

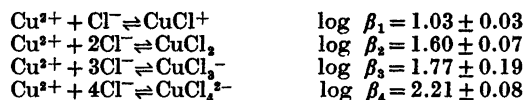
## Stability Constants for Chloride Complexes of Copper(II) in Sulphuric Acid Solution

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Spectrophotometric methods have been used to determine the stability constants of copper(II) chloride complexes in an ionic medium of 9 M sulphuric acid at 25 °C. The total molarity was held constant at 9 M.

Preliminary constants were obtained by graphical methods and were then refined with the generalized least squares program "LETAGROP". The experimental data could best be explained in terms of the following equilibria and stability constants:



The errors given correspond to an error of  $3\sigma$ , where  $\sigma$  is the standard deviation in  $\log \beta$ .

The formation of complexes between copper(II) ions and chloride ions in aqueous solution has mainly been studied by spectrophotometric methods, but a few investigators have used ion exchange or freezing point methods. The formation of complexes between Cu(II) ions and chloride ions cannot be investigated potentiometrically using a copper amalgam electrode or a silver chloride electrode, as both these electrodes reduce Cu(II) to Cu(I) in the presence of chloride ions.

The values of the stability constants (*cf.* Table 1) determined in the various investigations differ from each other, owing to different ionic media and methods of measurement. Some of the constants have been extrapolated to zero ionic strength.<sup>1,3,8,11</sup> From the values given in Table 1, it is evident that the complexes are very weak, the stability constant,  $\beta_1$ , for the

reaction  $\text{Cu}^{2+} + \text{Cl}^- \rightleftharpoons \text{CuCl}^+$  having an approximate value of 1.<sup>1-8,9,11</sup> Some authors have found a higher value for  $\beta_1$ .<sup>7,8,10</sup> This can be attributed to a more concentrated ionic medium, to the neglect of the second complex, or to the method of calculation. The uncertainty of the stability constant,  $\beta_2$ , for the reaction  $\text{Cu}^{2+} + 2\text{Cl}^- \rightleftharpoons \text{CuCl}_2$  is larger than that of  $\beta_1$ , but its value is probably less than 1.<sup>1,2</sup>

It has been claimed that copper(II) forms four mononuclear complexes with chloride ions, namely  $\text{CuCl}^+$ ,  $\text{CuCl}_2$ ,  $\text{CuCl}_3^-$  and  $\text{CuCl}_4^{2-}$ .<sup>1,9,10</sup> On account of the weak complexity, it has, however, proved difficult to determine the stability constants of the higher complexes. Using spectrophotometric measurements, with different metal chlorides as ionic media, Bjerrum<sup>1</sup> was, however, able to determine approximate values for  $\beta_3$  and  $\beta_4$ . The values determined by Morris and Short<sup>10</sup> differ, however, considerably from those determined by Bjerrum.

In this work, the copper(II) chloride system has been studied spectrophotometrically in 9 M sulphuric acid at 25 °C, sulphuric acid being chosen as medium since it seemed likely that the copper(II) complexes would be stronger in 9 M sulphuric acid than in dilute aqueous solution. Sulphuric acid medium has, moreover, industrial interest, since anhydrous chlorides of the transition metals can be obtained by the distillation of such solutions.

Table 1. Survey of reported values for the stability constants of copper(II) chloride complexes.

| Author                      | Ref. | Method    | Medium                             | Temp.<br>°C | $\beta_1$<br>(M <sup>-1</sup> ) | $\beta_2$<br>(M <sup>-2</sup> ) | $\beta_3$<br>(M <sup>-3</sup> ) | $\beta_4$<br>(M <sup>-4</sup> ) |
|-----------------------------|------|-----------|------------------------------------|-------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| Bjerrum                     | 1    | spectr.   | extrap. to 0                       | 22          | 1                               | 0.2                             | $8 \times 10^{-3}$              | $8 \times 10^{-5}$              |
| McConnell<br>and Davidsson  | 2    | spectr.   | 1 M HClO <sub>4</sub>              | 25.2        | 1.3                             | 0.3                             |                                 |                                 |
| Näsänen                     | 3    | spectr.   | extrap. to 0                       | 25          | 1.2                             |                                 |                                 |                                 |
| Kruh                        | 4    | spectr.   | 1 M HClO <sub>4</sub>              | 22          | 0.27                            |                                 |                                 |                                 |
| Lister and<br>Rosenblum     | 5    | spectr.   | 2 M NaClO <sub>4</sub>             | 25          | 1.22                            |                                 |                                 |                                 |
| Andreev and<br>Sapozhinkova | 6    | spectr.   | HCl                                |             | 1                               |                                 |                                 |                                 |
| Libus                       | 11   | spectr.   | extrap. to 0                       | 25          | 1.63                            |                                 |                                 |                                 |
| Faucherre<br>and Crego      | 7    | fp        | sat. KNO <sub>3</sub>              |             | 2.70                            |                                 |                                 |                                 |
| Kenttämää                   | 8    | fp        | sat. KClO <sub>3</sub>             |             | 1.50                            |                                 |                                 |                                 |
|                             |      | fp        | sat. KClO <sub>4</sub>             |             | 4.60                            |                                 |                                 |                                 |
|                             |      |           | extrap. to 0                       |             | 8.90                            |                                 |                                 |                                 |
| Tre'millon                  | 9    | ion exch. | 1.5 M NaNO <sub>3</sub>            |             | 0.4                             |                                 |                                 |                                 |
| Morris<br>and Short         | 10   | ion exch. | 0.69 M HClO <sub>4</sub>           | 20          | 9.6                             | 4.92                            | 3.52                            | 1.0                             |
| Ohlson and<br>Vannerberg    |      | spectr.   | 9 M H <sub>2</sub> SO <sub>4</sub> | 25          | 10.7                            | 39.6                            | 59                              | 163                             |

## EXPERIMENTAL

*Chemicals and analysis.* Stock solutions of copper(II) sulphate were prepared by dissolving copper(II) sulphate (Merck *p.a.*) in 9 M sulphuric acid and the copper content was determined electrogravimetrically.<sup>13</sup> Sulphuric acid was prepared by dilution of conc. sulphuric acid (Merck *p.a.*) and its concentration was calculated from the experimental density,<sup>14</sup> determined with an areometer, graduated from 1.470 to 1.520 g cm<sup>-3</sup> (accuracy  $\pm 0.001$  g cm<sup>-3</sup>). Sodium chloride (Merck *p.a.*) was dried at 110 °C and weighed.

The light absorption measurements in the range 350–385 nm were made with a Beckman spectrophotometer, Model DU-2. The measurements in the ultraviolet range 260–300 nm were made on a Gilford 240 spectrophotometer. Matched quartz cells of path lengths 0.1, 0.2, 0.5, 1.0 cm were employed, these being calibrated before use. During the measurements, the sample compartment was thermostated to 25.0  $\pm$  0.1 °C.

Four series of solutions of copper(II) chloride were prepared by adding accurately weighed sodium chloride to a solution of copper(II) sulphate. In each series, the total copper ion concentration (*B*) was kept constant (*B*: 0.005, 0.010, 0.020, 0.050 M), while the total chloride concentration (*A*) was varied between 0.004 and 0.600 M. The total molarity was held constant at 9 M by the addition of sulphuric acid.

In one and the same series of measurements, *B* and *l* were kept constant and in the different series of measurements the product *lB* was kept constant.<sup>15</sup>

The wave lengths employed, the numbers of solutions and the numbers of measurements are given in Table 2.

Table 2. The wave lengths used, the numbers of solutions and the chloride concentrations.

| Wave lengths<br>(nm)                   | Number of<br>solutions | Number of<br>measured<br>values | Chloride<br>concentration<br>(M) |
|--|------------------------|---------------------------------|----------------------------------|
| 260, 265, 270, 275, 280, 290, 300      | 63                     | 354                             | 0.004–0.064                      |
| 350, 355, 360, 365, 370, 375, 380, 385 | 113                    | 658                             | 0.0192–0.600                     |

## LIST OF SYMBOLS

|              |  |
|--------------|--|
| $A$          | total concentration of chloride ions, $\text{Cl}^-$  |
| $a$          | free » » » » »   |
| $B$          | total » » copper ions, $\text{Cu}^{2+}$  |
| $b$          | free » » » » »   |
| $A_s$        | absorbance   |
| $l$          | optical path length  |
| $\epsilon$   | apparent molar absorptivity  |
| $\beta_i$    | equilibrium constant for the reaction<br>$\text{Cu}^{2+} + i\text{Cl}^- \rightleftharpoons \text{CuCl}_i^{(2-i)+}$ |
| $\epsilon_i$ | molar absorptivity for the complex<br>$\text{CuCl}_i^{(2-i)+}$   |
| $\bar{n}$    | mean ligand number   |

## MEASUREMENTS

The measurements were performed spectrophotometrically, the method of corresponding solutions<sup>1,15-18</sup> being used. In order to find suitable wave lengths, spectra were recorded for copper chloride solutions with constant  $B$  and varying  $A$ . The spectra showed absorption maxima at 250, 375, and 800–900 nm (Figs. 1, 2). The absorption of the  $\text{Cu}^{2+}$  ion, which probably exists as a sulphate complex in the sulphuric acid solution, increases with decreasing wave length in the UV range, and shows an absorption maximum at 810 nm (Fig. 1). The absorption bands of the complexes are displaced towards longer wave lengths with increasing chloride concentrations, their band

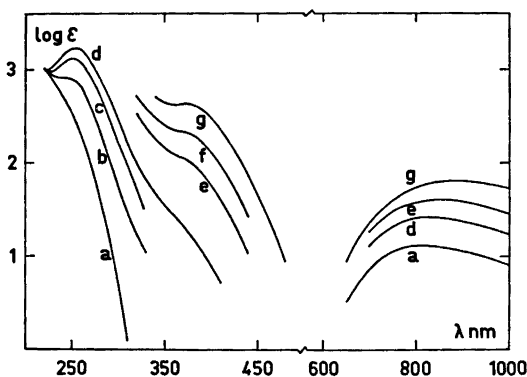


Fig. 1.  $\log \epsilon$  as a function of  $\lambda$  for copper(II) chloride solutions.  $B=0.010$  M and the following values of  $A$  were used: a. 0 M; b. 0.024 M; c. 0.060 M; d. 0.100 M; e. 0.300 M; f. 0.500 M; g. 1.000 M.

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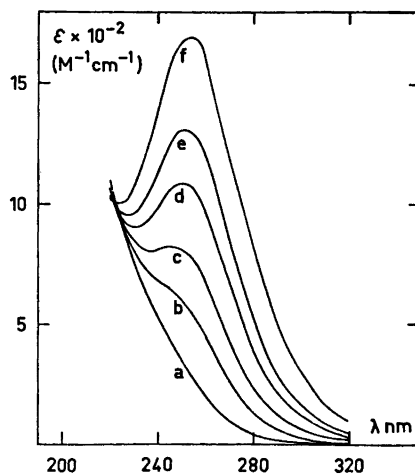


Fig. 2.  $\epsilon$  data as a function of  $\lambda$  for solutions with  $B=0.010$  M and different values of  $A$  a. 0 M; b. 0.012 M; c. 0.024 M; d. 0.044 M; e. 0.060 M; f. 0.100 M.

widths also increasing considerably. Solutions with low  $A$  show one isosbestic point at 224 nm.

The majority of the measurements (658 values) have been carried out in the range 350–385 nm, where the higher complexes can be detected. Another advantage of this range is that the  $\text{Cu}^{2+}$  ion does not absorb there. The remaining 354 measurements were made in the 260–300 nm range (Table 2). Only the stability constants of the two first complexes,  $\text{CuCl}^+$  and  $\text{CuCl}_2$ , could be determined from measurements in the latter range, owing to the strong absorption of both the  $\text{Cu}^{2+}$  ion and the copper(II) chloride complexes. No measurements have been carried out in the 800–900 nm range, because of the small absorptivities of the complexes. The absorption of chloride ions is negligible.

## TREATMENT OF THE DATA

The absorbance,  $A_s$ , of a solution is the product of the apparent molar absorptivity,  $\epsilon$ , the optical path length,  $l$ , and the total concentration of the absorbing substance,  $B$ ,

$$A_s = l\epsilon B = l \sum_{i=0}^N \epsilon_i [BA_i] = l \sum_{i=0}^N \epsilon_i \beta_i b a^i \quad (1)$$

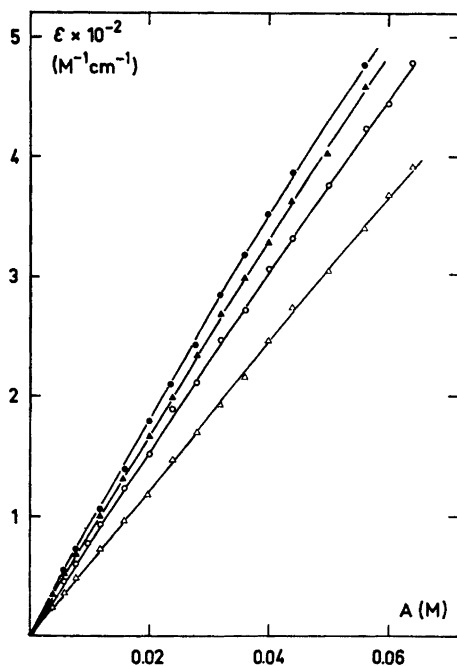


Fig. 3. The function  $\varepsilon(A)$  at different values of  $B$  at 280 nm.  $\triangle B=0.05$  M;  $\circ B=0.02$  M;  $\blacktriangle B=0.01$  M;  $\bullet B=0.005$  M.

where  $\varepsilon_0, \varepsilon_1, \dots, \varepsilon_N$  are the molar absorptivities for  $\text{Cu}^{2+}, \text{CuCl}^+, \dots, \text{CuCl}_N^{(2-N)+}$ , respectively.

The apparent molar absorptivity is defined as

$$\varepsilon = \frac{\sum_{i=0}^N \varepsilon_i [\text{BA}_i]}{B} = \left[ \frac{\sum_{i=0}^N \varepsilon_i \beta_i a^i}{1 + \sum_{i=1}^N \beta_i a^i} \right] \quad (2)$$

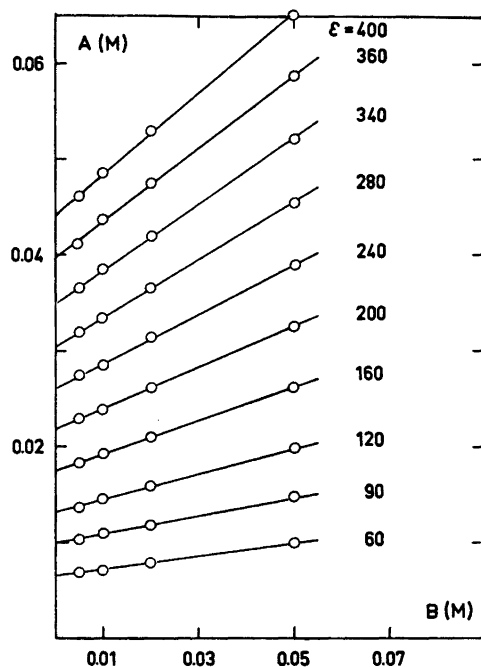


Fig. 4.  $A$  versus  $B$  at different  $\varepsilon$  at 280 nm.

From eqn. (2) it is seen that  $\varepsilon$  is solely a function of  $a$ , if only mononuclear complexes are present. The mean ligand number  $\bar{n}$  is defined as

$$\bar{n} = \frac{A-a}{B} = \left[ \frac{\sum_{i=1}^N i \beta_i a^i}{1 + \sum_{i=1}^N \beta_i a^i} \right] \quad (3)$$

and  $\bar{n}$  is thus only a function of  $a$ , this gives

$$A = a + \bar{n}B \quad (4)$$

Table 3. Corresponding values of  $B, A, a$  and  $\bar{n}$  obtained from the  $\varepsilon(A)$ -curve for  $\lambda=280$  nm.

| $B$ M         | $A$ M  |        |        |        | $a$    | $-\log a$ | $\bar{n}$ |
|---------------|--------|--------|--------|--------|--------|-----------|-----------|
|               | 0.005  | 0.01   | 0.02   | 0.05   |        |           |           |
| $\varepsilon$ |        |        |        |        |        |           |           |
| 60            | 0.0068 | 0.0071 | 0.0079 | 0.0099 | 0.0064 | 2.19      | 0.07      |
| 90            | 0.0103 | 0.0108 | 0.0117 | 0.0148 | 0.0098 | 2.01      | 0.10      |
| 120           | 0.0137 | 0.0145 | 0.0158 | 0.0198 | 0.0132 | 1.88      | 0.13      |
| 160           | 0.0183 | 0.0192 | 0.0211 | 0.0262 | 0.0174 | 1.76      | 0.18      |
| 200           | 0.0229 | 0.0239 | 0.0262 | 0.0325 | 0.0219 | 1.66      | 0.21      |
| 240           | 0.0274 | 0.0286 | 0.0314 | 0.0389 | 0.0261 | 1.58      | 0.26      |
| 280           | 0.0319 | 0.0335 | 0.0366 | 0.0454 | 0.0304 | 1.52      | 0.30      |
| 340           | 0.0388 | 0.0411 | 0.0448 | 0.0554 | 0.0373 | 1.43      | 0.36      |
| 360           | 0.0411 | 0.0437 | 0.0475 | 0.0587 | 0.0398 | 1.40      | 0.38      |
| 400           | 0.0460 | 0.0488 | 0.0531 | 0.0654 | 0.0447 | 1.35      | 0.41      |

Table 4. Corresponding values of  $\log a$  and  $\bar{n}$ , obtained from  $\varepsilon(A)$ -curves for 15 different wave lengths, followed by  $(\bar{n}_{\text{calc}} - \bar{n}) \times 10^3$ , which has been calculated with the "LETAGROP VRID" program.

| $\lambda$ nm | $\log a$ | $\bar{n}$ | $(\bar{n}_{\text{calc}} - \bar{n}) \times 10^3$ | $\lambda$ nm | $\log a$ | $\bar{n}$ | $(\bar{n}_{\text{calc}} - \bar{n}) \times 10^3$ | $\lambda$ nm | $\log a$ | $\bar{n}$ | $(\bar{n}_{\text{calc}} - \bar{n}) \times 10^3$ |
|--------------|----------|-----------|---|--------------|----------|-----------|---|--------------|----------|-----------|---|
| 385          | -0.9340  | 0.93000   | 4.99  | -0.5260      | 1.90000  | -1.29     | 290   | -2.1760      | 0.06800  | 1.73      |   |
|              | -0.878C  | 0.9500C   | 45.53   | -0.4980      | 1.96000  | 23.89     |   | -2.0560      | 0.08800  | 3.31      |   |
|              | -0.8330  | 1.11000   | 13.05   | -0.4740      | 2.04000  | 16.18     |   | -1.967C      | 0.11100  | 0.38      |   |
|              | -0.7930  | 1.17000   | 36.20   | -0.4500      | 2.11000  | 23.39     |   | -1.8880      | 0.12600  | 6.71      |   |
|              | -0.7610  | 1.30000   | -23.49  | -0.4280      | 2.20000  | 2.93      |   | -1.8240      | 0.14500  | 7.81      |   |
|              | -0.7030  | 1.43000   | -17.17  | -0.406C      | 2.29000  | -17.19    |   | -1.7750      | 0.16800  | 2.13      |   |
|              | -0.6560  | 1.60000   | -06.17  | -0.3870      | 2.41000  | -74.73    |   | -1.7280      | 0.18700  | 1.48      |   |
|              | -0.6130  | 1.69000   | -42.68  | -0.3670      | 2.48000  | -83.17    |   | -1.6880      | 0.21000  | -4.45     |   |
|              | -0.5530  | 1.71000   | -6.89   | -0.347C      | 2.50000  | -39.87    |   | -1.6520      | 0.22500  | -2.86     |   |
|              | -0.5750  | 1.78000   | -25.61  | -0.3270      | 2.50000  | -0.19     |   | -1.6160      | 0.24100  | -1.03     |   |
|              | -0.5410  | 1.86000   | -6.15   | -0.3070      | 2.50000  | -4.27     |   | -1.5800      | 0.26500  | -10.24    |   |
|              | -0.511C  | 1.92000   | 24.13   | -0.2870      | 2.50000  | 26.78     |   | -1.5560      | 0.27700  | -4.32     |   |
|              | -0.4840  | 2.00000   | 27.10   | -0.2670      | 2.50000  | 53.34     |   | -1.5300      | 0.29500  | -6.91     |   |
|              | -0.4580  | 2.08000   | 28.23   | -0.2470      | 2.50000  | 1.38      |   | -1.5020      | 0.31000  | -6.43     |   |
|              | -0.4340  | 2.15000   | 33.92   | -0.2270      | 2.50000  | -54.80    |   | -1.4750      | 0.33400  | -13.35    |   |
|              | -0.4100  | 2.20000   | 60.09   | -0.2070      | 2.50000  | -23.61    |   | -1.4470      | 0.35100  | 6.25      |   |
|              | -0.3890  | 2.29000   | 36.90   | -0.1870      | 2.50000  | -35.49    |   | -1.4200      | 0.37900  | -8.22     |   |
|              | -0.3680  | 2.36000   | 33.65   | -0.1670      | 2.50000  | 7.71      |   | -1.4090      | 0.37900  | -8.22     |   |
|              | -0.3490  | 2.48000   | -26.18  | -0.1470      | 2.50000  | -8.59     |   | -1.3920      | 0.35800  | -1.35     |   |
|              | -0.3310  | 2.55000   | -39.54  | -0.1270      | 2.50000  | -23.30    |   | -1.3750      | 0.37000  | -2.74     |   |
|              | -1.2030  | 0.57000   | -8.75   | -0.1070      | 2.50000  | -5.60     |   | -1.3580      | 0.39000  | -1.25     |   |
|              | -1.150C  | 0.66000   | -37.66  | -0.0870      | 2.50000  | 4.94      |   | -1.3410      | 0.39000  | 0.29      |   |
|              | -0.0930  | 0.72000   | -25.00  | -0.0670      | 2.50000  | 28.93     |   | -1.3240      | 0.41000  | 1.20      |   |
|              | -1.0410  | 0.79000   | -23.66  | -0.0470      | 2.50000  | 5.45      |   | -1.3070      | 0.43000  | 2.62      |   |
|              | -0.973C  | 0.80000   | -9.89   | -0.0270      | 2.50000  | 0.03      |   | -1.2900      | 0.45000  | 4.07      |   |
|              | -0.9120  | 0.94000   | 33.42   | -0.0070      | 2.50000  | 12.31     |   | -1.2730      | 0.47000  | 6.89      |   |
|              | -0.8690  | 1.06000   | -7.46   | -0.0070      | 2.50000  | 25.14     |   | -1.2560      | 0.49000  | 6.75      |   |
|              | -0.8280  | 1.12000   | 47.47   | -0.0070      | 2.50000  | -32.53    |   | -1.2390      | 0.51000  | 3.84      |   |
|              | -0.7910  | 1.20000   | 16.50   | -0.0070      | 2.50000  | -24.51    |   | -1.2220      | 0.53000  | 5.35      |   |
|              | -0.7590  | 1.27000   | 11.02   | -0.0070      | 2.50000  | -20.75    |   | -1.2050      | 0.55000  | 3.93      |   |
|              | -0.7330  | 1.36000   | -19.13  | -0.0070      | 2.50000  | -20.19    |   | -1.1880      | 0.57000  | 2.48      |   |
|              | -0.7060  | 1.45000   | -44.51  | -0.0070      | 2.50000  | -23.15    |   | -1.1710      | 0.59000  | -1.34     |   |
|              | -0.6830  | 1.53000   | 57.47   | -0.0070      | 2.50000  | 19.34     |   | -1.1540      | 0.61000  | -3.91     |   |
|              | -0.6410  | 1.63000   | -58.59  | -0.0070      | 2.50000  | 6.79      |   | -1.1370      | 0.63000  | -6.69     |   |
|              | -0.6050  | 1.74000   | -70.51  | -0.0070      | 2.50000  | 32.93     |   | -1.1200      | 0.65000  | -2.90     |   |
|              | -0.5710  | 1.80000   | -34.08  | -0.0070      | 2.50000  | 37.53     |   | -1.1030      | 0.67000  | -2.48     |   |
|              | -0.5390  | 1.88000   | -20.20  | -0.0070      | 2.50000  | 18.76     |   | -1.0860      | 0.69000  | 2.71      |   |
|              | -0.510C  | 1.93000   | 17.11   | -0.0070      | 2.50000  | 21.43     |   | -1.0690      | 0.71000  | -0.23     |   |
|              | -0.4830  | 2.00000   | 36.20   | -0.0070      | 2.50000  | 33.36     |   | -1.0520      | 0.73000  | 4.38      |   |
|              | -0.4590  | 2.10000   | 5.09  | -0.0070      | 2.50000  | 7.65      |   | -1.0350      | 0.75000  | 1.36      |   |
|              | -0.4360  | 2.19000   | -12.41  | -0.0070      | 2.50000  | 6.06      |   | -1.0180      | 0.77000  | -2.73     |   |
|              | -0.4140  | 2.24000   | 7.38  | -0.0070      | 2.50000  | 42.82     |   | -1.0010      | 0.79000  | 0.67      |   |
|              | -0.3930  | 2.33000   | -15.82  | -0.0070      | 2.50000  | 23.29     |   | -0.9840      | 0.81000  | -1.03     |   |
|              | -0.3720  | 2.40000   | 10.95   | -0.0070      | 2.50000  | 15.53     |   | -0.9670      | 0.83000  | 2.44      |   |
|              | -0.3540  | 2.45000   | -11.99  | -0.0070      | 2.50000  | 3.44      |   | -0.9500      | 0.85000  | 1.00      |   |
|              | -0.3350  | 2.54000   | -42.09  | -0.0070      | 2.50000  | -1.19     |   | -0.9330      | 0.87000  | -0.84     |   |
|              | -1.1970  | 0.58000   | -12.10  | -0.0070      | 2.50000  | 3.85      |   | -0.9160      | 0.89000  | -3.00     |   |
|              | -1.0910  | 0.69000   | 7.06  | -0.0070      | 2.50000  | 15.00     |   | -0.8990      | 0.91000  | -4.76     |   |
|              | -1.014C  | 0.83000   | -24.84  | -0.0070      | 2.50000  | 11.62     |   | -0.8820      | 0.93000  | 0.15      |   |
|              | -0.9530  | 0.87500   | 27.87   | -0.0070      | 2.50000  | 29.42     |   | -0.8650      | 0.95000  | -1.26     |   |
|              | -0.9070  | 0.98000   | 2.34  | -0.0070      | 2.50000  | 51.78     |   | -0.8480      | 0.97000  | 0.46      |   |
|              | -0.863C  | 1.06000   | 4.01  | -0.0070      | 2.50000  | 74.67     |   | -0.8310      | 0.99000  | -7.78     |   |
|              | -0.8250  | 1.11000   | 29.27   | -0.0070      | 2.50000  | 4.53      |   | -0.8140      | 1.01000  | -17.95    |   |
|              | -0.7650  | 1.31000   | -44.70  | -0.0070      | 2.50000  | 14.03     |   | -0.7970      | 1.03000  | -2.53     |   |
|              | -0.7140  | 1.40000   | -53.92  | -0.0070      | 2.50000  | 13.44     |   | -0.7800      | 1.05000  | 1.15      |   |
|              | -0.6710  | 1.58000   | -86.98  | -0.0070      | 2.50000  | 27.23     |   | -0.7630      | 1.07000  | 5.52      |   |
|              | -0.6310  | 1.65000   | -51.78  | -0.0070      | 2.50000  | 38.52     |   | -0.7460      | 1.09000  | 3.79      |   |
|              | -0.5940  | 1.71000   | -9.71   | -0.0070      | 2.50000  | 17.54     |   | -0.7290      | 1.11000  | 3.95      |   |
|              | -0.5620  | 1.77000   | 22.03   | -0.0070      | 2.50000  | 7.56      |   | -0.7120      | 1.13000  | 2.17      |   |
|              | -0.5330  | 1.83000   | 47.70   | -0.0070      | 2.50000  | 26.18     |   | -0.6950      | 1.15000  | 0.06      |   |
|              | -0.5040  | 1.91000   | 55.50   | -0.0070      | 2.50000  | 68.34     |   | -0.6780      | 1.17000  | -5.12     |   |
|              | -0.479C  | 2.00000   | 42.62   | -0.0070      | 2.50000  | 18.23     |   | -0.6610      | 1.19000  | -6.61     |   |
|              | -0.4560  | 2.11000   | 4.51  | -0.0070      | 2.50000  | 29.28     |   | -0.6440      | 1.21000  | -7.52     |   |
|              | -0.4340  | 2.20000   | -16.08  | -0.0070      | 2.50000  | -2.97     |   | -0.6270      | 1.23000  | -5.16     |   |
|              | -0.4130  | 2.26000   | 9.45  | -0.0070      | 2.50000  | 10.44     |   | -0.6100      | 1.25000  | -1.91     |   |
|              | -0.3920  | 2.29000   | 27.36   | -0.0070      | 2.50000  | 16.34     |   | -0.5930      | 1.27000  | 1.32      |   |
|              | -0.3730  | 2.30000   | -52.22  | -0.0070      | 2.50000  | -9.66     |   | -0.5760      | 1.29000  | 4.55      |   |
|              | -0.3590  | 2.40000   | 1.52  | -0.0070      | 2.50000  | -13.75    |   | -0.5590      | 1.31000  | 3.48      |   |
|              | -0.3410  | 2.52000   | 3.04  | -0.0070      | 2.50000  | -11.54    |   | -0.5420      | 1.33000  | 4.29      |   |
|              | -0.3200  | 2.62000   | -25.05  | -0.0070      | 2.50000  | 7.56      |   | -0.5250      | 1.35000  | 9.38      |   |
|              | -0.2990  | 2.70000   | -2.14   | -0.0070      | 2.50000  | 0.33      |   | -0.5080      | 1.37000  | -0.22     |   |
|              | -0.2820  | 1.13000   | 7.23  | -0.0070      | 2.50000  | 8.48      |   | -0.4910      | 1.39000  | -17.23    |   |
|              | -0.2760  | 1.21000   | -10.21  | -0.0070      | 2.50000  | 4.57      |   | -0.4740      | 1.41000  | 1.22      |   |
|              | -0.2660  | 1.28000   | -14.70  | -0.0070      | 2.50000  | 8.90      |   | -0.4570      | 1.43000  | 6.48      |   |
|              | -0.248C  | 1.33000   | -5.47   | -0.0070      | 2.50000  | 8.84      |   | -0.4400      | 1.45000  | 7.29      |   |
|              | -0.2310  | 1.38000   | 3.67  | -0.0070      | 2.50000  | 2.03      |   | -0.4230      | 1.47000  | 5.20      |   |
|              | -0.2140  | 1.46000   | -24.98  | -0.0070      | 2.50000  | 2.10      |   | -0.4060      | 1.49000  | 3.27      |   |
|              | -0.2070  | 1.50000   | -9.54   | -0.0070      | 2.50000  | 1.67      |   | -0.3890      | 1.51000  | 6.38      |   |
|              | -0.1930  | 1.53000   | 9.69  | -0.0070      | 2.50000  | 6.67      |   | -0.3720      | 1.53000  | 11.39     |   |
|              | -0.1810  | 1.64000   | -3.68   | -0.0070      | 2.50000  | 5.74      |   | -0.3550      | 1.55000  | 9.16      |   |
|              | -0.1710  | 1.70000   | -19.26  | -0.0070      | 2.50000  | 3.71      |   | -0.3380      | 1.57000  | -1.68     |   |
|              | -0.1650  | 1.73000   | -4.22   | -0.0070      | 2.50000  | 4.68      |   | -0.3210      | 1.59000  | 4.68      |   |
|              | -0.1540  | 1.80000   | 15.44   | -0.0070      | 2.50000  |           |   | -0.3040      | 1.61000  |           |   |

Solutions with the same  $\varepsilon$  have the same value of  $\bar{n}$  and  $a$ , and such solutions are known as corresponding solutions.<sup>1,15-18</sup>

The function  $\varepsilon(A)$ <sup>15</sup> was plotted for three or four given values of the total concentration  $B$ . From these curves pairs of values  $(B, A)$ , corresponding to selected  $\varepsilon$ , were obtained.

If  $A$  was plotted against  $B$  at a constant value of  $\varepsilon$ , a straight line was obtained, indicating that only mononuclear complexes

were present,  $\bar{n}$  being obtained from the slope and  $a$  from the intercept on the  $A$ -axis. Measurements for  $\lambda=280$  nm illustrate this procedure (cf. Figs. 3, 4 and Table 3).

The stability constants were then calculated from the  $\bar{n}(a)$  values by several different methods (cf. Table 4 and Fig. 6).

CALCULATIONS BASED ON THE DATA  $\bar{n} = (Ru + 2u^2)/(1 + Ru + u^2)$  (5)  
 IN THE LOW UV RANGE

Curve fitting. In order to determine values of  $\beta_1$  and  $\beta_2$ , the experimental curve in Fig. 5 was fitted to the following normalized curve:

where  $u = \beta_2 \lambda a$  and  $R = \beta_1 \beta_2^{-1}$ .<sup>19</sup> Functions  $\bar{n}(\log u)_R$  were drawn for different constant  $R$  values and compared with the experimental ones.

Table 5. Spectrophotometric data in the low UV range for 40 solutions.  $A$  and  $B$  are given for each solution, followed by  $\epsilon$ ,  $\epsilon_{\text{calc}}$  and  $\epsilon_{\text{calc}} - \epsilon$  for 7 wave lengths. The concentrations are expressed in  $M$  and the apparent absorptivities in  $M^{-1} \text{ cm}^{-1}$ . Missing data is indicated by  $-1$ .

|          |          |        |         |         |        |         |         |        |
|----------|----------|--------|---------|---------|--------|---------|---------|--------|
| 0.004000 | 0.005000 | C.001  | 34.300  | 34.516  | 0.216  | 81.300  | 80.787  | -0.513 |
| 15.200   | 15.301   | 0.268  | 168.500 | 169.406 | 1.106  | 230.500 | 231.706 | 1.206  |
| 118.700  | 118.968  | 0.268  | 168.500 | 169.406 | 1.106  | 230.500 | 231.706 | 1.206  |
| 304.300  | 304.348  | 0.048  |         |         |        |         |         |        |
| C.000000 | 0.005000 |        |         |         |        |         |         |        |
| 20.200   | 15.920   |        |         |         |        |         |         |        |
| 143.500  | 142.974  | -0.526 | 43.700  | 43.307  | -0.393 | 100.600 | 98.428  | -2.172 |
| 352.000  | 348.822  | -3.178 | 201.700 | 200.827 | -0.873 | 270.200 | 270.532 | -0.668 |
| 0.003000 | 0.005000 |        |         |         |        |         |         |        |
| 24.680   | 24.736   | 0.056  | 52.150  | 52.316  | 0.166  | 116.900 | 116.075 | -0.825 |
| 145.700  | 146.758  | 1.058  | 230.800 | 231.474 | 0.674  | 307.500 | 308.259 | 0.759  |
| 351.200  | 351.840  | 0.640  |         |         |        |         |         |        |
| 0.010000 | 0.005000 |        |         |         |        |         |         |        |
| 29.800   | 29.703   | -0.097 | 61.600  | 61.522  | -0.078 | 134.400 | 133.714 | -0.686 |
| 152.000  | 150.315  | -1.685 | 264.400 | 261.560 | -2.840 | 347.000 | 344.925 | -2.075 |
| 435.000  | 433.452  | -1.548 |         |         |        |         |         |        |
| 0.012000 | 0.005000 |        |         |         |        |         |         |        |
| 34.800   | 34.820   | 0.020  | 71.000  | 70.908  | -0.092 | 151.100 | 151.332 | 0.232  |
| 214.400  | 213.640  | -0.760 | 252.400 | 251.094 | -1.306 | 380.300 | 380.562 | 0.262  |
| 473.200  | 473.720  | 0.520  |         |         |        |         |         |        |
| 0.016000 | 0.005000 |        |         |         |        |         |         |        |
| 44.740   | 45.451   | 0.691  | 89.910  | 90.152  | 0.242  | 185.200 | 186.467 | 1.267  |
| 255.000  | 255.591  | -0.308 | 349.000 | 348.558 | -0.442 | 447.100 | 448.503 | 1.404  |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| 0.020000 | 0.005000 |        |         |         |        |         |         |        |
| 51.500   | 56.540   | -1.360 | 113.400 | 109.923 | -3.477 | -1.000  | -1.000  | C.0    |
| -1.000   | -1.000   | C.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| C.024000 | 0.005000 |        |         |         |        |         |         |        |
| 67.600   | 68.006   | 0.406  | 130.500 | 130.110 | -0.390 | 257.700 | 256.055 | -1.644 |
| 350.200  | 348.631  | -1.569 | 458.600 | 457.371 | -1.229 | 572.600 | 574.532 | 1.932  |
| -1.000   | 0.0      |        |         |         |        |         |         |        |
| C.028000 | 0.005000 |        |         |         |        |         |         |        |
| 78.720   | 75.760   | 1.060  | 148.800 | 150.619 | 1.819  | 288.300 | 290.385 | 2.085  |
| -1.000   | -1.000   | C.0    | -1.000  | -1.000  | C.0    | -1.000  | -1.000  | 0.0    |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| C.032000 | 0.005000 |        |         |         |        |         |         |        |
| 92.900   | 91.801   | -1.099 | 173.000 | 171.365 | -1.635 | -1.000  | -1.000  | 0.0    |
| -1.000   | -1.000   | C.0    | 0.0     | -1.000  | -1.000 | C.0     | -1.000  | 0.0    |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| 0.036000 | 0.005000 |        |         |         |        |         |         |        |
| 15.400   | 14.938   | -0.462 | 24.200  | 23.630  | -0.570 | 79.800  | 78.984  | -0.816 |
| 117.600  | 116.502  | -1.098 | 165.400 | 166.302 | 0.902  | 227.600 | 227.674 | 0.074  |
| 259.400  | 255.718  | -3.682 |         |         |        |         |         |        |
| 0.026000 | 0.010000 |        |         |         |        |         |         |        |
| 19.680   | 19.214   | -0.466 | 42.350  | 41.554  | -0.796 | 97.020  | 95.742  | -1.278 |
| 135.600  | 135.334  | -0.266 | 194.600 | 196.112 | 1.512  | 265.000 | 264.694 | -0.306 |
| 341.700  | 342.148  | 0.448  |         |         |        |         |         |        |
| 0.008000 | 0.010000 |        |         |         |        |         |         |        |
| 23.500   | 23.754   | 0.254  | 50.400  | 50.484  | 0.084  | 112.400 | 112.520 | 0.120  |
| 160.500  | 161.985  | 1.485  | 222.000 | 225.346 | 3.346  | 298.400 | 300.746 | 2.346  |
| 379.200  | 383.289  | 4.089  |         |         |        |         |         |        |
| 0.012000 | 0.010000 |        |         |         |        |         |         |        |
| 32.200   | 32.282   | 0.082  | 68.400  | 68.097  | -0.303 | 146.600 | 146.092 | -0.508 |
| 207.200  | 206.723  | -0.477 | 223.400 | 222.361 | -1.039 | 369.800 | 370.062 | 0.262  |
| 459.600  | 461.875  | 2.275  |         |         |        |         |         |        |
| C.016000 | 0.010000 |        |         |         |        |         |         |        |
| 42.150   | 43.325   | 1.175  | 84.890  | 86.346  | 1.456  | 176.400 | 179.614 | 3.214  |
| -1.000   | -1.000   | C.0    | -1.000  | -1.000  | C.0    | -1.000  | -1.000  | 0.0    |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| C.020000 | 0.010000 |        |         |         |        |         |         |        |
| 53.000   | 53.833   | 0.743  | 105.000 | 105.122 | 0.122  | 211.900 | 213.013 | 1.113  |
| 292.700  | 293.849  | 1.149  | 389.100 | 390.607 | 1.507  | 495.600 | 498.310 | 2.710  |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| 0.024000 | 0.010000 |        |         |         |        |         |         |        |
| 64.000   | 64.709   | 0.709  | 122.800 | 124.229 | 1.429  | 244.300 | 246.225 | 1.925  |
| 323.800  | 326.198  | 2.398  | 439.000 | 442.268 | 3.268  | -1.000  | -1.000  | C.0    |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| 0.028000 | 0.010000 |        |         |         |        |         |         |        |
| 76.200   | 75.899   | -0.301 | 144.100 | 143.681 | -0.419 | 275.600 | 279.196 | 3.596  |
| 371.300  | 371.721  | 0.422  | 492.400 | 492.241 | -0.159 | -1.000  | -1.000  | C.0    |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| 0.032000 | 0.010000 |        |         |         |        |         |         |        |
| 86.520   | 87.348   | 0.828  | 165.000 | 163.701 | -1.299 | 314.300 | 311.679 | -2.621 |
| 420.500  | 416.412  | -4.088 | 542.200 | 540.487 | -1.713 | -1.000  | -1.000  | 0.0    |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| 0.036000 | 0.010000 |        |         |         |        |         |         |        |
| 100.000  | 95.007   | -4.993 | 183.600 | 183.721 | 0.121  | 345.400 | 344.235 | -1.165 |
| 458.000  | 458.268  | 0.268  | -1.000  | -1.000  | C.0    | -1.000  | -1.000  | 0.0    |
| -1.000   | -1.000   | C.0    |         |         |        |         |         |        |
| C.040000 | 0.020000 |        |         |         |        |         |         |        |
| 18.100   | 17.985   | -0.115 | 39.260  | 39.628  | 0.368  | 90.750  | 91.100  | 0.350  |
| 133.800  | 133.030  | -0.770 | 166.500 | 167.520 | 1.020  | 253.400 | 254.542 | 1.142  |
| 331.000  | 330.531  | -0.469 |         |         |        |         |         |        |
| C.044000 | 0.020000 |        |         |         |        |         |         |        |
| 21.800   | 22.070   | 0.270  | 44.000  | 47.332  | 3.332  | 106.000 | 106.363 | 0.363  |
| 153.100  | 153.696  | 0.596  | 212.700 | 214.678 | 1.978  | 285.400 | 287.630 | 2.230  |
| 366.600  | 368.343  | 1.743  |         |         |        |         |         |        |
| 0.048000 | 0.020000 |        |         |         |        |         |         |        |
| 26.600   | 26.299   | -0.301 | 55.010  | 55.200  | 0.190  | 122.700 | 121.656 | -1.044 |
| 174.600  | 176.235  | 1.635  | 241.100 | 241.052 | -0.048 | 321.300 | 319.571 | -1.729 |
| 406.000  | 405.154  | -0.846 |         |         |        |         |         |        |

Table 5. Continued.

|          |          |        |         |         |        |         |         |        |  |
|----------|----------|--------|---------|---------|--------|---------|---------|--------|--|
| 0.012000 | 0.020000 |        |         |         |        |         |         |        |  |
| 31.070   | 30.638   | -0.432 | 63.480  | 63.243  | -0.237 | 136.700 | 136.971 | -1.729 |  |
| 154.500  | 154.641  | -0.141 | 268.200 | 267.057 | -1.143 | 353.200 | 351.584 | -1.616 |  |
| 442.800  | 440.554  | -1.606 |         |         |        |         |         |        |  |
| 0.016300 | 0.020000 |        |         |         |        |         |         |        |  |
| 39.840   | 39.682   | -0.158 | 80.050  | 79.750  | -0.300 | 168.500 | 167.629 | -0.871 |  |
| 225.700  | 235.945  | -0.655 | 320.800 | 317.977 | -2.822 | 415.600 | 412.698 | -2.901 |  |
| 512.100  | 505.867  | -2.232 |         |         |        |         |         |        |  |
| 0.029000 | 0.020000 |        |         |         |        |         |         |        |  |
| 48.550   | 45.145   | 0.555  | 96.570  | 96.770  | 0.200  | 197.600 | 198.279 | 0.679  |  |
| 273.700  | 274.882  | 1.182  | 367.800 | 367.476 | -0.324 | 471.400 | 471.114 | -0.286 |  |
| 575.100  | 575.173  | 0.073  |         |         |        |         |         |        |  |
| 0.024000 | 0.020000 |        |         |         |        |         |         |        |  |
| 55.440   | 58.973   | -0.467 | 116.400 | 114.226 | -2.174 | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    |         |         |        |         |         |        |  |
| 0.028000 | 0.020000 |        |         |         |        |         |         |        |  |
| 68.370   | 65.115   | 0.745  | 132.100 | 132.051 | -0.049 | 257.400 | 259.340 | 1.941  |  |
| 352.100  | 352.775  | 0.675  | 462.200 | 462.358 | 0.158  | 581.500 | 580.377 | -1.122 |  |
| 694.900  | 695.864  | 0.964  |         |         |        |         |         |        |  |
| 0.032000 | 0.020000 |        |         |         |        |         |         |        |  |
| 79.920   | 79.528   | -0.392 | 151.700 | 150.182 | -1.518 | 292.300 | 289.662 | -2.638 |  |
| 395.000  | 390.801  | -1.199 | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    |         |         |        |         |         |        |  |
| 0.036000 | 0.020000 |        |         |         |        |         |         |        |  |
| 88.550   | 90.171   | 1.621  | 165.700 | 168.561 | 2.861  | 317.800 | 319.792 | 1.993  |  |
| 425.900  | 428.198  | 2.298  | 550.900 | 551.999 | 1.100  | 680.500 | 680.366 | -0.133 |  |
| -1.000   | -1.000   | 0.0    |         |         |        |         |         |        |  |
| 0.040000 | 0.030000 |        |         |         |        |         |         |        |  |
| 12.296   | 12.370   | 0.080  | 28.540  | 28.884  | 0.344  | 68.850  | 69.240  | 0.390  |  |
| 103.400  | 103.124  | -0.276 | 147.300 | 148.839 | 1.539  | 203.900 | 205.658 | 2.158  |  |
| 273.500  | 274.358  | 0.858  |         |         |        |         |         |        |  |
| 0.046000 | 0.050000 |        |         |         |        |         |         |        |  |
| 15.300   | 15.397   | 0.097  | 34.260  | 34.699  | 0.439  | 81.230  | 81.159  | -0.071 |  |
| 118.900  | 115.477  | -0.577 | 168.000 | 170.272 | 2.272  | 229.400 | 232.538 | 3.138  |  |
| 301.700  | 305.303  | 3.603  |         |         |        |         |         |        |  |
| 0.050000 | 0.050000 |        |         |         |        |         |         |        |  |
| 18.640   | 18.521   | -0.119 | 40.440  | 40.644  | 0.204  | 94.360  | 93.131  | -1.229 |  |
| 136.000  | 135.791  | -0.209 | 151.000 | 151.516 | 0.516  | 258.800 | 258.994 | 0.195  |  |
| 335.900  | 335.627  | -0.273 |         |         |        |         |         |        |  |
| 0.054000 | 0.050000 |        |         |         |        |         |         |        |  |
| 25.630   | 25.052   | -0.578 | 52.600  | 52.905  | 0.305  | 117.600 | 117.216 | -0.384 |  |
| 168.600  | 168.288  | -0.312 | 233.300 | 233.437 | 0.137  | 309.600 | 310.662 | 1.062  |  |
| 393.300  | 394.573  | 1.273  |         |         |        |         |         |        |  |
| 0.058000 | 0.050000 |        |         |         |        |         |         |        |  |
| 32.440   | 31.935   | -0.505 | 65.530  | 65.627  | -0.303 | 142.100 | 141.461 | -0.639 |  |
| 262.600  | 260.596  | -2.004 | 277.500 | 274.600 | -2.892 | 362.400 | 360.713 | -1.687 |  |
| 453.000  | 451.316  | -1.684 |         |         |        |         |         |        |  |
| 0.062000 | 0.050000 |        |         |         |        |         |         |        |  |
| 39.290   | 39.141   | -0.149 | 77.720  | 78.769  | 1.049  | 162.700 | 165.834 | 3.134  |  |
| 236.100  | 232.695  | -2.595 | 311.700 | 315.036 | 3.336  | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    |         |         |        |         |         |        |  |
| 0.064000 | 0.050000 |        |         |         |        |         |         |        |  |
| 47.290   | 46.645   | -0.645 | 94.380  | 92.294  | -2.085 | 191.900 | 190.305 | -1.595 |  |
| 265.700  | 264.568  | -1.132 | 358.800 | 354.727 | -4.073 | 459.400 | 456.161 | -3.239 |  |
| 559.100  | 556.506  | -2.594 |         |         |        |         |         |        |  |
| 0.068000 | 0.050000 |        |         |         |        |         |         |        |  |
| 54.760   | 54.422   | -0.338 | 106.800 | 106.168 | -0.632 | 215.100 | 214.845 | -0.255 |  |
| 295.000  | 296.159  | 1.200  | 354.200 | 393.688 | -0.512 | 501.900 | 501.653 | -0.247 |  |
| -1.000   | -1.000   | 0.0    |         |         |        |         |         |        |  |
| 0.072000 | 0.050000 |        |         |         |        |         |         |        |  |
| 62.520   | 62.490   | -0.070 | 119.700 | 120.357 | 0.657  | 239.300 | 239.427 | 0.127  |  |
| 324.900  | 327.574  | 2.675  | 430.000 | 431.927 | 1.927  | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    |         |         |        |         |         |        |  |
| 0.076000 | 0.050000 |        |         |         |        |         |         |        |  |
| 69.386   | 70.704   | 1.324  | 132.500 | 134.829 | 2.329  | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    |         |         |        |         |         |        |  |

The best fit was obtained when  $R=1.5$  and  $\log u=1$  and  $\log a=1.83$  (cf. Fig. 5). This gave  $\beta_1=10.1 \text{ M}^{-1}$  and  $\beta_2=45.7 \text{ M}^{-2}$ .

#### "LETAGROP" CALCULATIONS

The experimental data from the low UV-range were also processed with the spectrophotometric version "SPEFO" of the "LETAGROP" program.<sup>22</sup>  $U$  is the error squares sum, defined as  $U = \sum (\epsilon_{\text{calc}} - \epsilon)^2$ .

The "best values" for  $\beta_1$  and  $\beta_2$  obtained were:

$$\beta_1 = 11.60 \pm 0.22 \text{ M}^{-1}$$

$$\beta_2 = 39.17 \pm 6.21 \text{ M}^{-2}$$

and  $U=490.2$  for 231 values for  $A < 0.04 \text{ M}$ . The errors given are  $\sigma$ , where  $\sigma$  is the standard deviation in  $\beta$ . The corresponding  $\epsilon_1$  and  $\epsilon_2$

values are given in Table 7 and Fig. 8. These  $\epsilon_1$  and  $\epsilon_2$  values were also confirmed by graphical methods. In Table 5 experimental and calculated data are presented.

#### CALCULATIONS BASED ON THE COMPLETE DATA SET

*Fronæus' method.*<sup>17,20</sup> The function used was

$$\bar{n} = \frac{d\phi_0/\phi_0}{da/a} = \frac{d \ln \phi_0}{d \ln a} \quad (6)$$

Integrating (6) between the limits 0 and  $a_i$ , gives

$$\ln \phi_0(a_i) = \int_0^{a_i} \bar{n} d \ln a \quad (7)$$

$\phi_0$  is determined from eqn. (7).

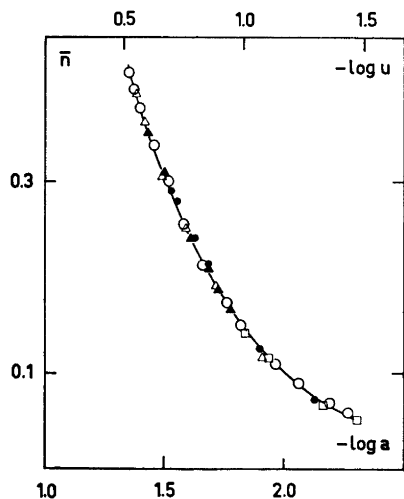


Fig. 5.  $\bar{n}$  as a function of  $\log a$  in the UV range.  $\triangle$  300 nm;  $\blacktriangle$  290 nm;  $\circ$  280 nm;  $\bullet$  270 nm;  $\square$  260 nm.

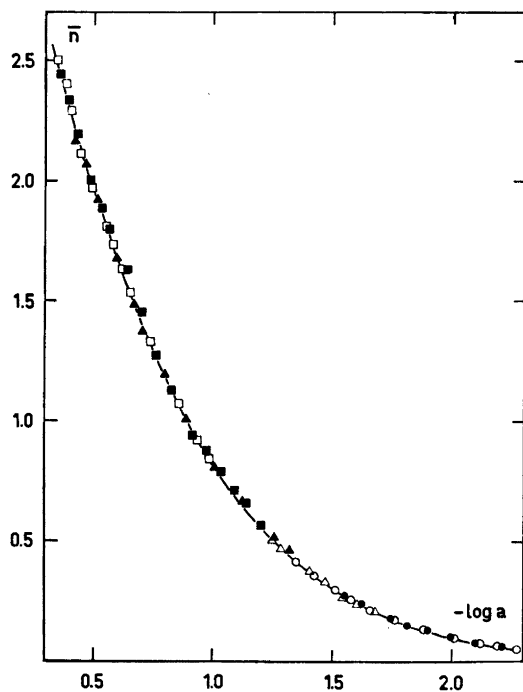


Fig. 6. The function  $\bar{n}(\log a)$  at different wave lengths.  $\circ$  280 nm;  $\bullet$  300 nm,  $\triangle$  350 nm;  $\blacktriangle$  360 nm;  $\square$  370 nm;  $\blacksquare$  380 nm.

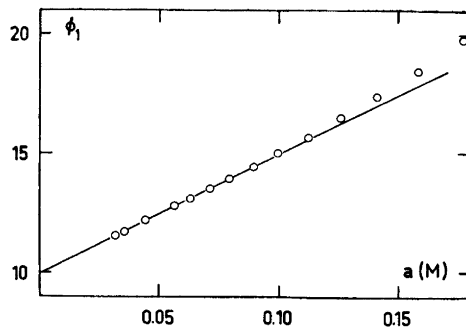


Fig. 7a.  $\phi_1$  as a function of  $a$ .

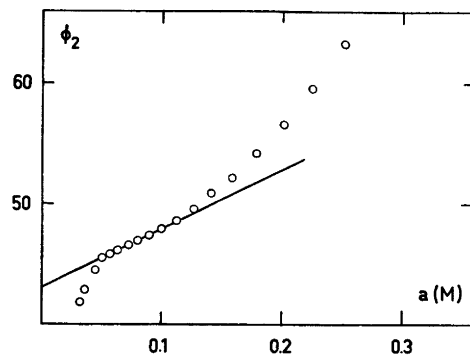


Fig. 7b.  $\phi_2$  as a function of  $a$ .

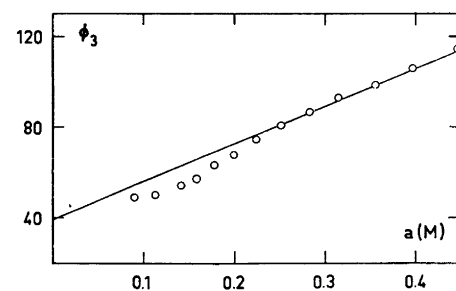


Fig. 7c.  $\phi_3$  as a function of  $a$ .

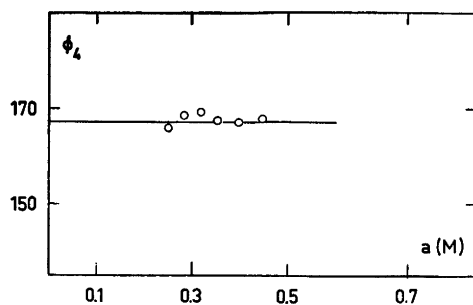


Fig. 7d.  $\phi_4$  as a function of  $a$ .



Table 6. The intercepts and the slopes of the different graphical functions for the calculation of the  $\beta$ -values.

|                              | Function       | Intercept | Slope | $\beta_1$<br>(M <sup>-1</sup> ) | $\beta_2$<br>(M <sup>-2</sup> ) | $\beta_3$<br>(M <sup>-3</sup> ) | $\beta_4$<br>(M <sup>-4</sup> ) |
|------------------------------|----------------|-----------|-------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| All data                     | $\phi_1$       | 10        | 50    |                                 |                                 |                                 |                                 |
|                              | $\phi_2$       | 43        | 49    |                                 |                                 |                                 |                                 |
|                              | $\phi_3$       | 39        | 167   | 10                              | 43                              | 39                              | 167                             |
|                              | $\phi_4$       | 167       | —     |                                 |                                 |                                 |                                 |
| Data in the range 350–385 nm | $\phi_1$       | 11.5      | 42.5  |                                 |                                 |                                 |                                 |
|                              | $\phi_2$       | 40.5      | 43    |                                 |                                 |                                 |                                 |
|                              | $\phi_3$       | 46        | 177   | 11.5                            | 40.5                            | 46                              | 177                             |
|                              | $\phi_4$       | 177       | —     |                                 |                                 |                                 |                                 |
| All data                     | F <sub>1</sub> | 10        | 46    |                                 |                                 |                                 |                                 |
|                              | F <sub>2</sub> | 36        | 75    |                                 |                                 |                                 |                                 |
|                              | F <sub>3</sub> | 41.5      | 161   | 10                              | 36                              | 42                              | 161                             |
|                              | F <sub>4</sub> | 161       | —     |                                 |                                 |                                 |                                 |
| All data                     | G <sub>2</sub> | 43        | 38    |                                 |                                 |                                 |                                 |
|                              | G <sub>3</sub> | 43        | 11    | 11                              | 38                              | 43                              | —                               |

$$\phi_1 = \frac{\phi_0 - 1}{a} = \beta_1 + \beta_2 a \left( + \sum_{i=3}^N \beta_i a^{i-1} \right) \quad (8) \quad F_1 = \frac{\bar{n}}{(1-\bar{n})a} = \beta_1 + \beta_2 \frac{2-\bar{n}}{1-\bar{n}} a +$$

$$\sum_{i=3}^N \frac{i-\bar{n}}{1-\bar{n}} \beta_i a^{i-1} \quad (9)$$

At very low values of  $a$ , the first two complexes,  $BA$  and  $BA_2$ , predominate, and the function  $\phi_1(a)$  becomes a straight line of slope  $\beta_2$  and with intercept  $\beta_1$ . A value of any constant  $\beta_i$  may be obtained by using a generalization of eqn. (8).

The disadvantage of this method is that any errors in the values of  $\beta_1, \dots, \beta_{i-1}$  will accumulate in the value of  $\beta_i$ .

In Figs. 7a–d, the different functions  $\phi_i(a)$  have been plotted, and the slopes and intercepts of these four functions are listed in Table 6. The approximate values of the stability constants obtained were:

$$\begin{array}{ll} \beta_1 = 10 \text{ M}^{-1} & \beta_3 = 39 \text{ M}^{-3} \\ \beta_2 = 43 \text{ M}^{-2} & \beta_4 = 167 \text{ M}^{-4} \end{array}$$

The values of the constants based on the 350–385 nm data, only, were somewhat different. This can be attributed to the selection of the tail of the  $\bar{n}(\log a)$  curve. The values obtained were:

$$\begin{array}{ll} \beta_1 = 11.5 \text{ M}^{-1} & \beta_3 = 46 \text{ M}^{-3} \\ \beta_2 = 40.5 \text{ M}^{-2} & \beta_4 = 177 \text{ M}^{-4} \end{array}$$

(cf. Table 6).

Rossotti's method.<sup>21</sup> The function

may be derived from eqn. (3). The plot of  $\bar{n}(1-\bar{n})/a$  against  $(2-\bar{n})a/(1-\bar{n})$  becomes a straight line of slope  $\beta_2$  and intercept  $\beta_1$ , as  $a \rightarrow 0$ .

A value of any constant  $\beta_i$  may be obtained by using a generalization of eqn. (9).

The slopes and the intercepts of the four functions  $F_i$  are given in Table 6. The following values of the stability constants were obtained:

$$\begin{array}{ll} \beta_1 = 10 \text{ M}^{-1} & \beta_3 = 42 \text{ M}^{-3} \\ \beta_2 = 36 \text{ M}^{-2} & \beta_4 = 161 \text{ M}^{-4} \end{array}$$

The reciprocal method of Rossotti.<sup>21</sup> The constants may also be obtained by extrapolation to  $a^{-1} = 0$ , using the function

$$G_N = \frac{\bar{n}a^{-N}}{N-\bar{n}} = \beta_N + \beta_{N-1} \frac{N-1-\bar{n}}{N-\bar{n}} a^{-1} + \sum_{i=1}^{N-2} \frac{i-\bar{n}}{N-\bar{n}} \beta_i a^{i-N} \quad (10)$$

In this case no value can be obtained for  $\beta_4$  (cf. Table 6). The values obtained were:

$$\begin{array}{ll} \beta_1 = 11 \text{ M}^{-1} & \beta_3 = 43 \text{ M}^{-3} \\ \beta_2 = 38 \text{ M}^{-2} & \end{array}$$

Table 7. Molar absorptivities,  $\epsilon_i$ , in  $M^{-1} \text{ cm}^{-1}$  calculated with the "LETAGROP" program. The errors given are  $\sigma$ , where  $\sigma$  is the standard deviation in  $\epsilon$ .

| $\lambda$ nm | $\epsilon_0$ | $\epsilon_1$  | $\epsilon_2$   | $\epsilon_3$ | $\epsilon_4$ |
|--------------|--------------|---------------|----------------|--------------|--------------|
| 260          | 210.9        | 2417 $\pm$ 10 | 1754 $\pm$ 199 | —            | —            |
| 265          | 150.6        | 2055 $\pm$ 7  | 2164 $\pm$ 111 | —            | —            |
| 270          | 105.4        | 1597 $\pm$ 7  | 2926 $\pm$ 100 | —            | —            |
| 275          | 70.3         | 1190 $\pm$ 5  | 3083 $\pm$ 67  | —            | —            |
| 280          | 45.6         | 847 $\pm$ 5   | 2913 $\pm$ 64  | —            | —            |
| 290          | 17.7         | 390 $\pm$ 4   | 2276 $\pm$ 53  | —            | —            |
| 300          | 6.6          | 195 $\pm$ 2   | 1434 $\pm$ 28  | —            | —            |
| 350          | —            | 8.8 $\pm$ 0.7 | 171 $\pm$ 3    | 222 $\pm$ 18 | 513 $\pm$ 15 |
| 355          | —            | 5.9 $\pm$ 0.6 | 157 $\pm$ 2    | 190 $\pm$ 16 | 503 $\pm$ 13 |
| 360          | —            | 4.1 $\pm$ 0.6 | 145 $\pm$ 2    | 141 $\pm$ 12 | 533 $\pm$ 8  |
| 365          | —            | 2.5 $\pm$ 0.4 | 129 $\pm$ 2    | 122 $\pm$ 13 | 534 $\pm$ 9  |
| 370          | —            | 1.0 $\pm$ 0.4 | 114 $\pm$ 2    | 110 $\pm$ 11 | 536 $\pm$ 7  |
| 375          | —            | 0.9 $\pm$ 0.4 | 98 $\pm$ 2     | 85 $\pm$ 12  | 549 $\pm$ 8  |
| 380          | —            | 0.6 $\pm$ 0.3 | 84 $\pm$ 2     | 62 $\pm$ 12  | 550 $\pm$ 8  |
| 385          | —            | 0.5 $\pm$ 0.3 | 71 $\pm$ 2     | 47 $\pm$ 13  | 530 $\pm$ 9  |

Table 8. Spectrophotometric data in the range 350–385 nm for 11 solutions and 8 wave lengths.  $A$  and  $B$  are given for each solution, followed by  $\epsilon$ ,  $\epsilon_{\text{calc}}$ , and  $\epsilon_{\text{calc}} - \epsilon$ . The concentrations are expressed in  $M$  and the apparent absorptivities in  $M^{-1} \text{ cm}^{-1}$ .  $\beta_1 = 10.7 M^{-1}$  and  $\beta_2 = 39.6 M^{-2}$  were kept constant during the calculation.

|          |          |        |       |       |        |       |       |        |  |
|----------|----------|--------|-------|-------|--------|-------|-------|--------|--|
| 0.019200 | 0.010000 |        |       |       |        |       |       |        |  |
| 3.200    | 3.176    | -0.024 | 2.550 | 2.554 | 0.004  | 2.050 | 2.085 | 0.035  |  |
| 1.650    | 1.668    | 0.018  | 1.250 | 1.317 | 0.067  | 1.100 | 1.101 | 0.001  |  |
| 0.850    | 10.842   | 0.032  | 0.650 | 0.714 | 0.064  |       |       |        |  |
| C.C250CC | C.010000 |        |       |       |        |       |       |        |  |
| 4.750    | 4.769    | C.019  | 3.850 | 3.914 | 0.064  | 3.300 | 3.241 | -0.059 |  |
| 2.600    | 2.647    | 0.047  | 2.100 | 2.150 | C.C5C  | 1.800 | 1.797 | -0.003 |  |
| 1.400    | 1.448    | 0.048  | 1.100 | 1.169 | 0.065  |       |       |        |  |
| C.C320CC | 0.010000 |        |       |       |        |       |       |        |  |
| 6.750    | 6.551    | -0.195 | 5.650 | 5.453 | -0.197 | 4.750 | 4.561 | -0.189 |  |
| 3.850    | 3.776    | -0.074 | 3.150 | 3.123 | -0.027 | 2.650 | 2.610 | -0.040 |  |
| 2.150    | 2.111    | -0.039 | 1.700 | 1.702 | 0.002  |       |       |        |  |
| 0.038400 | C.010000 |        |       |       |        |       |       |        |  |
| 8.600    | 8.463    | -0.137 | 7.250 | 7.138 | -0.112 | 6.050 | 6.014 | -0.036 |  |
| 5.050    | 5.028    | -0.022 | 4.250 | 4.212 | -0.038 | 3.600 | 3.520 | -0.080 |  |
| 2.900    | 2.853    | -0.047 | 2.300 | 2.298 | -0.002 |       |       |        |  |
| 0.020400 | 0.020000 |        |       |       |        |       |       |        |  |
| 3.040    | 3.057    | 0.017  | 2.440 | 2.454 | 0.014  | 2.000 | 2.000 | 0.000  |  |
| 1.600    | 1.567    | -0.033 | 1.300 | 1.257 | -0.043 | 1.100 | 1.052 | -0.048 |  |
| 0.850    | 0.842    | -0.008 | 0.700 | 0.682 | -0.018 |       |       |        |  |
| 0.027000 | 0.020000 |        |       |       |        |       |       |        |  |
| 4.540    | 4.600    | 0.060  | 3.690 | 3.768 | 0.078  | 3.040 | 3.116 | 0.076  |  |
| 2.540    | 2.541    | C.C01  | 2.040 | 2.059 | 0.019  | 1.700 | 1.721 | 0.021  |  |
| 1.400    | 1.386    | -0.014 | 1.150 | 1.120 | -0.030 |       |       |        |  |
| 0.034000 | 0.020000 |        |       |       |        |       |       |        |  |
| 6.400    | 6.331    | -0.069 | 5.300 | 5.263 | -0.037 | 4.450 | 4.397 | -0.053 |  |
| 3.750    | 3.635    | -0.115 | 3.100 | 3.002 | -0.098 | 2.550 | 2.509 | -0.041 |  |
| 2.100    | 2.028    | -0.072 | 1.750 | 1.635 | -0.115 |       |       |        |  |
| C.C400CC | C.020000 |        |       |       |        |       |       |        |  |
| 8.230    | 8.218    | -0.012 | 6.950 | 6.966 | -0.084 | 5.890 | 5.813 | -0.077 |  |
| 4.890    | 4.855    | -0.035 | 4.140 | 4.061 | -0.075 | 3.440 | 3.394 | -0.046 |  |
| 2.750    | 2.750    | -0.040 | 2.240 | 2.215 | -0.025 |       |       |        |  |
| 0.020000 | C.C500CC |        |       |       |        |       |       |        |  |
| 2.050    | 2.168    | 0.118  | 1.660 | 1.709 | 0.049  | 1.270 | 1.374 | 0.104  |  |
| 1.030    | 1.075    | 0.045  | 0.830 | 0.822 | -0.008 | 0.640 | 0.667 | 0.047  |  |
| C.54C    | 6.547    | 0.007  | 0.440 | 0.444 | 0.004  |       |       |        |  |
| 0.040000 | C.050000 |        |       |       |        |       |       |        |  |
| 5.690    | 5.841    | 0.151  | 4.760 | 4.828 | 0.068  | 3.930 | 4.032 | 0.102  |  |
| 3.240    | 3.322    | 0.082  | 2.650 | 2.731 | 0.081  | 2.160 | 2.283 | 0.123  |  |
| 1.770    | 1.844    | C.C74  | 1.470 | 1.487 | 0.017  |       |       |        |  |
| 0.060000 | 0.050000 |        |       |       |        |       |       |        |  |
| 10.330   | 10.536   | 0.206  | 8.760 | 8.939 | 0.175  | 7.430 | 7.574 | 0.144  |  |
| 6.300    | 6.380    | C.C80  | 5.310 | 5.396 | 0.086  | 4.430 | 4.508 | 0.078  |  |
| 3.590    | 3.661    | 0.071  | 2.900 | 2.946 | 0.046  |       |       |        |  |

## THE "LETAGROP" CALCULATIONS

The values obtained by the different graphical methods were refined using the computer program "LETAGROP VRID".<sup>23</sup> The "best values" for  $\beta_1$ ,  $\beta_2$ ,  $\beta_3$ , and  $\beta_4$  obtained were:

$$\beta_1 = 10.69 \pm 0.25 M^{-1} \quad \beta_3 = 58.53 \pm 8.37 M^{-3}$$

$$\beta_2 = 39.60 \pm 2.10 M^{-2} \quad \beta_4 = 163.3 \pm 9.66 M^{-4}$$

and  $U = \sum (\bar{n}_{\text{calc}} - \bar{n})^2 = 0.13946$ . 246  $\bar{n}(\log a)$ -values were used. The errors given are  $\sigma$ , where  $\sigma$  is the standard deviation in  $\beta$ .



Table 9. Continued.

|          |          |        |         |         |        |         |         |        |  |
|----------|----------|--------|---------|---------|--------|---------|---------|--------|--|
| 0.230400 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 88.900  | 89.687  | 0.787  |  |
| 81.800   | 82.583   | 0.783  | 75.500  | 76.301  | 0.801  | -1.000  | -1.000  | 0.0    |  |
| 62.800   | 63.336   | 0.536  | 56.100  | 56.706  | 0.606  |         |         |        |  |
| 0.240000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 95.600  | 94.709  | -0.891 |  |
| 87.800   | 88.418   | -0.382 | 81.000  | 80.995  | -0.005 | 76.900  | 76.446  | -0.354 |  |
| 67.900   | 67.646   | -0.254 | 60.700  | 60.724  | 0.024  |         |         |        |  |
| 0.243200 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 96.000  | 96.389  | 0.389  |  |
| 88.000   | 89.239   | 1.039  | 82.200  | 82.571  | 0.371  | 75.600  | 75.970  | 0.370  |  |
| 68.800   | 69.101   | 0.301  | 61.600  | 62.082  | 0.482  |         |         |        |  |
| 0.256000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.300   | 0.0    | -1.000  | -1.000  | 0.0    | 102.400 | 103.132 | 0.732  |  |
| 95.200   | 95.559   | 0.359  | 88.400  | 88.927  | 0.527  | -1.000  | -1.000  | 0.0    |  |
| 76.600   | 75.002   | 0.402  | 67.300  | 67.606  | 0.306  |         |         |        |  |
| 0.268800 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    | 95.100  | 95.352  | 0.252  | 87.900  | 88.401  | 0.501  |  |
| 80.600   | 81.021   | 0.421  | 73.100  | 73.234  | 0.134  |         |         |        |  |
| 0.270000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 111.100 | 110.535 | -0.565 |  |
| 103.100  | 102.744  | -0.356 | 96.100  | 95.957  | -0.143 | 89.500  | 88.993  | -0.507 |  |
| 82.100   | 81.590   | -0.510 | 74.200  | 73.789  | -0.410 |         |         |        |  |
| 0.285000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 119.200 | 118.479 | -0.721 |  |
| 110.800  | 110.483  | -0.317 | 103.600 | 103.556 | -0.044 | 96.600  | 96.440  | -0.160 |  |
| 89.000   | 88.703   | -0.220 | 80.600  | 80.561  | -0.039 |         |         |        |  |
| 0.300000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 127.000 | 126.414 | -0.586 |  |
| 119.200  | 118.240  | -0.960 | 111.800 | 111.201 | -0.599 | 106.600 | 103.967 | -0.633 |  |
| 96.400   | 96.375   | -0.325 | 87.600  | 87.453  | -0.147 |         |         |        |  |
| 0.315000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 133.600 | 134.319 | 0.719  |  |
| 125.200  | 125.395  | 0.795  | -1.000  | -1.000  | 0.0    | 112.100 | 111.547 | -0.553 |  |
| -1.000   | -1.000   | 0.0    | 95.100  | 96.439  | -0.661 |         |         |        |  |
| 0.330000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.300   | 0.0    | -1.000  | -1.000  | 0.0    | 142.500 | 142.175 | -0.325 |  |
| 131.700  | 132.764  | 0.026  | 127.000 | 126.559 | -0.471 | 118.400 | 119.155 | 0.755  |  |
| 110.900  | 110.880  | -0.020 | 101.800 | 101.494 | -0.306 |         |         |        |  |
| 0.345000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.300   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| 141.000  | 141.414  | 0.414  | 134.900 | 134.173 | -0.730 | 126.600 | 126.770 | 0.370  |  |
| 118.200  | 118.339  | 0.139  | 108.800 | 108.593 | -0.207 |         |         |        |  |
| 0.360000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 158.200 | 157.674 | -0.526 |  |
| 148.800  | 149.043  | 0.243  | 141.800 | 141.770 | -0.030 | 134.400 | 134.369 | -0.031 |  |
| 126.500  | 125.805  | -0.695 | 116.200 | 115.714 | -0.486 |         |         |        |  |
| 0.375000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 164.900 | 165.288 | 0.388  |  |
| 156.700  | 156.595  | -0.105 | 149.200 | 149.311 | 0.111  | 142.100 | 141.934 | -0.166 |  |
| 133.300  | 133.258  | -0.042 | 122.700 | 122.834 | 0.134  |         |         |        |  |
| 0.390000 | 0.010000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 173.100 | 172.795 | -0.305 |  |
| 162.600  | 164.060  | 1.460  | 157.000 | 156.718 | -0.222 | 150.500 | 149.447 | -1.053 |  |
| 141.400  | 140.678  | -0.722 | 130.600 | 129.937 | -0.663 |         |         |        |  |
| 0.081600 | 0.020000 |        |         |         |        |         |         |        |  |
| 23.200   | 23.174   | -0.026 | 20.500  | 20.416  | -0.084 | 17.900  | 18.081  | 0.181  |  |
| -1.000   | -1.300   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    |         |         |        |  |
| 0.095200 | 0.020000 |        |         |         |        |         |         |        |  |
| 29.100   | 28.992   | -0.108 | 25.800  | 25.701  | -0.099 | 22.700  | 22.859  | 0.159  |  |
| 19.800   | 20.050   | 0.250  | 17.300  | 17.437  | 0.137  | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    |         |         |        |  |
| 0.108000 | 0.030000 |        |         |         |        |         |         |        |  |
| 35.400   | 35.121   | -0.279 | 31.500  | 31.291  | -0.209 | 27.800  | 27.937  | 0.137  |  |
| 24.500   | 24.649   | 0.149  | 21.600  | 21.602  | 0.002  | 18.700  | 18.912  | 0.212  |  |
| 16.200   | 16.304   | 0.104  | -1.000  | -1.000  | 0.0    |         |         |        |  |
| 0.122400 | 0.020000 |        |         |         |        |         |         |        |  |
| 41.200   | 41.513   | 0.313  | 36.900  | 37.141  | 0.241  | 33.200  | 33.277  | 0.077  |  |
| 29.400   | 29.520   | 0.120  | 26.000  | 26.052  | 0.052  | 22.800  | 22.904  | 0.104  |  |
| 19.700   | 19.846   | 0.146  | 16.800  | 17.086  | 0.286  |         |         |        |  |
| 0.136000 | 0.020000 |        |         |         |        |         |         |        |  |
| 47.600   | 48.126   | 0.526  | 42.800  | 43.215  | 0.415  | 38.700  | 38.851  | 0.151  |  |
| 34.500   | 34.638   | 0.138  | 30.600  | 30.765  | 0.165  | 27.000  | 27.170  | 0.170  |  |
| 23.500   | 23.664   | 0.164  | 20.200  | 20.467  | 0.267  |         |         |        |  |
| 0.149600 | 0.020000 |        |         |         |        |         |         |        |  |
| 55.100   | 54.929   | -0.171 | 49.800  | 49.681  | -0.319 | 45.000  | 44.634  | -0.366 |  |
| 40.400   | 39.982   | -0.418 | 36.000  | 35.725  | -0.275 | 31.900  | 31.697  | -0.203 |  |
| 28.000   | 27.751   | -0.249 | 24.300  | 24.115  | -0.185 |         |         |        |  |
| 0.163200 | 0.020000 |        |         |         |        |         |         |        |  |
| 62.200   | 61.891   | -0.309 | 56.200  | 55.914  | -0.286 | 51.000  | 50.607  | -0.393 |  |
| 46.000   | 45.536   | -0.464 | 41.200  | 40.917  | -0.283 | 36.800  | 36.475  | -0.325 |  |
| 32.500   | 32.131   | -0.399 | 28.300  | 28.025  | -0.275 |         |         |        |  |
| 0.176800 | 0.020000 |        |         |         |        |         |         |        |  |
| 69.200   | 68.985   | -0.215 | 62.600  | 62.489  | -0.111 | 56.900  | 56.748  | -0.152 |  |
| 51.800   | 51.280   | -0.520 | 46.800  | 46.323  | -0.477 | 41.900  | 41.491  | -0.409 |  |
| 37.300   | 36.703   | -0.597 | 32.600  | 32.191  | -0.409 |         |         |        |  |
| 0.190400 | 0.020000 |        |         |         |        |         |         |        |  |
| 76.000   | 76.188   | 0.188  | 69.200  | 69.185  | -0.015 | 63.000  | 63.041  | 0.041  |  |
| 57.200   | 57.198   | -0.002 | 51.700  | 51.928  | 0.228  | 46.500  | 46.731  | 0.231  |  |
| 41.200   | 41.548   | 0.348  | 36.700  | 36.602  | -0.098 |         |         |        |  |
| 0.204000 | 0.020000 |        |         |         |        |         |         |        |  |
| 84.600   | 83.479   | -0.521 | 76.400  | 75.981  | -0.419 | 69.900  | 69.466  | -0.434 |  |
| 63.700   | 63.275   | -0.425 | -1.000  | -1.000  | 0.0    | 52.400  | 52.182  | -0.218 |  |
| -1.000   | -1.000   | 0.0    | 41.800  | 41.248  | -0.552 |         |         |        |  |
| 0.217600 | 0.020000 |        |         |         |        |         |         |        |  |
| 90.900   | 90.835   | -0.065 | 83.200  | 82.857  | -0.343 | 76.000  | 76.008  | 0.008  |  |
| 69.600   | 69.491   | -0.109 | 63.600  | 63.670  | 0.070  | 57.700  | 57.827  | 0.127  |  |
| 51.900   | 51.909   | 0.009  | 46.400  | 46.115  | -0.285 |         |         |        |  |
| 0.231200 | 0.020000 |        |         |         |        |         |         |        |  |
| 98.500   | 98.237   | -0.263 | 89.800  | 89.794  | -0.006 | 82.500  | 82.648  | 0.148  |  |
| 75.800   | 75.832   | 0.032  | 70.000  | 69.773  | -0.227 | 63.700  | 63.650  | -0.050 |  |
| 57.400   | 57.396   | -0.004 | 51.600  | 51.190  | -0.410 |         |         |        |  |

Table 9. Continued.

|          |          |        |         |         |        |         |         |        |  |
|----------|----------|--------|---------|---------|--------|---------|---------|--------|--|
| 0.244800 | 0.020000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 93.500  | 89.370  | -1.130 |  |
| 83.400   | 82.279   | -1.121 | 76.600  | 76.006  | -0.594 | 70.300  | 69.634  | -0.666 |  |
| 63.900   | 63.066   | -0.834 | 57.100  | 56.455  | -0.645 |         |         |        |  |
| 0.258400 | 0.020000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 97.000  | 96.158  | -0.842 |  |
| 89.500   | 86.916   | -0.684 | 82.900  | 82.354  | -0.546 | 76.100  | 75.760  | -0.340 |  |
| 69.500   | 68.900   | -0.600 | 62.400  | 61.895  | -0.505 |         |         |        |  |
| 0.272000 | 0.020000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| 96.500   | 95.425   | -1.075 | 89.400  | 88.797  | -0.603 | 82.500  | 82.011  | -0.489 |  |
| 75.400   | 74.881   | -0.519 | 67.800  | 67.490  | -0.310 |         |         |        |  |
| 0.285600 | 0.020000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    | 95.600  | 95.318  | -0.282 | 88.400  | 88.369  | -0.031 |  |
| 80.800   | 80.989   | 0.189  | 73.400  | 73.224  | -0.176 |         |         |        |  |
| 0.360000 | 0.020000 |        |         |         |        |         |         |        |  |
| 169.000  | 167.532  | -1.468 | 156.800 | 155.561 | -1.239 | 146.300 | 147.408 | 1.108  |  |
| 139.400  | 138.888  | -0.512 | 132.000 | 131.657 | -0.343 | 124.100 | 124.262 | 0.162  |  |
| 115.600  | 115.881  | 0.281  | 105.700 | 106.252 | 0.552  |         |         |        |  |
| 0.390000 | 0.020000 |        |         |         |        |         |         |        |  |
| 181.700  | 182.766  | 1.066  | 169.300 | 170.199 | 0.899  | 162.200 | 162.223 | 0.023  |  |
| 152.600  | 153.552  | 0.953  | 145.400 | 146.271 | 0.871  | 137.600 | 138.881 | 1.281  |  |
| 128.700  | 130.248  | 1.548  | 118.600 | 119.957 | 1.357  |         |         |        |  |
| 0.420000 | 0.020000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 177.700 | 176.691 | -1.009 |  |
| 168.900  | 167.940  | -0.960 | 161.300 | 160.667 | -0.633 | 154.500 | 153.367 | -1.133 |  |
| 144.900  | 144.557  | -0.343 | 133.700 | 133.654 | -0.046 |         |         |        |  |
| 0.140000 | 0.050000 |        |         |         |        |         |         |        |  |
| 38.200   | 38.183   | -0.017 | 34.000  | 34.091  | 0.091  | 30.600  | 30.490  | -0.110 |  |
| 27.000   | 26.974   | -0.026 | 23.700  | 23.721  | 0.021  | 20.700  | 20.809  | 0.109  |  |
| 17.800   | 17.983   | 0.183  | -1.000  | -1.000  | 0.0    |         |         |        |  |
| 0.120000 | 0.050000 |        |         |         |        |         |         |        |  |
| 30.600   | 30.431   | -0.169 | 27.200  | 27.012  | -0.188 | 23.700  | 24.047  | 0.347  |  |
| 20.800   | 21.123   | 0.323  | 18.000  | 18.406  | 0.406  | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    |         |         |        |  |
| 0.100000 | 0.050000 |        |         |         |        |         |         |        |  |
| 23.400   | 23.190   | -0.210 | 20.400  | 20.431  | 0.031  | 17.800  | 18.094  | 0.294  |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    |         |         |        |  |
| 0.160000 | 0.050000 |        |         |         |        |         |         |        |  |
| 46.200   | 46.362   | 0.162  | 41.900  | 41.592  | -0.308 | 37.600  | 37.358  | -0.242 |  |
| 33.700   | 33.285   | -0.415 | 29.400  | 29.497  | 0.097  | 26.200  | 26.018  | -0.182 |  |
| 22.500   | 22.633   | 0.130  | 19.300  | 19.549  | 0.249  |         |         |        |  |
| 0.180000 | 0.050000 |        |         |         |        |         |         |        |  |
| 35.100   | 34.894   | -0.206 | 49.600  | 49.449  | -0.151 | 45.000  | 44.604  | -0.396 |  |
| 40.400   | 39.955   | -0.445 | 36.000  | 35.700  | -0.300 | 31.900  | 31.673  | -0.227 |  |
| 28.000   | 27.730   | -0.270 | 24.200  | 24.096  | -0.104 |         |         |        |  |
| 0.200000 | 0.050000 |        |         |         |        |         |         |        |  |
| 64.100   | 63.720   | -0.380 | 57.900  | 57.607  | -0.293 | 52.300  | 52.185  | -0.115 |  |
| 47.100   | 47.008   | -0.091 | 42.600  | 42.299  | -0.301 | 38.000  | 37.754  | -0.246 |  |
| 33.500   | 33.271   | -0.229 | 29.200  | 29.082  | -0.118 |         |         |        |  |
| 0.220000 | 0.050000 |        |         |         |        |         |         |        |  |
| 73.200   | 72.786   | -0.414 | 66.400  | 66.620  | 0.220  | 60.400  | 60.161  | -0.239 |  |
| 54.400   | 54.392   | -0.008 | 49.800  | 49.266  | -0.534 | 44.400  | 44.237  | -0.163 |  |
| 39.400   | 39.238   | -0.162 | 34.700  | 34.495  | -0.205 |         |         |        |  |
| 0.240000 | 0.050000 |        |         |         |        |         |         |        |  |
| 81.200   | 82.045   | 0.845  | 73.600  | 74.643  | 1.043  | 67.800  | 68.199  | 0.399  |  |
| 61.600   | 62.073   | 0.473  | 56.600  | 56.569  | -0.031 | 51.200  | 51.099  | -0.101 |  |
| 45.400   | 45.610   | -0.090 | 40.600  | 40.320  | -0.280 |         |         |        |  |
| 0.260000 | 0.050000 |        |         |         |        |         |         |        |  |
| 92.000   | 91.453   | -0.547 | 83.800  | 83.435  | -0.365 | 77.000  | 76.560  | -0.440 |  |
| 70.200   | 70.018   | -0.182 | 64.400  | 64.176  | -0.224 | 58.200  | 58.308  | 0.108  |  |
| 52.400   | 52.361   | -0.039 | 46.700  | 46.533  | -0.167 |         |         |        |  |
| 0.280000 | 0.050000 |        |         |         |        |         |         |        |  |
| 101.000  | 100.968  | -0.032 | 92.300  | 92.358  | 0.058  | 84.700  | 85.112  | 0.412  |  |
| 77.600   | 78.192   | 0.592  | 71.500  | 72.051  | 0.551  | 65.400  | 65.833  | 0.433  |  |
| 59.200   | 59.462   | 0.262  | 53.100  | 53.105  | 0.005  |         |         |        |  |
| 0.300000 | 0.050000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 93.900  | 93.819  | -0.081 |  |
| 86.200   | 86.553   | 0.360  | 79.800  | 80.161  | 0.361  | 73.000  | 73.640  | 0.640  |  |
| 66.400   | 66.878   | 0.478  | 59.500  | 60.007  | 0.507  |         |         |        |  |
| 0.320000 | 0.050000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| 94.700   | 95.089   | 0.389  | 88.300  | 88.468  | 0.168  | 81.400  | 81.692  | 0.292  |  |
| 74.500   | 74.575   | 0.075  | 66.700  | 67.294  | 0.594  |         |         |        |  |
| 0.360000 | 0.050000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| -1.000   | -1.000   | 0.0    | 105.000 | 105.533 | 0.533  | 97.700  | 98.383  | 0.683  |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    |         |         |        |  |
| 0.420000 | 0.050000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 147.600 | 147.488 | -0.112 |  |
| 138.700  | 138.967  | 0.267  | 131.900 | 131.736 | -0.164 | 124.400 | 124.341 | -0.059 |  |
| 116.100  | 115.957  | -0.143 | 106.700 | 106.325 | -0.375 |         |         |        |  |
| 0.440000 | 0.050000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 155.900 | 156.392 | 0.492  |  |
| 147.600  | 147.773  | 0.173  | 141.600 | 140.503 | -1.097 | 134.000 | 133.101 | -0.899 |  |
| 125.500  | 124.558  | -0.942 | 115.500 | 114.523 | -0.977 |         |         |        |  |
| 0.460000 | 0.050000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 165.400 | 165.217 | -0.183 |  |
| 157.500  | 156.525  | -0.975 | 143.000 | 142.000 | -1.000 | 141.700 | 141.862 | 0.162  |  |
| 132.900  | 133.187  | 0.287  | 123.200 | 122.767 | -0.433 |         |         |        |  |
| 0.480000 | 0.050000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | -1.000  | -1.000  | 0.0    |  |
| 164.800  | 165.200  | 0.400  | 157.100 | 157.920 | 0.820  | 149.600 | 150.598 | 0.998  |  |
| -1.000   | -1.000   | 0.0    | 130.400 | 131.027 | 0.627  |         |         |        |  |
| 0.500000 | 0.050000 |        |         |         |        |         |         |        |  |
| -1.000   | -1.000   | 0.0    | -1.000  | -1.000  | 0.0    | 183.400 | 182.544 | -0.856 |  |
| 174.900  | 173.778  | -1.122 | 166.900 | 166.522 | -0.378 | 159.000 | 159.281 | 0.281  |  |
| 150.700  | 150.417  | -0.283 | -1.000  | -1.000  | 0.0    |         |         |        |  |

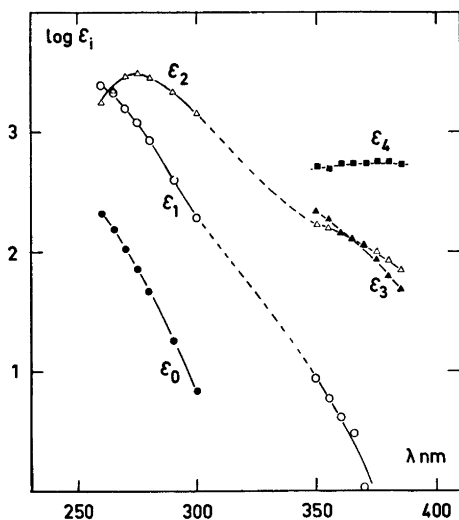


Fig. 8. The  $\log \epsilon_i$  values obtained from the "LETAGROP" program.  $\epsilon_0$  measured directly.

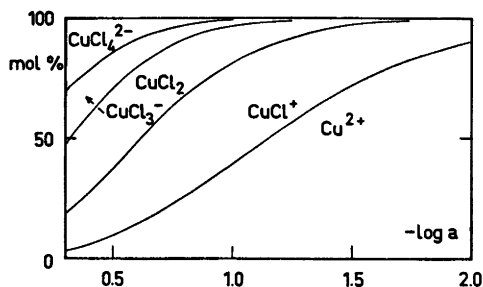


Fig. 9. The distribution of copper(II) chloride complexes as a function of  $\log a$  for  $B = 0.010$  M.

The values of the stability constants were determined from the  $\bar{n}(\log a)$ -curve by means of the program "LETAGROP VRID".<sup>23</sup> The values of the constants were then inserted in the "SPEFO" version to calculate the  $\epsilon_i$  values. The program requires that  $\epsilon_1$  is determined. By inserting the values of  $\beta_1$  and  $\beta_2$  and processing the experimental data obtained at low chloride ion concentration ( $A < 0.06$  M), it was possible to obtain approximate values for  $\epsilon_1$  in the range 350–385 nm.  $\epsilon_1$  was then fixed, and  $\epsilon_2$ ,  $\epsilon_3$ , and  $\epsilon_4$  were calculated (cf. Table 7). All the  $\epsilon_i$  values were then fixed, and the stability constants were calculated with the "SPEFO" program in the range 370–385 nm (cf. Table 10). The values for  $\beta_1$ ,  $\beta_2$ ,  $\beta_3$  and  $\beta_4$  obtained were:

$$\begin{aligned} \beta_1 &= 10.43 \pm 0.42 \text{ M}^{-1} & \beta_3 &= 56.54 \pm 2.13 \text{ M}^{-3} \\ \beta_2 &= 39.13 \pm 0.92 \text{ M}^{-2} & \beta_4 &= 160.0 \pm 4.86 \text{ M}^{-4} \end{aligned}$$

and  $U = 67.55$  for 274 values for  $A \leq 0.5$  M. The errors given are  $\sigma$ , where  $\sigma$  is the standard deviation. The errors are probably underestimated since it was necessary to hold the  $\epsilon_i$  values constant during the calculation. The experimental data, which were processed with the "SPEFO" program are presented in Tables 8 and 9.

## RESULTS AND DISCUSSION

The refinement of the constants thus gave the following values which are regarded as being the "best values":

$$\begin{aligned} \log \beta_1 &= 1.03 \pm 0.03 & \log \beta_3 &= 1.77 \pm 0.19 \\ \log \beta_2 &= 1.60 \pm 0.07 & \log \beta_4 &= 2.21 \pm 0.08 \end{aligned}$$

Table 10. Survey of the values for the stability constants,  $\beta$ , obtained by the different methods of calculation.

| Calculation method          | $\beta_1$<br>(M <sup>-1</sup> ) | $\beta_2$<br>(M <sup>-2</sup> ) | $\beta_3$<br>(M <sup>-3</sup> ) | $\beta_4$<br>(M <sup>-4</sup> ) |
|-----------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| Curve fitting               | 10.1                            | 45.7                            | —                               | —                               |
| LETAGROP "SPEFO"            | 11.6 ± 0.2                      | 39.2 ± 6.2                      | —                               | —                               |
| Fronæus' method             | 10                              | 43                              | 39                              | 167                             |
|                             | 11.5                            | 41                              | 46                              | 177                             |
| Rosotti's method            | 10                              | 36                              | 42                              | 161                             |
| Rosotti's reciprocal method | 11                              | 38                              | 43                              | —                               |
| LETAGROP VRID               | 10.7 ± 0.3                      | 39.6 ± 2.1                      | 59 ± 8                          | 163 ± 10                        |
| LETAGROP "SPEFO"            | 10.4 ± 0.4                      | 39.1 ± 0.9                      | 57 ± 2                          | 160 ± 5                         |

These were obtained from the "LETAGROP VRID" calculations based on the  $\bar{n}(\log a)$  data (cf. Table 10).

The errors given are  $3\sigma$ , where  $\sigma$  is the standard deviation in  $\log \beta$ . The third complex shows a greater error than the others. In Fig. 9 a distribution curve has been drawn from the above values of the constants. The narrow band of existence for the third complex shows that it only exists in comparatively small quantities.

The recorded spectra show absorption bands at 250, 375, and 800–900 nm. According to Andreev *et al.*<sup>6</sup> and Eswein *et al.*,<sup>12</sup> the absorption band at 250 nm indicates the formation of the lower complexes at these low concentrations. The absorption bands at 375 nm and 800–900 nm should indicate  $\text{CuCl}_4^{2-}$ . The fourth complex also absorbs in the low UV range.

The different  $\epsilon_i$  values have been calculated with the "LETAGROP" program (cf. Fig. 8). The maximum for  $\text{CuCl}_2$  is at 275 nm, which is in accordance with Andreev *et al.* The molar absorptivity,  $\epsilon_4$ , for  $\text{CuCl}_4^{2-}$  at 375 nm is about  $530 \text{ M}^{-1} \text{ cm}^{-1}$  which agrees with the findings of Eswein *et al.*<sup>12</sup> The value of  $\epsilon_2$  (approximately  $100 \text{ M}^{-1} \text{ cm}^{-1}$ ) is also similar to the value calculated by Eswein *et al.*

The coordination of the  $\text{Cu}^{2+}$  ion in aqueous solution is tetragonally distorted octahedral, and of  $\text{CuCl}_4^{2-}$  probably distorted tetrahedral. As can be seen from Fig. 8, the absorption maximum at 375 nm is characteristic for the  $\text{CuCl}_4^{2-}$  complex, only. Thus there is evidence that this complex has a different symmetry from the lower ones. However, it should be borne in mind that, although only  $\text{CuCl}_4^{2-}$  has an absorption maximum at 375 nm, the absorptivities of the other complexes cannot be neglected.

It is obvious that the stepwise stability constants in sulphuric acid solution are greater by a factor of 10 than those obtained in perchlorate medium. Without a knowledge of the entropies and heats of formation of the complexes in the perchlorate and sulphuric acid media, it is not worthwhile to speculate on the reason for this.

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