}$	794 m	wa 299	559 s	493 w sh	459 w	410 m		393 vw sh	356  w sh $348  m$	$321 \text{ vw sh}$ $\sim 240 \text{ vw}$	219 m 210 m 204 m
840 s	*	796 m	м 68 <i>L</i>	*	547 s	* * * * * * * * * * * * * * * * * * *	448 w	40s vw sn 401 m	*	*	338 m	* 235 vw *	179 m *
846 s P	833 m P	797 vs P	787 w	664 w P	. 549 s P	488 w sh D	449 m D	402 m P		385 w sh	338 w P	304 w P	Q
844 m	830 m	793 m	786 vw	661 m	547 s	487 m 482 m 476 m	448 vw	401 w	390 vw	381 w	337 m	312 vw 303 vw 235 vw 205 vw	166 w 157 w
845 m C 840,	834 m C 826	803{ 794}m C 787	(89)	$663 \atop 657$ m A/C	556) 547}s A 541}	488 m 483 m	452 w	399 m A	301)	$\frac{376}{3}$ w B	341) 333}m A/C 326	302 w	155 w bd

<sup>a</sup> Weak bands outside the fundamental regions (4000−3000 and 2700−1500 cm<sup>-1</sup>) are omitted. <sup>b</sup> Anisotropic phase (stable below 180 K). <sup>c</sup> Plastic phase <sup>a</sup>s, strong; m, medium; w, weak; v, very; sh, shoulder; bd, broad; asterisks (\*), indicate bands with strongly reduced intensities; A, B, C, vapour contours; combination band.

ordinarily observed at higher pressures. Most important, many bands (381, 661, 830, 865, 1031, 1126, 1258, 1328 and 1339 cm<sup>-1</sup>) were reduced to approximately 1/5 of their former intensities.

As is apparent from Table 1, these bands are the same ones which disappeared (or were greatly reduced in intensity) in the low temperature phase below 180 K. Undoubtedly, the high pressure anisotropic phase consists of molecules in the same conformation as the low temperature phase below 180 K, but a somewhat larger amount of the other conformer remains than in the low temperature solid. Still higher pressures caused no changes which could be observed by microscopic inspection. However, the bands of the "impurity" conformer were gradually reduced in intensity, and at the highest pressure applied to fluorocyclohexane (estimated to be 30-40 kbar) the 303, 381, 830, 865 and 1031 cm<sup>-1</sup> bands vanished. The bands at 661, 1328 and 1339 cm<sup>-1</sup> remained with very low intensities (cf. Fig. 3 and Table 1). A blue shift of the bands with increasing pressure was generally observed.

An important result of the studies at high pressure is the observation that the bands which vanish at the highest pressures (and at low temperatures below 180 K) in the anisotropic solid are those which increase in intensity as the pressure increases within the plastic phase or in CS<sub>2</sub> solutions of fluorocyclohexane. Within the liquid or plastic phases, the conformer having the smaller partial molar volume will be favoured with increase in pressure, and the results taken together show that the conformer which has the smaller partial molar volume is not that which crystallizes out at high pressures. The a-conformer has the smaller volume (see below), and this means that the anisotropic crystalline phase contains molecules in the equatorial conformation, as is the case with the other halocyclohexanes. Various spectral correlations (see below) also provided supporting evidence for this conclusion.

It is surprising that a significant (and apparently reproducible) amount of the a-conformer remained in the anisotropic crystal at low temperatures and at moderately high pressures. A trivial explanation might be that pressure gradients in the diamond anvil cell lead to regions with lower pressure at the edges and the existence of plastic phase mixed with the anisotropic crystals. However, this is contrary to the visual observations and our experience is that nearly hydrostatic pressures are obtained within the gasket-diamond cavity also when solids

are compressed. Instead we believe that domains of axial molecules are accommodated within the equatorial crystal lattice. Similar results were observed when the *trans*-1,4-dihalocyclohexanes were compressed and these are discussed in some detail elsewhere.<sup>14</sup>

Volume differences between the e- and the aconformers. It was reported 18 that the conformational equilibrium for certain halo- and dihalocyclohexanes in CS<sub>2</sub> solution shifts markedly in the direction of the axially substituted conformers at increased pressures. This is in agreement with larger crowding of atoms, and hence smaller volume, for the a- (or aa-) conformers. From the increase in the ratio of the axial to equatorial band areas with pressure, the volume change  $\Delta \overline{V}$  for the conversion  $e \rightarrow a$  was calculated. In fluorocyclohexane the bands in the 820-880 cm<sup>-1</sup> region were well enough separated to allow measurements of band areas. It was concluded that the 830 cm<sup>-1</sup> and 865 cm<sup>-1</sup> bands belonged to the axial conformer, since the relative intensity of these bands increased with pressure. In contrast, the 844 cm<sup>-1</sup> band became relatively less intense in both phases. For chlorocyclohexane the volume change for conversion of the equatorial to the axial form has been reported to be  $-1.9\pm0.2$  cm<sup>3</sup>/mol.<sup>18</sup> In fluorocyclohexane the variation of the ratios of band areas with pressure was smaller. From the accuracy of the data, we think it is only justified to give  $-1.0 \text{ cm}^3/\text{mol}$ as the upper limit for the volume change in CS<sub>2</sub> solution. In the plastic phase, absence of the solvent made area measurements more reliable. However, the pressure determination was somewhat more uncertain, since we had to assume the same frequency change with pressure for the 865 cm<sup>-1</sup> band in the plastic phase as in CS<sub>2</sub> solution. From a plot of  $ln(A_{830}/A_{844})$  versus pressure, a value of  $\Delta \overline{V} = -1.5 \pm 0.5$  cm<sup>3</sup>/mol for the conversion  $e \rightarrow a$ was calculated. The rather large estimated error reflects the uncertainty in the determination of the pressure.

Clathrates. In thiourea clathrates chloro- and bromocyclohexane are accomodated as a-conformer molecules in the channels,  $^{22-24}$  while iodocyclohexane  $^{23,24}$  has a certain amount of e-conformer in addition. When thiourea clathrates of fluorocyclohexane were prepared using the same techniques as described previously,  $^{24}$  the fluorocyclohexane bands in a Nujol mull were clearly visible in the thiourea windows 1000-800 and 400-300 cm<sup>-1</sup>. The intensities of the IR bands at 962, 938,

892, 865, 844, 830, 381, 336 and 303 cm<sup>-1</sup> in the clathrate were compared to those in the liquid. Surprisingly, the a-bands were only slightly enhanced relative to the e-bands in the clathrate. From the band intensities of the 865 (a) and 844 cm<sup>-1</sup> (e) bands, the ratio  $f = K_{clathr}/K_{liquid}$  (where  $K_{\text{clathr}}$  and  $K_{\text{liq}}$  are equilibrium constants  $C_{\text{a}}/C_{\text{e}}$  in clathrate and liquid, respectively) was found to be approximately equal to 1.4. There appears to be little enhancement of the axial conformer in fluorocyclohexane clathrate, in contrast to the behaviour of cyclohexanes with chloro-, bromo-, and pseudohalo-substituents, for which the axial conformer is highly preferred in the clathrate. (See Table 5 of Ref. 24). The fact that the axial form of fluorocyclohexanes is less favored in the clathrate probably reflects the smaller magnitude of  $\Delta \overline{V}$  for the  $e \rightarrow a$ conversion (in fluorocyclohexane relative to the other halocyclohexanes) and may indicate that a compressive effect analogous to mechanical pressure may be acting to stabilize particular conformers in the clathrate channels. On the other hand, axial iodocyclohexane is not so strongly favoured in the clathrate as the axial conformers of chloro- and bromocyclohexane; in the larger iodocyclohexane, the axial iodine may protrude too far into the channel walls of the clathrate to be accommodated easily.

Spectral correlations. As is apparent from Table 1, some 14 IR and Raman bands present in the vapour, liquid, solution or in the plastic crystal of fluorocyclohexane, vanished or were greatly reduced in intensity in the anisotropic crystalline solids (at low temperature and under high pressure). The number of vibrational lines remaining in the crystal below 1400 cm<sup>-1</sup> agrees with the ca. 35 fundamentals expected for one conformer in this region. For the chloro-, bromo- and iodocyclohexanes, it has been noted that the carbon - halogen stretching band of the equatorial conformer is invariably at higher wave number than that of the axial conformer. This observation was useful in demonstrating that these halocyclohexanes crystallize in the e-conformer.2-5 Earlier work by Crowder and co-workers 25 demonstrates that in fluorinated hydrocarbons the C-F stretching mode is mixed with CH2 bend and C-C stretch. The present normal coordinate analysis indicates that the 938 and 830 cm<sup>-1</sup> bands which vanish and the 1049, 1016 and 962 cm<sup>-1</sup> bands which remain in the anisotropic crystal, all have large contributions from the C-F stretch. Although the latter group of bands has higher wave numbers than the former, this fact alone does not provide convincing evidence that the anisotropic phase is an *e*-crystal.

The IR and Raman bands of halo- (and pseudohalo) cyclohexanes around 850 cm<sup>-1</sup> fall in regular patterns, useful for spectral correlations.<sup>26</sup> In fluorocyclohexane the vanishing bands (at 865 and 830 cm<sup>-1</sup>) should be assigned to the a-conformer and the bands remaining (at 892 and 844 cm<sup>-1</sup>) to the e-conformer for consistency with assignments in Table 2 of Ref. 26. These spectral correlations, then, support our independent conclusion from the high pressure band enhancements.

Isocyanatocyclohexane also crystallized in the e-conformer at low temperatures, while cyanocyclohexane apparently formed amorphous glass, with both conformers present at low temperatures. However, unlike the halocyclohexanes, the two latter compounds crystallized in the a-conformer at high pressure. <sup>26</sup>

The assigned fundamental frequencies for the e- and a-conformers of fluorocyclohexane are listed in Table 2 together with the calculated values. As is discussed below, the force field was transferred from the trans-1,4-dihalocyclohexanes 16 with minor modifications. The agreement with the observed values should be considered very satisfactory, since the deviations are ca. 1 %. When the ith fundamental of the e- and a-conformers are compared, they are separated 5 cm<sup>-1</sup> or less in 21 cases, with the separation being larger for the remaining 27 modes. Therefore, the force constant calculations support the experimental conclusion that the majority of eand a-fundamentals falls within such a small frequency range that the bands overlap. This seems generally true for the halo-4,5 and pseudohalocyclohexanes 26 while in the trans-1,4-dihalocyclohexanes 14-16 spectra the bands of the two conformers are farther separated.

As is apparent from Tables 1 and 2, the CH<sub>2</sub> stretching, scissoring and wagging modes (with the exception of the bands at 1470, 1456 and 1451 cm<sup>-1</sup>) generally coincide for both conformers, and accidental degeneracies between A' and A'' modes also occur frequently. In the region below  $1000 \, \text{cm}^{-1}$  the e- and a-bands are often well separated, an extreme case is presented by  $v_{23}$  for which the e- and a-conformer bands were observed with 114 cm<sup>-1</sup> difference (calculated 107 cm<sup>-1</sup>).

In spite of the fairly complete experimental results and the force constant calculations, there are obviously uncertainties in the interpretations. The

Table 2. Observed and calculated fundamental frequencies for fluorocyclohexane.

	e			a		
	PED <sup>b</sup>	Obs.	Calc.	PED	Obs.	Calc.
a'						
$v_1$	97d(X) <sup>c</sup>	2940	2957	98d(X)	2940	2958
$v_2$	81d	2910	2922	95d	2910	2922
$v_3$	92d	2910	2916	96d	2910	2916
$v_4$	98d	2910	2914	97d	2910	2914
$v_5$	96d	2863	2857	94d	2863	2857
$v_6$	95d	2863	2853	96d	2863	2854
$v_7$	95d	2863	2851	96d	2863	2851
$v_8$	$69\delta + 15\gamma$	1456	1457	$69\delta + 17\gamma$	1451	1456
v <sub>9</sub>	$69\delta + 18\gamma$	1440	1441	$67\delta + 22\gamma$	1440	1438
v <sub>10</sub>	$64\delta + 21\gamma + 10R$	1433	1427	$71\delta + 17\gamma$	1433	1422
v <sub>11</sub>	$36\theta + 31\gamma + 14R + 12\gamma(X)$	1368	1382	$56\theta + 20\gamma(X) + 11\gamma$	1347	1361
v <sub>12</sub>	$83\gamma + 16R$	1347	1341	$80\gamma + 19R$	1339	1348
v <sub>13</sub>	$49\gamma + 26\theta$	1328	1310	$71\gamma + 10R$	1339	1342
v <sub>14</sub>	77y + 13R	1270	1252	$73\gamma + 19R$	1270	1261
v <sub>15</sub>	82γ	1235	1231	81 <sub>7</sub>	1235	1233
v <sub>16</sub>	58y	1153	1134	$54\gamma + 19X$	1126	1122
v <sub>17</sub>	$51X + 17\gamma + 16\omega + 14R$	1049	1040	$50R + 32\gamma$	1031	1031
v <sub>18</sub>	$45R + 26X + 23\gamma + 10\omega$	1016	1015	$34\gamma + 33\omega$	1016	1000
v <sub>19</sub>	35y + 32X + 13R	962	945	$69X + 27\gamma + 25R$	938	937
	44y + 41R	892	896	$49\gamma + 34R$	865	857
V <sub>20</sub>	$51R + 38\gamma$	844	838	$38\gamma + 31R + 23X$	830	829
V <sub>21</sub>	$48R + 30\gamma$	793	778	69R	793	800
v <sub>22</sub>	$43\gamma + 30\omega$	547	541	$31\gamma + 31\omega + 11\Xi + 10R$	661	645
v <sub>23</sub>	$23\omega + 21\Xi + 21\gamma(X) + 16\gamma$		454	$46\omega + 32\gamma$	482	486
V <sub>24</sub>	$59\omega$	401	415	$58\omega + 21\Xi + 21\tau$	381	385
V <sub>25</sub>	$40\omega + 32\tau_s$	337	339	$38\omega + 32\tau_s + 28\Xi$	303	304
ν <sub>26</sub>		166	180		303 157	160
v <sub>27</sub> a''	$42\tau(X) + 27\omega + 14\Xi$	100	160	$40\tau(X) + 24\omega + 10\Xi$	137	100
v <sub>28</sub>	98d	2928	2918	97d	2928	2917
V29	98d	2910	2913	98d	2910	2913
v <sub>30</sub>	96d	2863	2855	97d	2863	2855
v <sub>31</sub>	97d	2863	2852	97d	2863	2852
v <sub>32</sub>	$59\delta + 15\gamma + 12R$	1470	1451	$71\delta + 16\gamma$	1451	1441
v <sub>33</sub>	$67\delta + 21\gamma$	1440	1435	$61\delta + 22\gamma + 12R$	1440	1435
V <sub>34</sub>	$40\gamma + 26\dot{R} + 23\gamma(X)$	1375	1389	$71\gamma + 21\dot{R}$	1368	1368
v <sub>35</sub>	$27\gamma + 20R$	1368	1353	$79\gamma + 13\gamma(X)$	1347	1350
v <sub>36</sub>	89γ	1347	1345	$54y + 20y(X) + 14\delta$	1339	1343
v <sub>37</sub>	$75\gamma + 14\gamma(X)$	1310	1302	46y + 45R + 14y(X)	1328	1330
v <sub>38</sub>	73γ	1243	1245	777	1258	1259
v <sub>39</sub>	$69\gamma + 19R$	1190	1185	$58\gamma + 39R$	1157	1152
v <sub>40</sub>	$53\gamma + 48R$	1095	1113	$88\gamma + 15\gamma(X)$	1153	1142
v <sub>41</sub>	$71\gamma + 21\gamma(X) + 14R$	1074	1071	$68\gamma + 18\mathbf{R}$	1089	1086
V <sub>42</sub>	$57R + 25\gamma$	1049	1052	$55R + 20\gamma$	1031	1034
	$49\gamma + 38\mathbf{R}$	924	917	85y	924	928
V <sub>43</sub>	$54\gamma + 25R$	892	888	$69R + 17\gamma$	865	857
V <sub>44</sub>	76y + 14R	786	<b>789</b>	$78\gamma + 13R$	786	789
V <sub>45</sub>	$59\omega$	448	458	$46\omega + 30\Xi$	487	489
V <sub>46</sub>	78 <b>E</b> +11 <b>R</b>	337	360	$46\Xi + 21\omega + 11\tau$	390	387
ν <sub>47</sub>						197
v <sub>48</sub>	$42\omega + 42\tau$	235	224	$40\omega + 34\tau$	205	

<sup>&</sup>lt;sup>a</sup> When possible, frequency values taken from the liquid spectra are given. <sup>b</sup> The potential energy distribution defined as  $X_{ik} = 100 \; F_{ii} L_{ik}^2/\lambda_k$ . <sup>c</sup> d(X) and  $\gamma$ (X), C–H stretching and CCH bending in the F–C–H group; d and  $\gamma$ , CH stretchings and CCH bendings in the C–CH<sub>2</sub> groups; R, C–C stretchings; X, C–F stretching; δ, H–C–H bendings; θ, H–C–F bending; ω, C–C–C bendings; Ξ, C–C–F bend;  $\tau_s$  and  $\tau$ (X), torsions around the C<sub>3</sub>–C<sub>4</sub> and the C<sub>1</sub>–C<sub>2</sub> bonds (FHC<sup>1</sup>–C<sup>2</sup>H<sub>2</sub>–C<sup>3</sup>H<sub>2</sub>–C<sup>4</sup>H<sub>2</sub>–C<sup>5</sup>H<sub>2</sub>–C<sup>6</sup>H<sub>2</sub>);  $\tau$ , the sum of  $\tau_s$ ,  $\tau$ (X) and the torsion around the C<sub>2</sub>–C<sub>3</sub> bond.

Table 3. Valence force constants for fluorocyclohexane.

Force constan	Group nt	Coordinate(s) involved	Atoms common to interacting coordinates	Calculated value $\phi_i$	Standard error $\sigma(\phi_i)$
Stretch $K_d$ $K_d(F)$ $K_R$ $K_R(F)$ $K_X$	C-CH <sub>2</sub> -C C-CHF-C (C)-C-C-(C) (C)-C-C-(F) C-F	C-H C-H C-C C-C C-F	- - - -	mdyn/Å (4.531) <sup>b</sup> (4.757) (4.369) 4.734 (5.555)	0.096
Bend $H_{\delta}$ $H_{\gamma}^{c}$	$C-CH_2-C$ $C-CH_2-C$	нсн нсс		mdyn Å/rad <sup>2</sup> (0.5055) (0.6450)	
$H_{\omega}$ $H_{\omega}$ $H_{\omega}$ (F)	C-CHF-C C-CHF-C C-CH <sub>2</sub> -C C-CHF-C C-C-F	HCF CCC CCC CCF	_ _ _	0.810 (0.913) (1.083) 1.083	0.036
$H_{\Xi}$ Torsion $\tau$ $\tau(F)_a$ $\tau(F)_e$ $\tau_s$		C+-C+ C-C C-C C-C	- - -	mdyn Å/rad² (0.0161) 0.0613 0.061 0.0463	
Stretch $F_{\rm d}$ $F_{\rm R}$ $F_{\rm RX}$	$\begin{array}{ll} \text{n-stretch} \\ \text{C-CH}_2\text{-C} \\ \text{C-C-C} \\ \text{C-C-F} \end{array}$	C-H,C-H C-C,C-C C-C,C-F	C C C	mdyn/Å (0.019) (0.296) 0.644	0.093
Stretch $F_{R\gamma}$ $F'_{R\gamma}$ $F_{X\theta}$ $F_{R\omega}$ $F_{R\Xi}$ $F_{X\Xi}$	n-bend $C-CH_2-C$ $C-CH_2-C$ C-CHF-C C-C-C C-C-F C-C-F C-CHF-C	C-C,HCC C-C,HCC C-F,HCF C-C,CCC C-C,CCF C-F,CCF	C-C C C-F C-C C-C C-F	mdyn/rad (0.069) (-0.174) 0.84 (0.255) 0.049 0.94 -0.08	0.11 0.086 0.11 0.13
Bend-b $F_{\gamma}$ $F'_{\gamma}$ $F'_{\gamma\theta}$ $F_{\gamma\omega}$	$\begin{array}{c} \text{cend} \\ \text{C-CH}_2\text{-C} \\ \text{C-CH}_2\text{-C} \\ \text{C-CHF-C} \\ \text{C-CH}_2\text{-C} \end{array}$	HCC,HCC HCC,HCC HCC,HCF HCC,CCC	C-C H-C H-C C-C	mdyn Å/rad² (-0.0227) (0.0041) (0) (-0.090)	
fry	$-CH_{2}-CH_{2}-\\-CH_{2}-CH_{2}-\\-CH_{2}-C^{+}H_{2}-C^{*}-\\-CH_{2}-C^{+}H_{2}-C^{*}-\\C^{+}-CH_{2}-CH_{2}-C^{*}-\\C^{+}-CH_{2}-CH_{2}-C^{*}$	H <sub>a</sub> CC,H <sub>b</sub> CC H <sub>a</sub> CC+,H <sub>b</sub> CC H <sub>a</sub> CC+,H <sub>b</sub> CC+ H <sub>a</sub> CC+,H <sub>b</sub> CC+ † H <sub>a</sub> CC+,H <sub>b</sub> CC+ † H <sub>a</sub> CC+,H <sub>b</sub> CC+	$ \begin{array}{l} (H_{a})C\frac{trans}{C}C(H_{b}) \\ (H_{a})C\frac{gauche}{C}C(H_{b}) \\ (C-CH_{b})-C^{+}(H_{a}) \\ (C-CH_{b})-C^{+}(H_{a}) \\ (C-CH_{a})-(CH_{b}-C) \\ (C-CH_{a})-(CH_{b}-C) \end{array} $	(0.0735) (-0.0687) (-0.0337) (-0.0293) (-0.0187) (-0.0309)	
f <sup>t</sup> <sub>γω</sub> f <sup>g</sup> <sub>ω</sub>	$C-C-CH_2$ $C-C-CH_2$ $C-C-C-C$	HCC,CCC HCC,CCC CCC,CCC	$(H)-C \frac{trans}{C}C(C)$ $(H)-C \frac{gauche}{C}C-(C)$ $(C)-C \frac{gauche}{C}C-(C)$ $(C)-C \frac{gauche}{C}C-(F)$	(0.0759) $(-0.0307)$ $(-0.024)$	0.025
f <sub>ω</sub> Ξ	C-C-C-F	CCC,CCF	(C)-C $C-(F)$	0.035	0.037

<sup>&</sup>lt;sup>a</sup> Internal coordinates and symbols are defined in Refs. 16, 28. <sup>b</sup> If a force constant is in paranthesis, its value was not adjusted in the refinement. <sup>c</sup>  $H_{\gamma} = H_{\gamma}(F)$ . <sup>d</sup> The torsion is defined as a normalized sum of three *trans*-torsions.

bands which disappear from the spectrum when the pure e-conformer crystal is formed, are obviously a-bands. The rest of the a-bands coincide with the e-bands and cannot be determined with certainty since no spectra of the pure a-conformer were observed.

The IR band contours and/or Raman polarization measurements can in favourable cases determine the A' or A'' species, but the frequent cases of accidental degeneracy cannot be decided.

As has been done in the case of the *trans*-1,4-dihalocyclohexanes <sup>14-16</sup> we hope later to correlate the spectral data for the whole series of halo and pseudohalocyclohexanes.

Force constant calculations. An initial valence force field for fluorocyclohexane was constructed by transferring force constants from mono- (Cl, Br, I) and trans-1,4-dihalocyclohexanes. <sup>16</sup> The force constants not common for all the different halocyclohexanes were given reasonable values comparable with those for n-alkyl fluorides. <sup>25,27</sup>

The molecular parameters used were the same as for the *trans*-1,4-dihalocyclohexanes <sup>16</sup> except for the C-F distance. That is, all the C-C distances are set equal to 1.54 Å, the C-H distances to 1.093 Å and all the valence angles tetrahedral. The C-F distance=1.398 Å is the same as for the n-alkyl fluorides. <sup>25,27</sup>

The final force field is given in Table 3. The symbols are defined in Refs. 16 and 28. Only 13 force constants were adjusted during the iterations. These are the C-C(F) stretching, the CCF and HCF bendings, three torsional force constants and some interaction terms involving the C-F stretching or the CCF or HCF bendings. The other 26 force constants were fixed at the same values as for the mono- (Cl, Br, I) and trans-1,4-dihalocyclohexanes. For the halogen stretching force constants a simple relationship between bond length, r, and force constant, K,  $Kr^2$  = constant, is found to be approximately valid. 16,29 For the halocyclohexanes 16 this constant was found to be 10.86 mdyn · Å which seems to be a suitable value for fluorocyclohexane as well. Hence the C-F stretching force constant was constrained at  $10.86/r^2 = 10.86/(1.398)^2$ =5.55 mdyn/Å.

All the final force constants are of the expected magnitude compared to those found for the n-alkyl fluorides. The torsional constant,  $\tau_s$ , around the  $C_1-C_2$  bond  $(X-C-C-C_1-C_2-C-C)$  is found to be 0.046 mdyn Å/rad². For chloro-, bromo- and iodocyclohexane as well as for cyclohexane a force

constant of ca. 0.04 mdyn Å/rad² will give a much better fit of the lowest vibrational frequencies than obtained in calculations <sup>28,30,31</sup> where a force constant of 0.024 mdyn Å/rad² was used.

The observed and calculated frequencies are given in Table 2. The agreement is very good considering the approximations used.

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