Thermodynamic Studies of Binary Charged Unsymmetrical Fused Salt Systems. Calorimetric and Electromotive Force Measurements of Yttrium(III) Chloride—Alkali Chloride Mixtures

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The thermodynamic quantities of mixing in liquid $YCl_3 - ACl$ (A = Li, Na, K, Rb, or Cs) mixtures have been measured. The molar enthalpies of mixing (ΔH^M) for all the above binaries have been determined calorimetrically in the temperature range 998 - 1143 K. The partial Gibbs energies of mixing of ACl in the binaries ($A \neq Cs$) have been determined by emf measurements of the galvanic cell:

C(s), $Cl_2(g)|ACl(l)|alkali glass|YCl_3(l)-ACl(l)|Cl_2(g),C(s)$

The partial Gibbs energies and entropies have been calculated.

The interaction parameters $(\lambda^{M} = \Delta H^{M}/x_1x_2)$ were found to be temperature independent and to increase to quite negative values as the size of the alkali metal cation increased. The systems have significant energetic asymmetries with more negative values of λ^{M} in the alkali chloride-rich than in the yttrium chloride-rich region. With the exception of the YCl₃-LiCl binary, all other binaries show a distinct minimum at YCl₃ concentration $X_{YCl_3} \leq 0.25$. The partial entropies of mixing $(A \neq Li)$ show inflection points and a sharp dependence on composition in the concentration region $0.2 \leq X_{YCl_3} < 0.25$. The results are compared with recent thermodynamic data on the lanthanide(III) chloride—alkali chloride binary mixtures and discussed in view of recent Raman spectroscopic studies on the YCl₃-ACl binaries.

A comparison of the interaction parameters for the sequences of binaries LCl_3-ACl (L=La, Ce) indicates that the $\lambda^{M'}$ s could be fitted to a general curve of the form:^{3,5}

$$\lambda^{M} = a(T, P, X) + b(T, P, X)\delta_{1,2} + c(T, P, X)\delta_{1,2}^{2}$$
 (1)

Here $\delta_{12} = (d_1 - d_2)/d_1d_2$ is the size parameter $(d_1$ and d_2 are characteristic interionic distances in the

Recently, the thermodynamic and structural properties of a series of binary liquid LaCl₃-ACl and CeCl₃ – ACl (A = Li, Na, K, Rb, Cs) mixtures have been investigated by means of calorimetric, 1,2 electromotive force. 1,3 and Raman spectroscopic 4,5 measurements. The Raman studies of LaCl₃-KCl mixtures⁴ and especially the Raman spectral changes observed on melting Cs₂NaLaCl₆, Cs₃LaCl₆ and K₃LaCl₆⁵ solids, showed that in alkali chloride-rich mixtures LaCl₆³ configurations are formed. In this species the La3+ cation is in an octahedral chloride geometry. The thermodynamic quantities [integral enthalpy ($\Delta H^{\rm M}$), partial enthalpy $(\Delta \bar{H}_{ACI})$ and chemical potential $(\Delta \mu_{ACI})$ for both the LaCl₃-ACl and CeCl₃-ACl systems were found to increase to quite large negative values as the size of the alkali metal cation increased in the sequence Li < Na < K < Rb < Cs. For mixtures with KCl, RbCl, and CsCl, the enthalpy interaction parameter $\lambda^{M} = \Delta H^{M}/X_{i}$ (1 – X_{i}), (X_{i} = mol fraction of component i), varies strongly with composition and shows a broad minimum at composition $X_{\rm LCl_3} < 0.25$.

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two salts which are mixed) and a, b, and c are functions of temperature, pressure, and composition. It was further argued that, since the characteristic physical and chemical properties (polarizabilities, interionic distances, etc.) of all lanthanide chlorides are similar, eqn. (1) should be general for lanthanide chloride – ACl mixtures.

However, more recent calorimetric data by Dienstbach and Blachnik 6 on the sequence of binaries $GdCl_3 - ACl$ show that the magnitudes of λ^{M} 's are more positive than those expected from eqn. (1); also, the shape of the λ^{M} curves are similar to those of $LaCl_3 - ACl$ or $CeCl_3 - ACl$, with a pronounced broad minimum at $X_{GdCl_3} \leq 0.25$ (A = K, Rb, Cs).

It appears that a better understanding of the systematics of the thermodynamics of the lanthanide chloride – alkali chloride series requires some knowledge of the thermodynamics of binaries containing the end chlorides of the series (i.e., LuCl₃). An alternative to the rare and expensive end members of the lanthanide chloride series is yttrium chloride, having physicochemical properties very similar to those of YbCl₃.⁷

In this paper we report the enthalpies, partial Gibbs energies, and entropies of mixing for YCl₃ – ACl liquid mixtures. The results are compared with data of other LCl₃ – ACl (L=La, Ce, Gd) systems and discussed in terms of the possible melt structures suggested by the recent Raman spectroscopic studies on these systems.⁸

The purpose of this study is to establish the systematics of the thermodynamic and structural properties of the liquid lanthanide chloride—alkali metal chloride mixtures.

EXPERIMENTAL

Yttrium(III) chloride for the calorimetric studies was prepared by dissolving yttrium oxide purchased from A. D. Mackay, Inc. in concentrated HCl. Slow evaporation of the solution gave the hydrated YCl₃, which was dried according to procedures described previously.¹

Yttrium(III) chloride for the emf measurements was prepared by dissolving yttrium oxide from Research Chemicals in concentrated HCl. The hydrated YCl₃ was dried under vacuum at temperatures up to 200 °C. The salt was then treated with gaseous HCl and melted under HCl atmosphere. After this treatment, the melt was filtered through a quartz frit and distilled under vacuum (10⁻⁵ Torr). The source and methods of purifica-

tion of the alkali chlorides were the same as those previously used. ^{1,2} The measurements of the integral enthalpies of mixing were of the "crucible-double breakoff" type, where both liquid salts were contained in fused silica containers. ⁹ The calorimetric apparatus used, its calibration, and the required corrections have been described elsewhere. ¹⁰ The cell used in the emf measurements is similar to the one described in previous papers. ^{11–13} The composition of the glasses and the experimental techniques are given elsewhere. ^{14–16}

By adding small crystals of YCl₃ or ACl in the anode compartment of the cell the composition of the mixture could be changed. One could then either start with a low YCl₃ concentration and add YCl₃ or start with a high YCl₃ concentration and add ACl.

The emf, E, of the cell is related to the chemical potential of the ACl salt in the mixture, $\Delta \mu_{ACl}$, through the equation

$$\Delta \mu_{ACI} = -FE$$

where F is the Faraday constant.

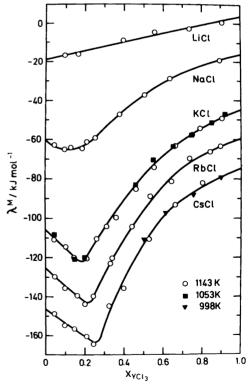


Fig. 1. Enthalpy interaction parameters in liquid mixtures of yttrium(III) chloride with the alkali chlorides.

RESULTS AND DISCUSSION

Fig. 1 presents the results of the liquid-liquid enthalpy of mixing experiments. In Fig. 1, the enthalpy interaction parameters are plotted *versus* mol fraction. The lines shown in the figure represent the "best" curves. The mean deviation of the actual experimental points from the interaction parameter curves is estimated to $\sim \pm 2 \%$.

The enthalpy of mixing becomes more negative with increasing size of the alkali metal cation. For the YCl₃-LiCl binary and at concentrations rich in YCl₃, positive enthalpies of mixing have been observed. The values of the interaction parameter (Fig. 1) decrease sharply from about $+4 \text{ kJ mol}^{-1}$ for the YCl₃-LiCl binary to about -165 kJ mol⁻¹ for the YCl₃-CsCl binary. Within experimental error, the interaction parameters are independent of temperature. All considered systems show more negative values of the interaction parameter in the alkali chloride-rich than in the yttrium chloriderich region. For the mixtures containing CsCl, RbCl, and KCl, distinct minima are found for $\lambda^{\rm M}$ at concentrations $0.2 \le X_{\rm YCl_3} < 0.25$. A broad minimum is also present in the λ^{M} of the YCl₃ – NaCl mixtures, while the data for the λ^{M} of the YCl₃ - LiCl vary linearly with X_{YCl_2} , within experimental

These trends have been observed previously in the studies of other $LCl_3 - ACl^{1.2.6}$ binaries. However, the data for the $YCl_3 - ACl$ binaries are unique in showing both the sharp minima near $X_{YCl_3} \sim 0.25$ and the high energetic asymmetry in the interaction parameter. Similar sharp minima at $X_{ZnCl_2} \sim 0.33$ and high energetic asymmetry have been observed previously for the $ZnCl_2 - CsCl$ binary.

Raman investigations ⁸ have shown that at concentrations of YCl₃, where $X_{YCl_3} < 0.25$, octahedral YCl₆³⁻ ions are present in the melts containing NaCl, KCl, RbCl, or CsCl. The shift of the minimum of $\lambda^{\rm M}$ towards smaller X_{YCl_3} values for the binaries containing RbCl, KCl, and NaCl (Fig. 1) can probably be attributed to the increasing polarizing strength of the solvent cation and/or interactions between YCl₆³⁻ species in these melts. The large volume of the YCl₆³⁻ ion and the large number of Cl⁻ anions associated with the Y³⁺ cation increase the probability of having two of these species as nearest neighbours at concentrations below $X_{YCl_3} = 0.25$. Consequently, the YCl₆³⁻ ions will share chlorides, the octahedra will be distorted,

and Y-Cl interactions will be weakened. These effects are expected to shift the minimum of $\lambda^{\rm M}$ to mol fractions below $X_{\rm YCl_3} = 0.25$. It is worth noting that if one assumes binuclear species like $\rm Y_2Cl_9^{3-}$ in equilibrium with $\rm YCl_6^{3-}$, then the minimum in $\lambda^{\rm M}$ should shift to $\rm X_{\rm YCl_3}$ values higher than 0.25.

The interaction parameter for the lithium chloride—yttrium chloride mixtures varies approximately linearly with composition. As has been argued previously ¹ and shown by the Raman studies, ⁸ the absence of the minimum does not necessarily imply the absence of YCl₆³—configurations from the melt mixtures. The high ionic strength of Li is important in diminishing Y—Cl interactions and thus weakly bonded and probably distorted YCl₆³—configurations are formed.

The validity of eqn. (1) for the YCl₃ – ACl binaries was tested by plotting the enthalpy interaction parameter at different compositions $(X_{YCl_3}=0, 0.25, 0.50, 1)$ as a function of δ_{12} $(r_{Y^3}+=0.88)$. It was found, however, that the data did not fit a smooth, second-order-in- δ_{12} equation. Therefore, it appears that eqn. (1) holds only for the first members of the lanthanide series where the ionic radii of the trivalent cations are very similar and that, as the L³⁺ cation radius is reduced, a more complex equation and/or more complex size parameters are needed. It was found, for example, that the use of a new size parameter

$$\delta_{12}' = \frac{Z_1}{d_1} - \frac{Z_2}{d_2}$$

where Z_1 and Z_2 are the charges of the cations in the binary mixture $(Z_1 = 1, Z_2 = 3)$, yields a smooth, second-order-in δ'_{12} algebraic equation, results which fit all the present interaction parameters.

Tables 1 and 2 present experimental results of the calorimetric and emf measurements. Except for the LiCl system, emf measurements obtained by starting with a high YCl₃ concentration and adding ACl give results slightly different from results obtained by starting with a low YCl₃ concentration and adding YCl₃. Measurements starting with a low YCl₃ concentration were more reproducible than measurements starting with a high YCl₃ concentration. The reason for the difference between the two sets of data are difficult to understand, but since data obtained by adding YCl₃ give higher and more reproducible potentials, we believe that this set of data is the more reliable.

Table 1. Enthalpies of mixing liquid ytterium(III) chloride and alkali chlorides.

System	Mol fraction X_{YCl_3}	Molar enthalpy — ΔH ^M /kJ mol ⁻¹	System	Mol fraction X_{YCl_3}	Molar enthalpy -ΔH ^M /kJ mol ⁻¹
CsCl – YCl ₃	0.047	6.61	CsCl-YCl ₃	0.502	27.67
T = 1148 K	0.098	13.65	T = 998 K	0.614	23.02
	0.149	19.80		0.753	16.41
	0.212	26.75		0.897	7.28
	0.247	30.64			
	0.325	31.94	KCl-YCl ₃	0.045	4.73
	0.400	32.48	$T = 1143 \text{ K}^{\circ}$	0.103	10.59
	0.528	27.46		0.146	14.94
	0.658	20.89		0.212	20.09
	0.801	13.06		0.263	21.39
				0.313	22.35
RbCl-YCl ₃	0.049	6.07		0.363	23.02
T = 1143 K	0.099	12.06		0.463	21.18
	0.161	18.84		0.555	18.29
	0.201	23.15		0.662	14.06
	0.245	25.83		0.749	10.80
	0.333	27.29		0.785	9.17
	0.343	27.04		0.901	4.35
	0.443	25.74			
	0.536	22.06	KCl-YCl ₃	0.048	4.90
	0.644	18.67	$T = 1053 \text{ K}^3$	0.150	15.40
	0.737	13.44		0.201	19.21
	0.843	8.75		0.463	20.68
	0.896	5.94		0.551	17.37
				0.652	14.40
NaCl-YCl ₃	0.047	2.80		0.748	10.84
T = 1143 K	0.0985	5.78		0.851	6.49
	0.130	7.24		0.917	3.56
	0.189	9.88			
	0.211	10.21	LiCl-YCl ₃	0.096	1.47
	0.253	11.18	$T = 1143 \text{ K}^3$	0.166	2.26
	0.377	11.01		0.397	2.09
	0.505	9.25		0.556	1.21
	0.633	6.66		0.735	0.54
	0.890	1.88		0.907	-0.08

In Fig. 2, $\Delta \overline{S}_{ACI}$ is plotted versus X_{YCI_3} for the binaries with A = Li, Na, K, and Rb. The entropies were obtained by combining the partial Gibbs energies calculated from the emf measurements and partial enthalpies calculated from integral data by the method of intercepts. The calculated partial entropies compared within 10% with entropies measured directly by the temperature dependence of the emf. This comparison was made for a few concentrations only. Except for the $YCI_3 - LiCI$ system, the partial entropies show inflection points at YCI_3 concentrations in the region $0.2 \le X_{YCI_3} < 0.25$ and a sharp dependence on composition at

this concentration. Even if the errors in the $\Delta \bar{H}_{ACI}$ values calculated from integral data by the methods of intercepts are relatively great ($\pm 800~\mathrm{J~mol^{-1}}$) the results (Figs. 1 and 2) indicate a definite ordering on the cation lattice, *i.e.*, complex formation, around the composition $X_{YCI_3} = 0.25$.

For the YCl₃ – LiCl system, no minimum occurs in the enthalpy interaction parameter, the partial entropies are more ideal, and the regular solution model seems to fit fairly well. For the YCl₃ – NaCl system, the situation is different from that found for the LaCl₃ – NaCl ¹ and the CeCl₃ – NaCl ² binaries where no significant deviation from regular solution

Table 2. Emf's for the galvanic cell C(s), $\text{Cl}_2(g)|\text{ACl(l)}|\text{A-glass}|\text{YCl}_3(l)-\text{ACl(l)}|\text{Cl}_2(g),\text{C(s)}$.

System	Mol fraction X_{YCl_3}	Emf E/mV	System	Mol fraction X_{YCl_3}	Emf E/mV
RbCl-YCl ₃ ^a	0.098	19	RbCl-YCl ₃	0.199	63
T=1143 K	0.101	16	T = 1143 K	0.248	93
	0.150	39		0.249	94
	0.196	61		0.299	140
	0.206	75		0.349	186
	0.249	115		0.351	175
	0.253	115		0.398	246
	0.303	170		0.400	270
	0.351	220		0.449	290
	0.444	324		0.452	306
	0	521		0.501	370
KCl-YCl ₃ a	0.101	18		0.548	411
T = 1143 K	0.102	18		0.548	415
	0.102	20		0.651	527
	0.156	41		0.654	523
	0.196	65		0.054	223
	0.201	65	KCl-YCl ₃	0.299	146
	0.201	66	T = 1143 K	0.334	172
	0.252	111	1 = 1143 K	0.349	191
	0.300	154		0.400	244
	0.300	157		0.447	278
	0.351	207		0.500	338
	0.403	257		0.547	381
	0.450	304		0.598	427
	0.498	348		0.650	477
	0.476	340		0.696	514
NaCl VCL4	0.006	16			560
NaCl - YCl3a $T = 1103 K$	0.096	16 17		0.741	300
	0.100	17 53	NaCl VCI	0.160	21
	0.197	52	NaCl-YCl ₃	0.150	31
	0.201		T = 1103 K	0.191	46
	0.251	78		0.199	49
	0.295	108		0.200	52
	0.300	108		0.249	75 78
	0.399	175		0.251	78
	0.401	170		0.299	104
	0.499	232		0.300	103
	0.500	236		0.301	108
I:CL VCL4	0.102	12		0.348	134
LiCl—YCl ₃ ^a	0.102	12		0.399	172
T=974 K	0.202	34		0.399	165
	0.300	62		0.400	162
	0.400	96		0.449	197
	0.500	129		0.493	220
ria va	0.050	40		0.500	240
LiCl – YCl ₃	0.250	49		0.501	230
T=974 K	0.349	80		0.543	254
	0.452	111		0.596	290
	0.549	142		0.598	305
	0.640	173		0.601	284
	0.751	215		0.649	315
				0.702	344
				0.787	399

^a Obtained from measurements starting with a low YCl₃ concentration.

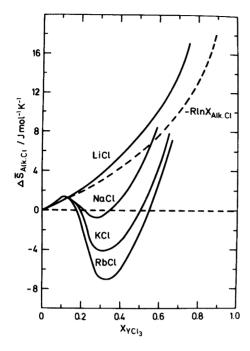


Fig. 2. Partial entropies of mixing of the alkali chlorides in mixtures with yttrium(III) chloride. The dotted line represents the ideal entropies given by $-R \ln X_{ACI}$.

behavior was observed. In the YCl₃-NaCl system, a minimum in the enthalpy interaction parameter is found around $X_{\rm YCl_3}=0.2$ and an inflection point in the curve for partial entropy versus mol fraction is observed at the same composition, an observation which is not surprising since the Y³⁺ ion is significantly smaller than the La³⁺ ion. As expected, these properties in the enthalpy and the partial entropy of mixing are more pronounced in the YCl₃-KCl and YCl₃-RbCl systems. This is consistent with the observations made for the LaCl₃-ACl¹ and MCl₂-ACl (M=Mg, Co, and Mn)^{12,17,18} mixtures and is indicative of the formation of associated species in these melts.

The detailed Raman spectroscopic study ⁸ of the YCl_3-KCl and the YCl_3-CsCl mixtures and the Raman changes occurring on melting the compound Cs_2NaYCl_3 have shown that at concentrations $X_{YCl_3} < 0.25$, octahedral YCl_6^{3-} species are present in these melts. At higher yttrium chloride concentrations, the YCl_6^{3-} octahedra appear to be distorted, sharing edges with each other. This

spectroscopic information reinforces the present thermodynamic data and our conclusions about the ionic geometry in binary YCl₃ – ACl systems.

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