

Crystal Structure of DL-Tryptophan Formate

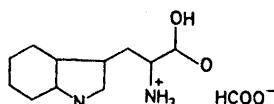
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The crystal structure of DL-tryptophan formate has been determined by X-ray methods using 2346 reflections recorded by counter methods. The crystals are monoclinic, space group $P2_1/c$, with unit cell dimensions $a = 11.23$, Å; $b = 6.72$, Å; $c = 16.01$, Å; $\beta = 96.2^\circ$. The structure was refined to a conventional *R*-factor of 0.051; estimated standard deviations are 0.002–0.003 Å in interatomic distances and 0.15° in angles.

The 3-indolylmethyl part of the molecule is planar and the alanine moiety exists in the extended form with the acid group *anti* relative to the aromatic part. The crystals are built up by layers of molecules; within each layer there is an extensive network of hydrogen bonds whereas the layers are held together by van der Waals forces.

The crystal structure of tryptophan formate has been determined as part of the series of structure determinations of tyrosine and tryptophan derivatives being carried out in this laboratory. Preliminary results have previously been published.¹ In the present paper a more detailed account of the structure is given.



EXPERIMENTAL

Plate formed single crystals were formed by diffusion of diethyl ether into a solution of DL-tryptophan in formic acid.

Oscillation, Weissenberg and precession photographs indicated monoclinic symmetry. Systematically absent reflections were $h0l$ for l odd and $0k0$ for k odd; the space group is thus $P2_1/c$.

Unit cell dimensions were determined from diffractometer measurements on twelve general reflections and their Laue-symmetric equivalents. A manual Picker four-circle diffractometer was used with $CuK\beta$ radiation ($\lambda = 1.3922$ Å). The computer program applied for the least-squares calculations as well as the computer programs used for the structure investigation are described in Ref. 2.

Three-dimensional intensity data were recorded on an automatic Picker four-circle diffractometer using graphite crystal monochromated MoK α radiation. The crystal had dimensions $0.50 \times 0.25 \times 0.06$ mm 3 and was mounted with the [302] direction along the diffractometer ϕ -axis. The $\omega - 2\theta$ scanning mode with a 2θ scan speed of 1° min^{-1} was applied through the scan range of 0.5° below $2\theta(\alpha_1)$ to 0.5° above $2\theta(\alpha_2)$. Background counts were taken for 20 sec at each of the scan range limits. The take-off angle was 4° and the temperature was kept constant at 18°C . The intensities of three standard reflections were measured for every 100 reflections of the data set. They showed slow variation and also a small net decrease, and the data was accordingly adjusted. The standard deviations in the intensities were taken as the square root of the total counts with a 2 % addition.

The measurements included 2757 unique reflections with $\sin \theta/\lambda$ less than 0.7; 2346 had net intensity larger than $2\sigma(I)$ and were regarded as observed whereas the remaining reflections were excluded from the further calculations.

The intensity data were corrected for Lorentz and polarization effects.

Atomic form factors used were those of Hanson *et al.*³ for oxygen, nitrogen, and carbon, and of Stewart *et al.*⁴ for hydrogen.

CRYSTAL DATA

DL-Tryptophan formate (DL- α -ammonium- β -indolepropionic acid formate), C₁₁H₁₃N₂O₂CHO₂, monoclinic. $a = 11.237(0.003)$ Å; $b = 6.728(0.002)$ Å; $c = 16.013(0.003)$ Å; $\beta = 96.29(0.01)^\circ$. $V = 1203.4$ Å 3 , $M = 250.26$, $F(000) = 528$, $Z = 4$. $D_{\text{obs}} = 1.37$ g cm $^{-3}$, $D_{\text{calc}} = 1.381$ g cm $^{-3}$. Absent reflections: $h0l$ when l is odd, $0k0$ when k is odd, space group P₂₁/c.

STRUCTURE DETERMINATION

Preliminary scale and isotropic thermal vibration factors were calculated using Wilson's statistical method and unitary structure factors were computed. Three origin defining reflections were given positive sign and three additional reflections were assigned symbolic signs. The symbolic addition procedure^{5,6} yielded signs or symbols for nine additional structure factors (acceptance probability 97 %). The fifteen unitary structure factors were now used for sign determination by the application of Sayre's equation⁷ for each of the eight sign combinations of the three symbols. Signs for 165 structure factors were evaluated in each case followed by a Fourier synthesis.

In one of the Fourier maps the position of the indole part and the carbon atom directly bonded to it could readily be found and one Fourier refinement based on these atoms yielded information of the coordinates of all non-hydrogen atoms. Further Fourier refinements followed by several cycles of least squares refinement with anisotropic thermal parameters gave a conventional R -factor of 0.08. Most of hydrogen atoms were assigned coordinates from stereochemical considerations, the hydrogen atoms of the hydroxyl and ammonium groups were localized from difference Fourier maps. Final least squares refinement calculations with individual isotropic thermal parameters for hydrogen atoms yielded an R -factor of 0.051 ($R_w = 0.047$). A total difference Fourier map showed no electron density exceeding 0.3 e Å $^{-3}$.

A comparison of the observed and calculated structure factors is given in Table 1; the parameters for non-hydrogen atoms are listed in Table 2 and for hydrogen atoms in Table 3. The anisotropic temperature factor is given by

Table 1. Observed and calculated structure factors. The columns are $h, k, l, 10|F_O|$ and $10|F_C|$

h	k	l	$10 F_O $	$10 F_C $
-15	0	0	92	-81
-15	0	0	86	-81
-14	0	4	52	-45
-14	0	5	95	-83
-13	0	14	21	-17
-13	0	14	41	-39
-13	0	14	62	-57
-13	0	14	75	-27
-13	0	14	35	-27
-12	0	4	59	-54
-12	0	4	83	-66
-12	0	5	54	-54
-12	0	11	16	-34
-12	0	14	59	-56
-12	0	14	61	-66
-12	0	14	37	-33
-11	0	14	40	-30
-11	0	14	29	-31
-11	0	14	71	-68
-11	0	14	105	-105
-11	0	4	109	-109
-11	0	5	91	-49
-11	0	6	77	-75
-10	0	4	74	-76
-10	0	5	65	-65
-10	0	12	21	-21
-10	0	14	21	-21
-10	0	14	68	-68
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-10	0	14	21	-21
-10	0	14	65	-65
-10	0	14	21	-21
-10	0	14	65	-65
-9	0	12	174	-177
-9	0	14	40	-41
-9	0	14	77	-76
-9	0	14	16	-12
-9	0	14	257	-247
-9	0	14	19	-24
-9	0	14	644	-591
-9	0	6	39	-37
-9	0	5	688	-688
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-8	0	12	17	-20
-8	0	14	31	-32
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-7	0	14	165	-164
-7	0	14	75	-79
-6	0	14	387	-394
-6	0	8	289	-280
-6	0	14	229	-209
-6	0	14	189	-184
-6	0	14	154	-162
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-6	0	14	119	-119
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-5	0	20	34	-32
-5	0	14	103	-109
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-5	0	14	76	-78
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-5	0	14	422	-415
-5	0	14	299	-300
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Table 1. Continued.

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-4	1	10	86	-167	-11	1	10	32	24	-7	2	7	44	-38	-1	2	6	199	-	370	109	
-4	1	9	72	63	-11	1	12	85	66	-7	2	5	78	-79	-1	2	4	320	-	306	7	
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Table 1. Continued.

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Table 1. Continued.

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3	5	14	31	30	8	5	2	34	-	41	1	5	16	70	-	90	-	89	-	-5	6	6	13	-	37	-	-	
3	5	14	37	37	8	5	2	34	-	41	1	5	16	71	-	91	-	90	-	-5	6	6	13	-	37	-	-	
3	5	14	121	124	7	5	2	34	-	41	1	5	16	72	-	92	-	91	-	-5	6	6	5	-	53	-	-	
3	5	14	117	116	7	5	2	34	-	41	1	5	16	73	-	93	-	92	-	-5	6	6	4	-	77	-	-	
3	5	14	68	68	7	5	2	34	-	41	1	5	16	74	-	94	-	93	-	-5	6	6	4	-	77	-	-	
3	5	14	198	199	7	5	2	34	-	41	1	5	16	75	-	95	-	94	-	-5	6	6	2	-	64	-	-	
3	5	14	305	307	7	5	2	34	-	41	1	5	16	76	-	96	-	95	-	-5	6	6	2	-	64	-	-	
3	5	14	101	101	7	5	2	34	-	41	1	5	16	77	-	97	-	96	-	-5	6	6	1	-	75	-	-	
3	5	14	37	37	7	5	2	34	-	41	1	5	16	78	-	98	-	97	-	-5	6	6	1	-	75	-	-	
3	5	14	126	124	7	5	2	34	-	41	1	5	16	79	-	99	-	98	-	-5	6	6	1	-	75	-	-	
3	5	14	87	87	7	5	2	34	-	41	1	5	16	80	-	100	-	99	-	-5	6	6	1	-	75	-	-	
3	5	14	166	167	7	5	2	34	-	41	1	5	16	81	-	101	-	100	-	-5	6	6	2	-	75	-	-	
3	5	14	122	122	7	5	2	34	-	41	1	5	16	82	-	102	-	101	-	-5	6	6	1	-	75	-	-	
3	5	14	11	31	34	7	5	2	34	-	41	1	5	16	83	-	103	-	102	-	-5	6	6	1	-	75	-	-
3	5	14	97	97	6	5	2	34	-	41	1	5	16	84	-	104	-	103	-	-5	6	6	1	-	75	-	-	
3	5	14	239	234	6	5	2	34	-	41	1	5	16	85	-	105	-	104	-	-5	6	6	1	-	75	-	-	
3	5	14	62	61	6	5	2	34	-	41	1	5	16	86	-	106	-	105	-	-5	6	6	1	-	75	-	-	
3	5	14	58	59	6	5	2	34	-	41	1	5	16	87	-	107	-	106	-	-5	6	6	1	-	75	-	-	
3	5	14	125	123	6	5	2	34	-	41	1	5	16	88	-	108	-	107	-	-5	6	6	1	-	75	-	-	
3	5	14	57	56	6	5	2	34	-	41	1	5	16	89	-	109	-	108	-	-5	6							

Table 1. Continued.

3	6	6	113	-	111	11	6	0	43	-	42	1	7	6	85	40	-	4	7	4	35	29	0	8	8	39	-	29				
3	6	6	62	-	67	7	1	31	30	-	1	7	1	53	-	55	-	5	7	1	36	35	1	8	8	44	-	41				
3	6	6	119	-	120	9	7	0	49	38	-	1	7	2	54	47	-	5	7	2	35	-	43	1	8	8	11	28	-	25		
3	6	6	50	-	43	9	7	1	40	42	-	1	7	2	3d	-	36	-	5	7	7	49	-	43	1	8	8	10	29	-	8	
4	6	6	76	-	74	9	7	2	40	27	-	1	7	4	29	24	-	5	7	8	32	-	27	1	8	8	6	42	-	45		
4	6	6	1	-	37	9	7	4	36	28	-	1	7	5	52	51	-	5	7	9	44	-	42	1	8	8	5	27	-	22		
4	6	6	74	-	74	9	7	5	34	37	-	1	7	6	53	-	50	-	5	7	10	44	-	40	1	8	8	4	43	-	43	
4	6	6	104	-	103	8	7	6	37	35	-	1	7	7	57	-	59	-	6	7	11	51	-	53	1	8	8	23	-	26		
4	6	6	43	-	50	8	7	8	28	27	-	1	7	10	56	55	-	6	7	10	49	-	46	2	8	8	37	-	32			
4	6	6	22	-	10	8	7	2	49	42	-	1	7	11	36	-	42	-	6	7	9	46	-	48	2	8	8	1	27	-	17	
4	6	6	44	-	37	8	7	0	28	27	-	1	7	14	102	-	92	-	6	7	9	49	-	40	2	8	8	2	50	-	54	
4	6	7	30	-	43	7	7	1	27	-	29	0	7	14	36	-	29	-	6	7	6	28	-	15	2	8	8	31	-	26		
4	6	6	31	-	35	7	7	2	33	35	-	0	7	11	41	-	31	-	6	7	1	27	18	-	2	8	8	46	-	41		
4	6	6	11	-	35	7	7	3	82	83	-	0	7	10	39	-	34	-	7	7	2	53	-	45	2	8	8	34	-	35		
4	6	6	36	-	40	7	7	6	51	47	-	0	7	7	28	-	24	-	7	5	54	60	-	62	2	8	8	10	-	16		
4	6	6	12	-	46	38	7	7	33	-	31	0	7	7	112	-	104	-	7	3	34	-	28	3	8	8	31	-	31			
4	6	6	14	-	41	35	6	7	10	57	46	-	0	7	7	34	-	24	-	7	1	38	38	-	33	3	8	8	68	-	69	
5	6	6	12	-	68	53	6	7	6	50	45	-	0	7	7	46	-	42	-	7	7	7	43	-	35	3	8	8	1	52	-	45
5	6	6	116	-	106	6	7	7	30	-	29	0	7	7	43	-	41	-	10	7	4	31	-	31	3	8	8	4	52	-	45	
5	6	6	118	-	125	6	7	8	47	49	-	-1	7	1	65	-	61	-	10	7	6	34	-	34	3	8	8	46	-	75		
5	6	6	49	-	43	6	7	9	35	36	-	-1	7	8	59	-	57	-	10	7	8	42	-	43	4	8	8	74	-	69		
5	6	6	116	-	114	6	7	10	32	-	29	-1	7	8	55	-	50	-	7	8	2	58	-	60	4	8	8	66	-	66		
5	6	6	137	-	132	6	7	1	96	-	90	-1	7	5	51	-	132	-	6	8	1	79	-	91	4	8	8	29	-	14		
5	6	6	1	-	30	23	5	7	1	83	-	76	-1	7	6	44	-	43	-	6	8	4	57	-	46	4	8	8	44	-	36	
5	6	6	45	-	43	5	7	2	65	-	61	-1	7	7	73	-	74	-	5	8	6	75	-	79	5	8	8	29	-	29		
5	6	6	32	-	23	5	7	3	57	-	50	-1	7	6	43	-	47	-	5	8	6	69	-	63	5	8	8	42	-	39		
6	6	6	1	-	69	57	5	7	4	46	-	43	-1	7	5	72	-	62	-	5	8	3	42	-	39	5	8	8	52	-	50	
6	6	6	102	-	100	5	7	5	69	59	-	-1	7	4	54	-	48	-	5	8	2	124	-	115	5	8	8	1	44	-	40	
6	6	6	30	-	43	5	7	6	65	-	61	-2	7	12	63	-	58	-	8	1	40	19	-	5	8	8	47	-	40			
6	6	6	79	-	73	4	7	12	45	36	-	-2	7	12	16	-	26	-	8	1	27	39	-	6	8	8	69	-	64			
6	6	6	144	-	144	4	7	13	36	-	32	-2	7	1	41	-	40	-	8	1	27	47	-	6	8	8	32	-	32			
6	6	7	31	-	26	4	7	14	62	-	54	-2	7	7	131	-	137	-	8	1	45	46	-	41	6	8	8	32	-	31		
6	6	6	8	-	34	4	7	15	76	-	67	-2	7	5	100	-	107	-	8	1	21	71	-	65	7	8	8	33	-	27		
6	6	6	52	-	52	4	7	6	27	23	-	-2	7	4	44	-	33	-	8	1	26	32	-	27	7	8	8	21	-	27		
6	6	6	32	-	26	4	7	7	32	-	34	-2	7	6	47	-	49	-	8	1	20	25	-	24	7	8	8	20	-	27		
6	6	6	11	-	48	4	7	8	139	-	131	-2	7	1	124	-	134	-	8	1	11	45	-	11	4	8	8	42	-	40		
6	6	6	54	-	54	4	7	9	61	-	59	-3	7	1	41	-	45	-	8	1	10	63	-	59	3	8	8	34	-	31		
7	6	6	99	-	97	4	7	10	27	29	-	-3	7	6	103	-	107	-	8	1	8	69	-	67	3	8	8	30	-	29		
7	6	6	69	-	69	3	7	11	41	-	49	-3	7	7	87	-	84	-	8	1	7	49	-	41	2	8	8	29	-	27		
7	6	6	31	-	31	4	7	12	27	-	20	-3	7	7	74	-	70	-	8	1	8	61	-	53	2	8	8	38	-	30		
7	6	6	8	-	34	4	7	13	56	-	54	-3	7	7	100	-	97	-	8	1	8	56	-	41	1	8	8	31	-	31		
7	6	6	52	-	52	4	7	14	76	-	70	-3	7	7	100	-	107	-	8	1	8	65	-	65	7	8	8	33	-	31		
7	6	6	32	-	26	4	7	15	29	-	21	-3	7	7	44	-	41	-	8	1	8	36	-	32	7	8	8	23	-	23		
7	6	6	6	-	44	4	7	16	46	-	24	-3	7	9	26	-	24	-	8	1	8	41	-	32	0	8	8	41	-	39		
7	6	6	6	-	46	4	7	17	56	-	55	-3	7	10	29	-	31	-	8	1	8	33	-	26	0	8	8	24	-	23		
7	6	6	6	-	27	4	7	18	54	-	55	-3	7	11	63	-	60	-	8	1	8	25	-	25	0	8	8	23	-	23		
7	6	6	6	-	29	4	7	19	30	-	36	-3	7	10	63	-	60	-	8	1	8	10	-	45	-1	8	8	12	-	11		
7	6	6	6	-	49	4	7	20	35	-	31	-3	7	12	32	-	24	-	8	1	8	12	-	78	-1	8	8	52	-	40		
7	6	6	44	-	33	4	7	21	25	-	28	-3	7	11	39	-	36	-	8	1	8	27	-	24	-2	8	8	40	-	40		
7	6	6	26	-	27	4	7	21	39	-	45	-3	7	10	80	-	73	-	8	1	8	22	-	21	-2	8	8	31	-	21		
10	6	6	54	-	51	2	7	6	50	-	53	-4	7	6	34	-	32	-	8	1	8	22	-	24	-2	8	8	64	-	64		
10	6	6	33	-	39	2	7	7	45	53	-	-4	7	5	78	-	71	-	8	1	8	45	-	54	-3	8	8	41	-	39		
10	6	6	4	-	37	2	7	8	70	64	-	-4	7	6	42	-	40	-	8	1	8	22	-	31	-4	8	8	62	-	59		
10	6	6	87	-	81	2	7	2	27	-	22	-4	7	3	42	-	34	-	8	1	8	24	-	36	-4	8	8	58	-	59		
10	6	6	29	-	32	2	7	1	144	-	146	-4	7	2	34	-	34	-	8	1	8	27	-	19	-4	8	8	58	-	59		

DISCUSSION

Interatomic distances and bond angles are listed in Table 5; bond lengths and angles are shown in Fig. 1 in which the numbering of the atoms is also indicated. The molecular arrangement and hydrogen bonding system are illustrated in Figs. 2 and 3.

Table 2. Fractional atomic coordinates and thermal parameters with standard deviations ($\times 10^3$) for non-hydrogen atoms.

Atom	<i>x</i>	<i>y</i>	<i>z</i>	<i>B</i> 11	<i>B</i> 22	<i>B</i> 33	<i>B</i> 12	<i>B</i> 13	<i>B</i> 23
N1	24678 12	50370 20	27235 9	842 13	1459 35	437 7	-6 36	216 15	-438 25
C2	20728 13	42927 24	19447 10	671 14	1431 40	391 7	-198 41	88 16	71 29
C3	26182 12	25425 23	18144 9	511 11	1356 27	298 6	-396 36	106 13	-88 26
C4	41920 14	6009 27	28133 10	646 14	2393 49	380 8	486 36	97 16	-261 34
C5	48286 16	6908 34	36010 12	757 16	3765 69	470 9	1170 60	-57 19	-16 43
C6	47011 15	22972 37	41392 10	819 17	4776 82	338 8	213 64	-157 18	-427 44
C7	39342 15	38305 31	39079 10	833 16	3248 62	347 7	-520 55	154 17	-833 37
C8	32855 13	37392 25	31182 9	751 13	1815 42	334 7	-397 40	183 15	-430 30
C9	34028 12	21394 23	25630 9	490 12	1550 39	300 6	-251 37	162 13	-245 27
C10	24047 13	12857 25	10433 9	702 14	1686 42	275 6	-546 42	90 15	-79 28
C11	16571 13	-5641 24	11741 8	644 13	1465 38	221 6	-290 39	-2 13	-2 25
C12	13522 12	-17159 23	3597 8	767 14	1368 39	235 6	-453 41	60 14	1 25
O13	22810 9	-21321 19	-197 6	747 10	3169 40	393 5	-620 35	209 12	-1016 25
O14	3278 8	-21431 19	197 6	749 11	2667 36	312 5	-882 33	63 11	-545 22
N15	5117 10	-321 18	15104 7	710 11	1491 33	227 5	-476 33	71 12	-80 20
C16	12109 13	3533 24	36877 8	717 14	1641 41	216 5	64 41	101 14	-87 25
O17	6435 8	13985 15	31516 5	732 9	1533 26	239 4	284 27	87 95	52 18
O18	15775 10	-13832 16	35874 6	1023 11	1532 27	286 4	765 30	250 11	127 19

Table 3. Fractional coordinates ($\times 10^4$) and isotropic thermal parameters (\AA^2) with standard deviations for hydrogen atoms.

Atom	<i>x</i>	<i>y</i>	<i>z</i>	<i>B</i>
H1	2214 15	6206 28	2930 11	4.9 .4
H2	1500 13	4998 24	1508 10	3.9 .4
H4	4264 13	-516 23	2430 9	3.3 .4
H5	5398 15	-388 29	3810 12	5.7 .5
H6	5099 15	2371 29	4721 11	5.2 .4
H7	3836 14	4914 26	4272 11	4.7 .4
H101	3165 13	791 24	864 10	3.7 .4
H102	1933 13	2079 25	556 10	3.8 .4
H11	2134 12	-1452 22	1592 9	2.8 .3
H13	1983 17	2773 31	-603 13	7.4 .6
H151	672 13	542 23	2047 10	3.6 .4
H152	17 14	-1195 26	1556 10	4.7 .5
H153	108 13	905 24	1146 10	3.8 .4
H16	1389 13	963 24	4250 10	4.0 .4

The crystal structure is built up by molecular double layers parallel to (100). The layers are connected through van der Waals forces whereas the ions within the layers are bonded together by an extensive hydrogen bond system. Similar arrangements are reported for the tryptophan halides.⁸ Dimers of tryptophan ions are formed about centers of symmetry through hydrogen bonds between carboxyl and amino groups (O14—N15 3.026 Å). These are the only direct hydrogen bonds between two tryptophan molecules. The formate anions link the dimers together with hydrogen bonds to form the layers. All hetero atoms

Table 4. R.m.s. amplitudes of vibration and B -values (\AA^2) along the principal axes of vibration given by the components of a unit vector \mathbf{e} in fractional coordinates ($\times 10^4$).

Atom	$(\bar{u}^2)^{\frac{1}{2}}$	B	e_x	e_y	e_z
N1	0.249	4.90	343	531	558
	0.228	4.09	825	310	141
	0.168	2.22	-54	1353	251
C2	0.226	4.02	-136	236	599
	0.208	3.43	839	430	185
	0.177	2.47	280	1403	-44
C3	0.202	3.22	521	823	412
	0.191	2.89	-404	580	470
	0.155	1.90	606	1093	61
C4	0.252	5.00	303	1217	-267
	0.215	3.64	422	415	555
	0.187	2.77	-729	746	126
C5	0.312	7.70	381	1322	-75
	0.250	4.94	-124	367	589
	0.190	2.86	801	-571	204
C6	0.335	8.88	96	1448	-116
	0.245	4.72	-715	302	299
	0.187	2.77	530	145	540
C7	0.297	6.96	227	-1286	288
	0.226	4.02	850	204	110
	0.180	2.55	164	716	548
C8	0.238	4.46	343	-1000	421
	0.184	2.68	-690	215	335
	0.171	2.31	456	1074	324
C9	0.213	3.59	347	914	456
	0.176	2.43	-318	874	429
	0.167	2.21	762	781	53
C10	0.229	4.13	712	901	53
	0.189	2.81	138	307	593
	0.174	2.40	525	1141	201
C11	0.212	3.54	-770	646	108
	0.177	2.48	270	1271	-243
	0.165	2.15	369	420	569
C12	0.229	4.14	-820	566	16
	0.174	2.39	89	-135	626
	0.167	2.19	348	1367	55
O13	0.305	7.36	230	-1212	342
	0.211	3.52	843	136	-137
	0.178	2.50	194	850	509

Table 4. Continued.

	0.274	5.94	428	- 1237	208
O14	0.214	3.62	620	241	- 391
	0.167	2.21	483	787	446
	0.224	3.96	778	- 733	32
N15	0.176	2.45	275	904	- 436
	0.165	2.15	348	925	451
	0.213	3.60	882	249	38
C16	0.195	3.00	156	- 1425	152
	0.164	2.13	8	339	609
	0.220	3.83	830	554	37
O17	0.183	2.64	- 293	1277	223
	0.174	2.38	164	- 522	586
	0.267	5.62	822	560	142
O18	0.187	2.75	112	42	- 611
	0.171	2.30	338	- 1376	39

Table 5. Bond lengths (\AA) and bond angles ($^\circ$) in DL-tryptophan formate.

Bond length	Corrected	Bond angle		
N1-C2	1.372	1.376	N1-C2-C3	110.53
N1-C8	1.371	1.377	N1-C8-C9	107.43
C2-C3	1.354	1.360	C2-N1-C8	108.68
C3-C9	1.434	1.440	C2-C3-C9	106.43
C3-C10	1.494	1.498	C3-C9-C8	106.92
C4-C9	1.393	1.400	C3-C9-C4	134.01
C4-C5	1.382	1.386	C9-C4-C5	118.67
C5-C6	1.399	1.404	C4-C5-O6	121.22
C6-C7	1.369	1.375	C5-C6-C7	121.29
C7-C8	1.390	1.395	C6-C7-C8	117.68
C8-C9	1.412	1.418	C7-C8-C9	122.07
C10-C11	1.529		C8-C9-C4	119.07
C11-C12	1.523		C7-C8-N1	130.50
C11-N15	1.492		C2-C3-C10	125.81
C12-O13	1.295		C9-C3-C10	127.74
C12-O14	1.214		C3-C10-C11	112.85
C16-O17	1.232		C10-C11-C12	111.85
C16-O18	1.255		C10-C11-N15	111.27
N1-H1	0.91		C12-C11-N15	108.00
C2-H2	0.95		C11-C12-O13	113.24
C4-H4	0.98		C11-C12-O14	121.88
C5-H5	1.00		O13-C12-O14	124.86
C6-H6	0.99		O17-C16-O18	126.46
C7-H7	0.95			
C10-H101	0.99		Hydrogen bond lengths	
C10-H102	1.04		N1-O18 ($x, 1+y, z$)	3.003
C11-H11	1.01		O13-O18 ($x, -\frac{1}{2}-y, -\frac{1}{2}+z$)	2.492
O13-H13	1.05		N15-O14 ($-x, -y, -z$)	3.026
N15-H151	0.94		N15-O17 (x, y, z)	2.787
N15-H152	0.97		N15-O17 ($-x, -\frac{1}{2}+y, \frac{1}{2}-z$)	2.811
N15-H153	0.94			
C16-H16	0.99			

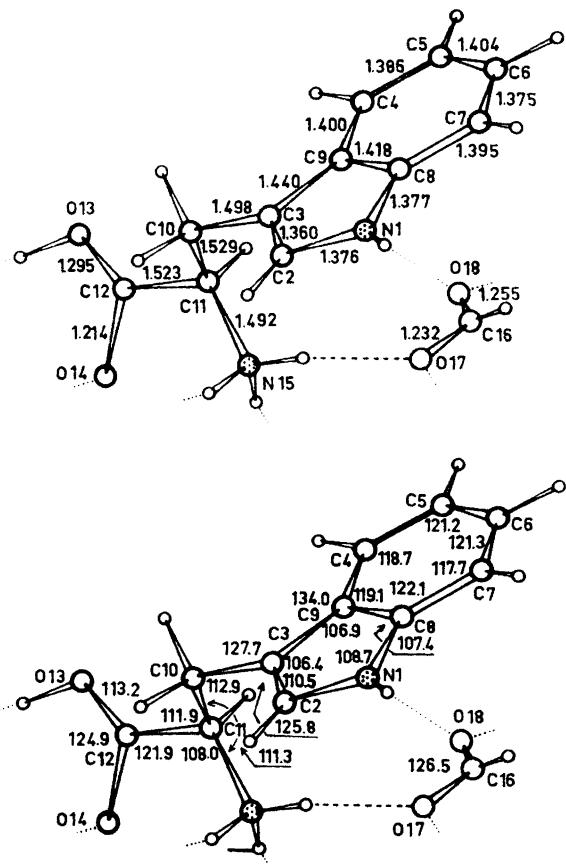


Fig. 1. Bond lengths (\AA) and angles ($^{\circ}$) in DL-tryptophan formate. Bond lengths in the 3-indolymethyl-part are corrected for thermal effects.

of the tryptophan molecules are engaged in the hydrogen bond network; each tryptophan molecule is thus donor in five such bonds and acceptor in one. Each formate ion is hydrogen acceptor in four hydrogen bonds involving different tryptophan molecules ($\text{N}1 - \text{O}18$ 3.003 \AA , $\text{N}15' - \text{O}17$ 2.787 \AA , $\text{O}13'' - \text{O}18$ 2.492 \AA , and $\text{N}15'' - \text{O}17$ 2.811 \AA). The short distance of 2.492 \AA between $\text{O}13''$ and $\text{O}18$ indicates a rather strong competition for the proton situated between the carboxy oxygen atoms. The $\text{O}13 - \text{H}$ bond is found to be relatively long (*cf.* Table 5). The angles $\text{O}13'' - \text{H} \dots \text{O}18$ and $\text{C}16 - \text{O}18 \dots \text{H}$ were found to be 179° and 110° , respectively.

The two $\text{C} - \text{O}$ bond lengths in the formate ion, $\text{C}16 - \text{C}17$ 1.232 \AA and $\text{C}16 - \text{O}18$ 1.255 \AA , are consistent with the ionized state of the molecule. The difference between the two is highly significant, however, and the greater

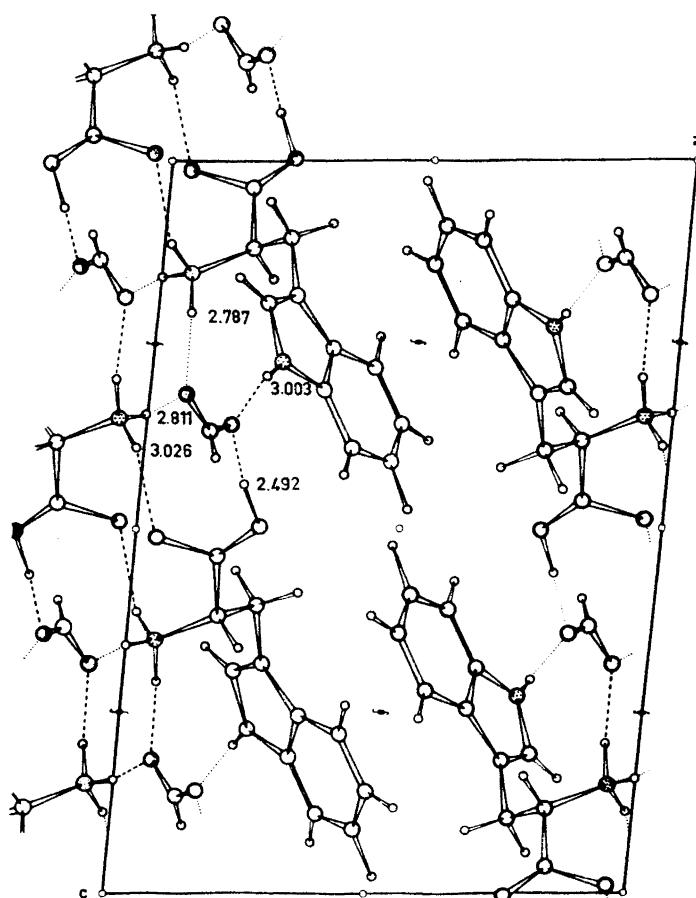


Fig. 2. Molecular arrangement and hydrogen bonds (\AA) in the DL-tryptophan formate crystals as seen along the b -axis.

length of C16–C18 is believed to be due to the very strong O18–O13 hydrogen bond.

In the alanine part of the molecule the two C–O distances agree well with the expected values for a protonized carboxyl group. The slight shortening of the C–OH bond (1.291 Å) relative to the weighted average of such bonds (1.306 Å⁹) is also believed to be a result of the strong hydrogen bond O18–O13. All other bond lengths and angles in the alanine moiety are in agreement with those reported for other α -amino acids. The dihedral angle N15–C11–C12–O14 is only -4.3° and the N15 atom is thus close to the plane of the carboxyl group.

The atoms of the indole moiety are co-planar, the C10 atom also included. The largest deviation from a least-squares plane through these atoms is 0.008

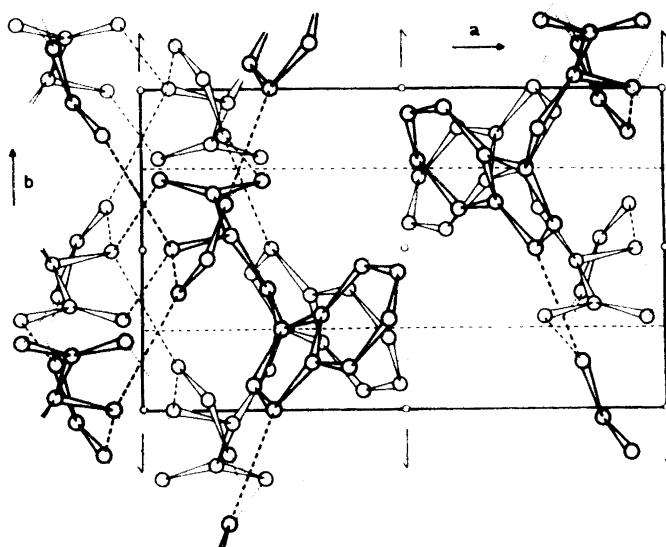


Fig. 3. The crystal structure as seen along the *c*-axis.

Å (C3) The bond lengths and angles in the indole nucleus as given in Table 5 and Fig. 1 are in good agreement with what is found in similar systems, *e.g.* serotonin picrate¹⁰ and 5-methoxy-*N,N*-dimethyl tryptamine,¹¹ and they seem to be typical for such molecules.

The conformation of the tryptophan cation may be described by the torsion angles about the C—C and C—N bonds in the side chain. The dihedral angle C2—C3—C10—C11 is 105.1° and C3—C10—C11—C12 is —174.6°. The C3 atom and the carbon atoms in the alanine part lie thus approximately in a plane which is close to be normal to the indole plane; the carboxyl group is in the *anti* position relative to the indole group. The conformation about the C11—N15 bond is staggered.

REFERENCES

1. Bye, E., Mostad, A. and Rømming, C. *Acta Chem. Scand.* **25** (1971) 364.
2. Dahl, T., Gram, F., Groth, P., Klewe, B. and Rømming, C. *Acta Chem. Scand.* **24** (1970) 2232.
3. Hanson, H. P., Herman, F., Lea, J. D. and Skillman, S. *Acta Cryst.* **17** (1964) 1040.
4. Stewart, R. F., Davidson, E. R. and Simpson, W. T. *J. Chem. Phys.* **42** (1965) 3175.
5. Zachariassen, W. H. *Acta Cryst.* **5** (1952) 68.
6. Karle, J. and Karle I. L. *Acta Cryst.* **21** (1966) 849.
7. Sayre, D. *Acta Cryst.* **5** (1952) 60.
8. Takigawa, T., Ashida, T., Sasada, Y. and Kakudo, M. *Bull. Chem. Soc. Japan* **39** (1966) 2369.
9. Sundaralingam, M. and Putkey, E. F. *Acta Cryst.* **B 26** (1970) 790.
10. Thewalt, U. and Bugg, C. E. *Acta Cryst.* **B 28** (1972) 82.
11. Falkenberg, G. and Carlstrom, D. *Acta Cryst.* **B 27** (1971) 411.

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