

Normal Coordinate Analysis of Azulene

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A normal coordinate analysis was performed for azulene. A harmonic force field, potential energy distribution, and calculated mean amplitudes of vibration are reported. The results agree reasonably well with previously given electron diffraction mean amplitude values. The mean amplitudes of vibration are shortly discussed in relation to the partial aromatic character of azulene.

Several structural and spectral investigations on cyclic hydrocarbons have been reported in the last years. Davis and Muecke¹ have reported an electron diffraction study of cyclopentene, and Adams *et al.*² have performed similar work on cyclopentane. An investigation of spiropentane has been reported by Dallinga *et al.*³ Electron diffraction works on the six-membered ring molecules cyclohexene, 1,3-cyclohexadiene, and 1,4-cyclohexadiene are reported by various authors.⁴⁻⁸ Recently published spectral data and normal coordinate analysis for these three molecules are also available.⁹⁻¹² Hagen in his thesis¹³ has thoroughly treated the structural aspects of 1,3-cycloheptadiene, bicyclo[4.1.0]-2-heptene and bicyclopropyl on the basis of gas electron diffraction works. Structural and spectroscopic data for 1,3-cycloheptadiene are also available.¹⁴⁻¹⁵ Among the other cyclic hydrocarbons treated by electron diffraction are bicyclo[1.1.1]pentane,¹⁶⁻¹⁸ bicyclo[2.1.0]pentane,¹⁹ 1,3,5,7-cyclooctatetraene,²⁰⁻²³ 1,3-cyclooctadiene,²⁴ and perylene.²⁵⁻²⁶ Almenningen *et al.*²⁷ have reported an electron diffraction study on the aromatic molecules naphthalene, anthracene, and coronene. Spectroscopic calculations of mean amplitudes have been performed for benzene,²⁸ naphthalene,²⁹ and anthracene.²⁹ For benzene some earlier electron diffraction analyses are available.^{20,30,31}

The azulene molecule has been investigated several times, both structurally³² and spectroscopically.³³⁻³⁶ In the present work a normal coordinate analysis is carried out for this molecule, and mean amplitudes of vibration are calculated. Some comments are finally given on the interesting correlation between the aromatic character of the molecule and the mean amplitudes of vibration.

SYMMETRY COORDINATES

According to Bastiansen and Derrisen³² azulene possesses C_{2v} symmetry. Fig. 1 shows the molecular model. The following set of symmetry coordinates were constructed by the method described by Wilson *et al.*³⁷

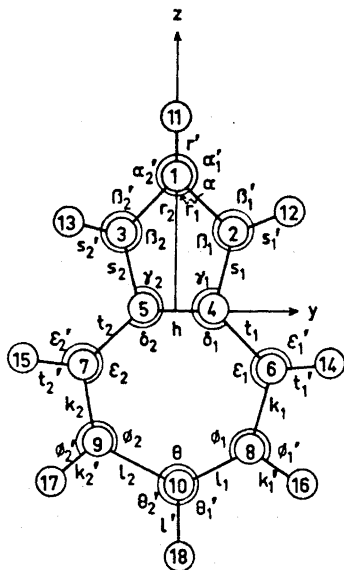


Fig. 1. Molecular model of azulene. In-plane valence coordinates are indicated. The out-of-plane coordinates (not indicated on the figure) are specified below in terms of the respective atom numbers. (i) Torsions: τ_{r_1} (3-1-2-4), τ_{r_2} (2-1-3-5), τ_{k_1} (10-8-6-4), τ_{k_2} (10-9-7-5), τ_{l_1} (9-10-8-6), τ_{l_2} (8-10-9-7); (ii) out-of-plane bendings: ξ_1 (7,3-5-4), ξ_2 (6,2-4-5), β_1'' (4,1-2-12), β_2'' (5,1-3-13), ε_1'' (8,4-6-14), ε_2'' (9,5-7-15), ϕ_1'' (10,6-8-16), ϕ_2'' (10,7-9-17), α'' (2,3-1-11), θ'' (8,9-10-18). The capital letters $R, S, R', S', etc.$, are used to designate the appropriate equilibrium distances.

Species A_1 :

$$\begin{aligned}
 S_1 &= 2^{-\frac{1}{2}}(r_1 + r_2), \quad S_2 = 2^{-\frac{1}{2}}(s_1 + s_2), \quad S_3 = 2^{-\frac{1}{2}}(t_1 + t_2) \\
 S_4 &= h, \quad S_5 = 2^{-\frac{1}{2}}(k_1 + k_2), \quad S_6 = 2^{-\frac{1}{2}}(l_1 + l_2) \\
 S_7 &= (RS/2)^{\frac{1}{2}}(\beta_1 + \beta_2), \quad S_8 = (HT/2)^{\frac{1}{2}}(\delta_1 + \delta_2), \quad S_9 = (TK/2)^{\frac{1}{2}}(\varepsilon_1 + \varepsilon_2) \\
 S_{10} &= r', \quad S_{11} = 2^{-\frac{1}{2}}(s_1' + s_2'), \quad S_{12} = 2^{-\frac{1}{2}}(t_1' + t_2') \\
 S_{13} &= 2^{-\frac{1}{2}}(k_1' + k_2'), \quad S_{14} = l', \quad S_{15} = (RS/2)^{\frac{1}{2}}(\beta_1' + \beta_2') \\
 S_{16} &= (TT'/2)^{\frac{1}{2}}(\varepsilon_1' + \varepsilon_2'), \quad S_{17} = (KK'/2)^{\frac{1}{2}}(\phi_1' + \phi_2')
 \end{aligned}$$

Species A_2 :

$$\begin{aligned}
 S_1 &= (RS/2)^{\frac{1}{2}}(\tau_{r_1} + \tau_{r_2}), \quad S_2 = (LT/2)^{\frac{1}{2}}(\tau_{k_1} + \tau_{k_2}) \\
 S_3 &= (KL/2)^{\frac{1}{2}}(\tau_{l_1} + \tau_{l_2}), \quad S_4 = [(RS)^{\frac{1}{2}}S'/2]^{\frac{1}{2}}(\beta_1'' + \beta_2'') \\
 S_5 &= [(KT)^{\frac{1}{2}}K'/2]^{\frac{1}{2}}(\varepsilon_1'' + \varepsilon_2''), \quad S_6 = [(LK)^{\frac{1}{2}}K'/2]^{\frac{1}{2}}(\phi_1'' + \phi_2'')
 \end{aligned}$$

Species B_1 :

$$\begin{aligned}
 S_1 &= [(ST)^{\frac{1}{2}}H/2]^{\frac{1}{2}}(\xi_1 - \xi_2), \quad S_2 = (RS/2)^{\frac{1}{2}}(\tau_{r_1} - \tau_{r_2}) \\
 S_3 &= (LT/2)^{\frac{1}{2}}(\tau_{k_1} - \tau_{k_2}), \quad S_4 = (KL/2)^{\frac{1}{2}}(\tau_{l_1} - \tau_{l_2})
 \end{aligned}$$

$$S_5 = [(RS)^{\frac{1}{2}} S' / 2]^{\frac{1}{2}} (\beta_1'' - \beta_2''), S_6 = [(KT)^{\frac{1}{2}} T' / 2]^{\frac{1}{2}} (\varepsilon_1'' - \varepsilon_2'')$$

$$S_7 = [(LK)^{\frac{1}{2}} K' / 2]^{\frac{1}{2}} (\phi_1'' - \phi_2''), S_8 = S = (RR')^{\frac{1}{2}} \alpha''$$

$$S_9 = (LL')^{\frac{1}{2}} \theta''$$

Species B_2 :

$$S_1 = 2^{-\frac{1}{2}} (r_1 - r_2), S_2 = 2^{-\frac{1}{2}} (s_1 - s_2), S_3 = 2^{-\frac{1}{2}} (t_1 - t_2)$$

$$S_4 = 2^{-\frac{1}{2}} (k_1 - k_2), S_5 = 2^{-\frac{1}{2}} (l_1 - l_2), S_6 = (RS/2)^{\frac{1}{2}} (\beta_1 - \beta_2)$$

$$S_7 = (HT/2)^{\frac{1}{2}} (\delta_1 - \delta_2), S_8 = (Tk/2)^{\frac{1}{2}} (\varepsilon_1 - \varepsilon_2), S_9 = 2^{-\frac{1}{2}} (s_1' - s_2')$$

$$S_{10} = 2^{-\frac{1}{2}} (t_1' - t_2'), S_{11} = 2^{-\frac{1}{2}} (k_1' - k_2'), S_{12} = (RS'/2)^{\frac{1}{2}} (\beta_1' - \beta_2')$$

$$S_{13} = (TT'/2)^{\frac{1}{2}} (\varepsilon_1' - \varepsilon_2'), S_{14} = (KK'/2)^{\frac{1}{2}} (\phi_1' - \phi_2')$$

$$S_{15} = (RR'/2)^{\frac{1}{2}} (\alpha_1' - \alpha_2'), S_{16} = (LL'/2)^{\frac{1}{2}} (\theta_1' - \theta_2')$$

Table 1. Experimental frequencies of vibration (cm^{-1}) for azulene used in the present calculations.

| | | | | | |
|---------------------------------|-----------------------------|---------------------------|-----------------------------|------------------|----------|
| A_1^a | C-H stretching | 3091 | B_1^b | C-H op c bend | 1000 |
| | | 3074 | | | 960 |
| | | 3059 | | | 946 |
| | | 3024 | | | 764 |
| | | 3002 | | | 721 |
| | C-C stretching (arom.) | 1638 | Ring op c deformation | 664 | |
| | | 1580 | | 492 | |
| | | 1443 | | 311 | |
| | | 1392 | | 165 | |
| | CCH ip c bend | 1294 | B_2^a | C-H stretching | 3083 |
| 1117 | | 3044 | | | |
| 1054 | 3007 | | | | |
| C-C stretching (single bond) | 899 | C-C stretching (arom.) | | 1694 | |
| | | | | 1580 | |
| | | | | 1479 | |
| | | | | 1453 | |
| CCC ring bend | 671 | CCH ip c bend | | 1301 | |
| | | | | 559 | 1205 |
| | | | | 492 | 1151 |
| | | | 403 | 1007 | |
| A_2^b | C-H op c bend | 1000 | CCC ring bend | 721 | |
| | | | | 908 | 593 |
| | | | | 795 | 559 |
| | Ring op c deformation | 531 | | 163 d | 478 |
| | | | | | 323 d |
| | | | | | 163 d |

a From Ref. 34. b From Ref. 33. c ip=in plane, op=out of plane. d Calculated in Ref. 33.

STRUCTURAL AND SPECTRAL DATA

Bastiansen and Derrisen³² report structural data for azulene, obtained by electron diffraction. Vibrational frequencies are given by Steele,^{33,35} Hunt and Ross,³⁶ and van Tets and Günthard.³⁴ There are some small discrepancies between these works, and Table 1 shows the frequencies we have adopted for the computations in the present work. The in-plane vibrational frequencies, species A_1 and B_2 , are taken from van Tets and Günthard,³⁴ taking into consideration the assignment of Steele.³⁵ All out-of-plane frequencies are from Ref. 33.

FORCE FIELD AND POTENTIAL ENERGY DISTRIBUTION

The harmonic force field for azulene was arrived at through several iterations. In Table 2 the final force constants are given which reproduce the vibrational frequencies exactly. Some of the force constants in Table 2 might seem astonishingly great. However, they are understandable in view of the theory of redundant symmetry coordinates described by Cyvin and Cyvin.³⁸ Table 3 gives the approximate description of the normal modes according to the calculated potential energy distribution terms. Compared to the experimental assignment of frequencies (Table 1) there are a few discrepancies.

Table 2. Symmetry force constants (in mdyne/Å) for azulene.

| | | | | | | | | | | |
|----|--------|--------|--------|--------|--------|---------|--------|--------|--------|---------------|
| 1 | 7.320 | | | | | | | | | Species A_1 |
| 2 | 0.207 | 6.613 | | | | | | | | |
| 3 | -0.359 | -0.529 | 7.828 | | | | | | | |
| 4 | -0.440 | -0.543 | 2.393 | 7.507 | | | | | | |
| 5 | -0.078 | -0.315 | -1.045 | -1.670 | 7.055 | | | | | |
| 6 | 0.010 | 0.147 | -3.905 | -4.844 | 2.037 | 12.031 | | | | |
| 7 | -0.227 | -0.059 | -0.059 | -0.174 | 0.118 | 0.115 | 0.641 | | | |
| 8 | -0.242 | -0.977 | 6.825 | 8.581 | -3.415 | -11.358 | -0.364 | 23.102 | | |
| 9 | -0.114 | -0.451 | 4.135 | 4.956 | -1.813 | -6.716 | -0.139 | 13.225 | 8.313 | |
| 10 | -0.121 | 0.0531 | -0.043 | -0.006 | 0.006 | 0.009 | -0.035 | -0.052 | -0.023 | |
| 11 | -0.050 | -0.084 | -0.027 | -0.019 | -0.041 | -0.004 | 0.048 | -0.012 | -0.007 | |
| 12 | -0.020 | -0.045 | -0.101 | 0.037 | -0.119 | -0.006 | -0.001 | 0.071 | 0.074 | |
| 13 | -0.014 | -0.048 | -0.063 | -0.122 | -0.012 | 0.070 | -0.003 | -0.213 | -0.144 | |
| 14 | 0 | 0.010 | 0.035 | 0.024 | 0.025 | -0.092 | 0.005 | 0.126 | 0.087 | |
| 15 | -0.015 | -0.075 | 0.085 | 0.074 | 0.029 | 0.013 | -0.031 | 0.036 | 0.030 | |
| 16 | -0.035 | -0.092 | 0.012 | -0.021 | -0.067 | 0.004 | 0.018 | -0.094 | -0.046 | |
| 17 | -0.042 | -0.053 | 0.131 | 0.007 | 0.018 | -0.177 | -0.004 | 0.187 | 0.126 | |
| 10 | 5.086 | | | | | | | | | Species A_1 |
| 11 | 0.041 | 5.115 | | | | | | | | (continued) |
| 12 | -0.007 | 0.002 | 5.070 | | | | | | | |
| 13 | 0 | -0.003 | -0.055 | 4.973 | | | | | | |
| 14 | 0 | -0.001 | 0.018 | -0.029 | 4.912 | | | | | |
| 15 | 0.013 | -0.011 | 0.002 | 0.005 | 0.001 | 0.582 | | | | |
| 16 | 0 | -0.012 | -0.016 | -0.004 | 0.001 | 0.004 | 0.599 | | | |
| 17 | -0.005 | -0.003 | 0.018 | -0.006 | -0.010 | 0.012 | 0.032 | 0.595 | | |

Table 2. Continued.

| | | | | | | | | | |
|----|--------|--------|--------|--------|---------------------------|--------|--------|--------|-------|
| 1 | 0.773 | | | | Species A_1 | | | | |
| 2 | -0.117 | 1.001 | | | | | | | |
| 3 | -0.154 | 1.673 | 3.177 | | | | | | |
| 4 | -0.015 | -0.046 | -0.085 | 0.219 | | | | | |
| 5 | 0.020 | 0.009 | -0.002 | -0.010 | 0.192 | | | | |
| 6 | 0.024 | -0.016 | -0.004 | 0.006 | 0.013 | 0.208 | | | |
| 1 | 0.320 | | | | Species B_1 | | | | |
| 2 | 0.005 | 0.130 | | | | | | | |
| 3 | -0.035 | -0.018 | 0.195 | | | | | | |
| 4 | -0.041 | -0.005 | 0.027 | 0.157 | | | | | |
| 5 | 0.031 | -0.023 | 0.008 | -0.006 | 0.223 | | | | |
| 6 | 0.035 | -0.011 | 0.043 | -0.026 | 0.009 | 0.244 | | | |
| 7 | -0.016 | 0.004 | -0.043 | 0.053 | -0.003 | -0.009 | 0.220 | | |
| 8 | -0.003 | 0.018 | -0.006 | -0.002 | 0.005 | 0.003 | 0.004 | 0.217 | |
| 9 | -0.020 | 0.002 | -0.027 | 0.053 | -0.009 | 0.001 | 0.009 | 0.001 | 0.227 |
| 1 | 8.482 | | | | Species B_2 | | | | |
| 2 | 3.619 | 11.463 | | | | | | | |
| 3 | 1.050 | 1.583 | 8.241 | | | | | | |
| 4 | 0.450 | 0.528 | 1.163 | 7.217 | | | | | |
| 5 | 0.112 | 0.094 | 0.182 | 0.701 | 6.297 | | | | |
| 6 | 2.421 | 3.566 | 1.057 | 0.580 | 0.099 | 2.964 | | | |
| 7 | -0.744 | -1.438 | 0.394 | 0.008 | -0.128 | -0.668 | 1.466 | | |
| 8 | -0.040 | -0.444 | 1.103 | 0.645 | 0.005 | 0.059 | 0.877 | 1.603 | |
| 9 | -0.151 | -0.102 | 0.001 | -0.034 | -0.006 | 0.006 | -0.013 | -0.026 | |
| 10 | 0.005 | 0.040 | -0.043 | -0.050 | 0.073 | 0.003 | -0.026 | -0.003 | |
| 11 | 0.014 | -0.020 | 0.087 | -0.019 | -0.108 | 0.255 | 0.020 | 0.030 | |
| 12 | -0.083 | -0.107 | 0.042 | 0.080 | 0.005 | -0.095 | 0.055 | 0.061 | |
| 13 | 0.068 | 0.137 | 0.217 | 0.135 | 0.044 | 0.059 | -0.006 | 0.015 | |
| 14 | 0.022 | 0.041 | -0.028 | -0.036 | -0.097 | 0.225 | -0.066 | -0.034 | |
| 15 | 0.216 | 0.096 | 0.008 | 0.020 | 0.012 | 0.026 | -0.020 | -0.014 | |
| 16 | 0.020 | 0.033 | 0.015 | 0.033 | 0.144 | 0.021 | -0.006 | 0.007 | |
| 9 | 5.125 | | | | Species B_2 (continued) | | | | |
| 10 | 0.068 | 5.008 | | | | | | | |
| 11 | -0.003 | -0.040 | 4.925 | | | | | | |
| 12 | -0.001 | -0.003 | 0.007 | 0.360 | | | | | |
| 13 | -0.001 | 0.003 | 0.009 | -0.033 | 0.336 | | | | |
| 14 | 0 | 0.004 | -0.010 | 0.007 | 0.038 | 0.374 | | | |
| 15 | 0.023 | 0.002 | 0.001 | 0.006 | 0.004 | 0.001 | 0.347 | | |
| 16 | 0.001 | 0 | 0.013 | 0.007 | 0.014 | -0.005 | -0.003 | 0.352 | |

Table 3. Approximate description of normal modes and potential energy distribution for azulene.

| Symm | Fre., cm ⁻¹ . | | |
|-------|-----------------------------|----------------|--------------------------------|
| A_1 | 3091 | C-H stretching | (31r' + 66s') |
| | 3074 | C-H stretching | (77t' + 16k') |
| | 3059 | C-H stretching | (65r' + 31s') |
| | 3024 | C-H stretching | (19t' + 66k' + 14l') |
| | 3002 | C-H stretching | (16k' + 83l') |
| | 1638 | C-C stretching | (20s + 44t + 33k + 34δ + 11ε') |
| | 1580 | C-C stretching | (16r + 29s + 18k + 24β') |

Table 3. Continued.

| | | | |
|-----------------------|------|---|--|
| | 1443 | CCC bend | $(33t + 51h + 19l + 92\delta + 102\varepsilon + 19\phi')$ |
| | 1392 | C-C stretching, CCC bend | $(15r + 19h + 18l + 57\delta + 10\beta' + 21\varepsilon' + 23\phi')$ |
| | 1294 | C-C stretching, CCC bend | $(17r + 23s + 10\varepsilon' + 17\phi')$ |
| | 1117 | C-C stretching, CCC bend | $(11r + 11k + 10l + 32\varepsilon' + 19\phi')$ |
| | 1054 | CCH ip ^a bend | $(33r + 12\delta + 43\beta')$ |
| | 899 | C-C stretching | $(13k + 98l + 60\delta)$ |
| | 671 | CCC bend | $(128\delta + 466\varepsilon)$ |
| | 559 | C-C stretching, CCC bend | $(35t + 71h + 18l + 15\beta + 20\delta)$ |
| | 492 | CCC bend | $(12t + 74\beta + 106\delta + 52\varepsilon)$ |
| | 403 | CCC bend | $(739\delta + 514\varepsilon)$ |
| <i>A</i> ₁ | 1000 | Ring torsion, CCH op ^a bend | $(172\tau_k + 108\tau_l + 49\varepsilon'' + 35\phi'')$ |
| | 908 | CCH op ^a bend | $(13\tau_l + 58\beta'' + 21\phi'')$ |
| | 795 | CCH op ^a bend | $(27\beta'' + 28\varepsilon'' + 39\phi'')$ |
| | 531 | Ring torsion, CCH op ^a bend | $(22\tau_r + 30\tau_k + 14\beta'' + 21\varepsilon'')$ |
| | 323 | Ring torsion | $(653\tau_k + 701\tau_l)$ |
| | 163 | Ring torsion | $(65\tau_r + 27\tau_l)$ |
| <i>B</i> ₁ | 1000 | Ring op ^a deformation, CCH op ^a bend | $(42\tau_k + 63\tau_l + 22\varepsilon'' + 58\phi'' + 42\theta'')$ |
| | 960 | CCH op ^a bend | $(18\tau_r + 53\beta'' + 40\alpha'')$ |
| | 946 | CCH op ^a bend | $(64\varepsilon'' + 26\theta'')$ |
| | 764 | CCH op ^a bend | $(35\beta'' + 47\alpha'')$ |
| | 721 | CCH op ^a bend | $(14\varepsilon'' + 46\phi'' + 32\theta'')$ |
| | 664 | Ring op ^a deformation | $(11\xi + 24\tau_k + 23\tau_l)$ |
| | 492 | Ring op ^a deformation | $(48\xi + 18\tau_r + 24\tau_l)$ |
| | 311 | Ring op ^a deformation | $(20\xi + 65\tau_r + 11\tau_k)$ |
| | 165 | Ring op ^a deformation | $(13\xi + 47\tau_k + 14\tau_l)$ |
| <i>B</i> ₂ | 3083 | C-H stretching | $(98s')$ |
| | 3044 | C-H stretching | $(84t' + 14k')$ |
| | 3007 | C-H stretching | $(15t' + 84k')$ |
| | 1694 | C-C stretching | $(41s + 37t + 23k + 17l + 23\delta)$ |
| | 1580 | C-C stretching | $(25s + 59l + 11\theta')$ |
| | 1479 | C-C stretching | $(86r + 21\beta + 35\alpha')$ |
| | 1453 | C-C stretching | $(39s + 34k + 21\theta')$ |
| | 1301 | C-C stretching, CCH ip ^a bend | $(11s + 28t + 37\theta')$ |
| | 1205 | Ring ip ^a bend, CCH ip ^a bend | $(25r + 11s + 18\beta + 12\delta + 47\alpha')$ |
| | 1151 | Ring ip ^a bend, CCH ip ^a bend | $(12t + 14k + 13l + 18\varepsilon' + 22\theta')$ |
| | 1007 | CCH ip ^a bend | $(16\delta + 12\varepsilon + 58\beta' + 12\phi')$ |
| | 970 | CCH ip ^a bend | $(18\varepsilon' + 56\phi')$ |
| | 721 | CCH ip ^a bend, ring ip ^a bend | $(13s + 18k + 12\beta + 22\beta' + 56\varepsilon' + 16\phi')$ |
| | 593 | Ring ip ^a bend | $(25s + 81\beta + 71\delta + 92\varepsilon)$ |
| | 559 | Ring ip ^a bend | $(24\beta + 38\varepsilon)$ |
| | 478 | Ring ip ^a bend | (42δ) |

^a ip = in plane, op = out of plane.

Table 4. Mean amplitudes of vibration, u , (\AA units), for azulene.

| Distance type ($i-j$) ^a | (Equil. dist. in \AA) | u spectr. | | u electr. diff. Ref. 29 | |
|---|------------------------------------|-------------|--------|------------------------------|--------|
| | | 0 K | 298 K | | |
| C-H | (1-11) | (1.085) | 0.0770 | 0.0770 | |
| C-H | (2-12) | (1.085) | 0.0769 | 0.0769 | |
| C-H | (6-14) | (1.085) | 0.0772 | 0.0772 | 0.090 |
| C-H | (8-16) | (1.085) | 0.0776 | 0.0776 | |
| C-H | (10-18) | (1.085) | 0.0777 | 0.0777 | |
| C-C | (1-2) | (1.399) | 0.0447 | 0.0448 | 0.0486 |
| C-C | (2-4) | (1.418) | 0.0442 | 0.0445 | |
| C-C | (4-5) | (1.501) | 0.0488 | 0.0497 | |
| C-C | (4-6) | (1.383) | 0.0446 | 0.0451 | |
| C-C | (6-8) | (1.406) | 0.0445 | 0.0448 | |
| C-C | (8-10) | (1.403) | 0.0451 | 0.0454 | |
| C...C | (1-4) | (2.290) | 0.0569 | 0.0603 | |
| C...C | (1-6) | (3.624) | 0.0608 | 0.0652 | |
| C...C | (1-8) | (4.780) | 0.0648 | 0.0705 | |
| C...C | (1-10) | (5.203) | 0.0670 | 0.0741 | |
| C...C | (2-6) | (2.487) | 0.0553 | 0.0584 | |
| C...C | (2-8) | (3.808) | 0.0598 | 0.0639 | |
| C...C | (2-10) | (4.548) | 0.0636 | 0.0694 | |
| C...C | (2-9) | (4.509) | 0.0618 | 0.0657 | |
| C...C | (2-7) | (3.685) | 0.0594 | 0.0623 | |
| C...C | (2-5) | (2.335) | 0.0551 | 0.0572 | |
| C...C | (2-3) | (2.292) | 0.0575 | 0.0604 | 0.054 |
| C...C | (4-8) | (2.499) | 0.0542 | 0.0567 | |
| C...C | (4-10) | (3.130) | 0.0608 | 0.0658 | 0.078 |
| C...C | (4-9) | (3.172) | 0.0601 | 0.0637 | |
| C...C | (4-7) | (2.599) | 0.0571 | 0.0596 | |
| C...C | (6-10) | (2.537) | 0.0554 | 0.0571 | 0.057 |
| C...C | (6-9) | (3.190) | 0.0641 | 0.0687 | |
| C...C | (6-7) | (3.227) | 0.0664 | 0.0723 | |
| C...C | (8-9) | (2.542) | 0.0584 | 0.0614 | |
| C...H | (1-12) | (2.212) | 0.1007 | 0.1033 | |
| C...H | (1-14) | (4.029) | 0.1334 | 0.1379 | |
| C...H | (1-16) | (5.703) | 0.1080 | 0.1116 | |
| C...H | (1-18) | (6.288) | 0.0989 | 0.1040 | |
| C...H | (2-11) | (2.208) | 0.0975 | 0.0981 | |
| C...H | (2-14) | (2.688) | 0.1373 | 0.1420 | |
| C...H | (2-16) | (4.598) | 0.1127 | 0.1155 | |
| C...H | (2-18) | (5.604) | 0.0984 | 0.1024 | |
| C...H | (2-17) | (5.550) | 0.0979 | 0.1003 | |
| C...H | (2-15) | (4.414) | 0.1179 | 0.1207 | |
| C...H | (2-13) | (3.335) | 0.0934 | 0.0947 | |
| C...H | (4-11) | (3.335) | 0.0942 | 0.0966 | |
| C...H | (4-12) | (2.231) | 0.1055 | 0.1074 | |
| C...H | (4-13) | (3.390) | 0.0955 | 0.0976 | |
| C...H | (4-14) | (2.103) | 0.1048 | 0.1057 | |
| C...H | (4-16) | (3.416) | 0.0998 | 0.1010 | |
| C...H | (4-18) | (4.192) | 0.0961 | 0.0995 | |
| C...H | (4-17) | (4.242) | 0.0948 | 0.0970 | |
| C...H | (4-15) | (3.528) | 0.1015 | 0.1030 | |
| C...H | (6-16) | (2.113) | 0.1051 | 0.1059 | |
| C...H | (6-18) | (3.444) | 0.0998 | 0.1008 | |
| C...H | (6-17) | (4.250) | 0.0997 | 0.1032 | |
| C...H | (6-15) | (4.293) | 0.0987 | 0.1025 | |

Table 4. Continued.

| | | | | |
|-------|---------|---------|--------|--------|
| C...H | (6-13) | (4.708) | 0.1019 | 0.1049 |
| C...H | (6-11) | (4.621) | 0.0996 | 0.1029 |
| C...H | (6-12) | (2.858) | 0.1345 | 0.1394 |
| C...H | (8-18) | (2.106) | 0.1013 | 0.1017 |
| C...H | (8-17) | (3.448) | 0.1085 | 0.1111 |
| C...H | (8-15) | (4.254) | 0.0997 | 0.1035 |
| C...H | (8-13) | (5.403) | 0.1136 | 0.1178 |
| C...H | (8-11) | (5.834) | 0.0991 | 0.1032 |
| C...H | (8-12) | (4.263) | 0.1360 | 0.1414 |
| C...H | (8-14) | (2.123) | 0.1118 | 0.1140 |
| C...H | (10-11) | (6.288) | 0.0987 | 0.1038 |
| C...H | (10-12) | (5.232) | 0.1281 | 0.1340 |
| C...H | (10-14) | (3.455) | 0.1068 | 0.1091 |
| C...H | (10-16) | (2.110) | 0.1107 | 0.1126 |
| H...H | (11-12) | (2.653) | 0.1597 | 0.1616 |
| H...H | (11-14) | (4.894) | 0.1644 | 0.1692 |
| H...H | (11-16) | (6.723) | 0.1351 | 0.1384 |
| H...H | (11-18) | (7.373) | 0.1226 | 0.1268 |
| H...H | (12-14) | (2.622) | 0.1952 | 0.2024 |
| H...H | (12-16) | (4.858) | 0.1790 | 0.1843 |
| H...H | (12-18) | (6.236) | 0.1538 | 0.1593 |
| H...H | (12-17) | (6.472) | 0.1340 | 0.1374 |
| H...H | (12-15) | (5.484) | 0.1392 | 0.1420 |
| H...H | (12-13) | (4.339) | 0.1219 | 0.1224 |
| H...H | (14-16) | (2.353) | 0.1852 | 0.1901 |
| H...H | (14-18) | (4.227) | 0.1487 | 0.1510 |
| H...H | (14-17) | (5.299) | 0.1286 | 0.1321 |
| H...H | (14-15) | (5.347) | 0.1230 | 0.1257 |
| H...H | (16-18) | (2.328) | 0.1693 | 0.1715 |
| H...H | (16-17) | (4.215) | 0.1519 | 0.1549 |

MEAN AMPLITUDES OF VIBRATION

Table 4 shows the calculated mean amplitudes of vibration (u) at absolute zero and 298 K, along with the observed values from electron diffraction. No serious discrepancies between observed and calculated u values are found.

Table 5. Bond lengths, r , and mean amplitudes of vibration, u , (\AA units) of bonded carbon-carbon atom pairs in some cyclic hydrocarbons at 298 K.

| Molecule | C=C double bond | | CC aromatic | | C-C single bond | |
|---------------------------------|--------------------|--------|----------------|--------|--------------------|--------|
| | r | u | r | u | r | u |
| Benzene ^a | | | 1.397 | 0.0461 | | |
| 1,4-Cyclohexadiene ^b | 1.334 | 0.0419 | | | 1.496 | 0.0475 |
| 1,3-Cyclohexadiene ^b | 1.348 | 0.0427 | | | 1.465 | 0.0484 |
| | | | | | 1.519 | 0.0478 |
| | | | | | 1.538 | 0.0482 |
| Azulene | | | 1.383 | 0.0451 | 1.501 | 0.0497 |
| | | | 1.399 | 0.0448 | | |
| | | | 1.403 | 0.0454 | | |
| | | | 1.406 | 0.0448 | | |
| | | | 1.418 | 0.0445 | | |

^a From Ref. 28. ^b From Ref. 12.

Carbon-carbon bond lengths and corresponding u values for some cyclic hydrocarbons are shown in Table 5. It is seen that a clear correlation exists between the bond length, mean amplitude of vibration, and the type of carbon-carbon bond (*e.g.* double bond, aromatic bond, single bond). Single-bond u values lie around 0.048–0.050 Å, double-bond values around 0.042 Å, whereas aromatic carbon-carbon u values lie in between these limits, around 0.045–0.046 Å. The bond 4–5 (Fig. 1) of azulene has typical single-bond values of r and u , and all the other carbon-carbon bond lengths and mean amplitudes are typical for aromatic molecules.

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REFERENCES

1. Davis, M. I. and Muecke, T. W. *J. Phys. Chem.* **74** (1970) 1104.
2. Adams, W. J., Geise, H. J. and Bartell, L. S. *J. Am. Chem. Soc.* **92** (1970) 5013.
3. Dallinga, G., Van der Draai, R. K. and Toneman, L. H. *Rec. Trav. Chim.* **87** (1968) 897.
4. Chiang, J. F. and Bauer, S. H. *J. Am. Chem. Soc.* **91** (1969) 1898.
5. Trætteberg, M. *Acta Chem. Scand.* **22** (1968) 2305.
6. Oberhammer, H. and Bauer, S. H. *J. Am. Chem. Soc.* **91** (1969) 10.
7. Dallinga, G. and Toneman, L. H. *J. Mol. Struct.* **1** (1967) 11.
8. Dallinga, G. and Toneman, L. H. *J. Mol. Struct.* **1** (1967) 117.
9. Neto, N., Di Lauro, C., Castellucci, E. and Califano, S. *Spectrochim. Acta A* **23** (1967) 1763.
10. Di Lauro, C., Neto, N. and Califano, S. *J. Mol. Struct.* **3** (1969) 219.
11. Stidham, H. D. *Spectrochim. Acta* **21** (1965) 23.
12. Gebhardt, O. *Thesis*, Trondheim NTH 1971.
13. Hagen, K. *Thesis*, Trondheim NLHT 1970.
14. Chiang, J. F. and Bauer, S. H. *J. Am. Chem. Soc.* **88** (1966) 420.
15. Hagen, G. *Private communication*.
16. Cyvin, S. J., Elvebredd, I., Hagen, G. and Andersen, B. *Chem. Phys. Lett.* **2** (1968) 556.
17. Chiang, J. F. and Bauer, S. H. *J. Am. Chem. Soc.* **92** (1970) 1614.
18. Almenningen, A., Andersen, B. and Nyhus, B. A. *Acta Chem. Scand.* **25** (1971) 1217.
19. Bohn, R. K. and Tai, Y.-H. *J. Am. Chem. Soc.* **92** (1970) 6447.
20. Karle, I. L. *J. Chem. Phys.* **20** (1952) 65.
21. Bastiansen, O., Hedberg, L. and Hedberg, K. *J. Chem. Phys.* **27** (1957) 1311; Erratum: *Ibid.* **28** (1958) 512.
22. Trætteberg, M. *Acta Chem. Scand.* **20** (1966) 1724.
23. Haugen, W. and Trætteberg, M. In Andersen, P., Bastiansen, O. and Furberg, S., Eds., *Selected Topics in Structure Chemistry*, Universitetsforlaget, Oslo 1967, p. 113.
24. Trætteberg, M. *Acta Chem. Scand.* **24** (1970) 2285.
25. Trætteberg, M. *Proc. Roy. Soc. (London) Ser. A* **283** (1965) 557.
26. Dallinga, G., Toneman, L. H. and Trætteberg, M. *Rec. Trav. Chim.* **86** (1967) 795.
27. Almenningen, A., Bastiansen, O. and Dyvik, F. *Acta Cryst.* **14** (1961) 1056.
28. Cyvin, S. J. *Molecular Vibrations and Mean Square Amplitudes*, Universitetsforlaget, Oslo 1968.
29. Cyvin, B. N. and Cyvin, S. J. *J. Phys. Chem.* **73** (1969) 1430.
30. Almenningen, A., Bastiansen, O. and Fernholt, L. *Kgl. Norske Videnskab. Selskabs Skrifter* **1958** No. 3.
31. Kimura, K. and Kubo, M. *J. Chem. Phys.* **32** (1960) 1776.
32. Bastiansen, O. and Derrisen, J. L. *Acta Chem. Scand.* **20** (1966) 1319.
33. Steele, D. J. *Mol. Spectry.* **15** (1965) 333.
34. Van Tets, A. and Günthard, H. H. *Spectrochim. Acta* **19** (1963) 1495.

35. Steele, D. *Spectrochim. Acta* **22** (1966) 1275.
36. Hunt, G. R. and Ross, I. G. *J. Mol. Spectry.* **3** (1959) 604.
37. Wilson, E. B., Jr., Decius, J. C. and Cross, P. C. *Molecular Vibrations*, McGraw, New York 1955, 117–125.
38. Cyvin, B. N. and Cyvin, S. J. *Acta Chem. Scand.* **23** (1969) 3139.

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