

## Studies on Peroxomolybdates

### IX. The Crystal Structure of Potassium Diperoxoheptamolybdate(VI) Octahydrate, $K_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$

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The crystal structure of  $K_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$  has been determined from visually estimated X-ray reflexion intensities, using Patterson and Fourier methods, and refined by the least-squares technique to a final  $R$ -value of 0.097, based on 1593 observed reflexions.

The yellow crystals are orthorhombic, belonging to space group  $C2cm$ , with  $a = 8.487$  (2) Å,  $b = 19.047$  (5) Å,  $c = 19.974$  (5) Å,  $V = 3228.8$  Å<sup>3</sup> and  $Z = 4$ .

The diperoxoheptamolybdate ion has the same general appearance as the normal heptamolybdate ion,<sup>10</sup> the difference being that two peroxy groups replace two oxygen atoms, one at either end of the heptamolybdate ion. The molybdenum atoms which are coordinated to a peroxy group are thus surrounded by seven oxygen atoms. The geometry is pentagonal bipyramidal, the equatorial plane of the bipyramid containing five oxygen atoms, two of which belong to a peroxy group. The apical positions are occupied by one double-bonded and one weakly bonded oxygen atom. Molybdenum is displaced 0.31 Å out of the equatorial plane towards the double-bonded oxygen atom. Bond distances: Mo—O<sub>bridging</sub> 1.76–2.49 Å, Mo—O<sub>peroxy</sub> 1.86–1.96 Å, Mo=O 1.64–1.75 Å and (O—O)<sub>peroxy</sub> 1.38 Å.

Baerwald<sup>1</sup> was, unwittingly, in 1885, probably the first to prepare crystals of  $\text{Ba}_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$ . He dissolved ammonium paramolybdate in an excess of hydrogen peroxide and evaporated the solution isothermally. He formulated the compound he obtained, however,  $14\text{NH}_3 \cdot 18\text{MoO}_3 \cdot 3\text{H}_2\text{O}_2 \cdot 18\text{H}_2\text{O}$ .

From the short historical review of ammonium peroxyheptamolybdates given by Hansson and Lindqvist,<sup>2</sup> it is obvious that the earlier contributions are rather confusing, since the conditions of formation were not studied and the formula of the paramolybdate was unknown until 1937 when Sturdivant<sup>3</sup> showed the paramolybdate to be a heptamolybdate.

By varying the  $\text{MoO}_3 : \text{H}_2\text{O}_2$  ratio or the temperature in solutions of paramolybdates, Gagliotti<sup>4</sup> obtained crystals of varying peroxide content. It is,

however, possible to obtain peroxyheptamolybdates with stoichiometric compositions by choosing the conditions carefully. Stomberg and Trysberg<sup>5</sup> have shown that the nature of the crystals formed by the isothermal evaporation of solutions, obtained by adding hydrogen peroxide and a strong acid to solutions of normal potassium molybdate, depends on the H<sub>2</sub>O<sub>2</sub> : Mo ratio, the acidity and the temperature of the solution. When the H<sub>2</sub>O<sub>2</sub> : Mo ratio is 0.1–0.8 and the pH 5.8–6.8, two peroxyheptamolybdates are obtained, one with orthorhombic and one with monoclinic symmetry. The structure of the orthorhombic peroxyheptamolybdate is described in this paper, while an investigation of the structure of the monoclinic compound is soon to be commenced. Some of the results of the present investigation have been published previously in a preliminary report.<sup>6</sup>

## EXPERIMENTAL

*Preparation of crystals.* Crystals of K<sub>6</sub>Mo<sub>7</sub>O<sub>22</sub>(O<sub>2</sub>)<sub>2</sub>·8H<sub>2</sub>O can be prepared by the method proposed by Trysberg,<sup>7</sup> in which 1.0 ml 8 M hydrogen chloride and 1.75 ml 6 M hydrogen peroxide are added to 20.0 ml 1.3 M potassium molybdate. The acidity of the solution is adjusted to pH = 6.2. The yellow solution is set to evaporate at room temperature (below 25°C), yellow, rod-shaped crystals being eventually deposited.

*Analysis.* Crystals of the potassium diperoxyheptamolybdate used in this investigation were analyzed by Trysberg.<sup>7</sup> (Found: K 15.8; Mo 45.5; O<sub>peroxide</sub> 3.65; H<sub>2</sub>O 10.8. Calc. for K<sub>6</sub>Mo<sub>7</sub>O<sub>24-x</sub>(O<sub>2</sub>)<sub>x</sub>·9H<sub>2</sub>O with x = 1.67; K 15.9; Mo 45.4; O<sub>peroxide</sub> 3.65; H<sub>2</sub>O 11.0.) The analysis indicates nine water molecules in the formula, while the X-ray analysis is more consistent with eight water molecules. It is possible to obtain crystals of the compound with x = 2. The X-ray data were, however, collected from a crystal of the compound with x = 1.67.<sup>6</sup> For simplicity we formulate the compound K<sub>6</sub>Mo<sub>7</sub>O<sub>22</sub>(O<sub>2</sub>)<sub>2</sub>·8H<sub>2</sub>O.

*X-Ray methods.* For the single crystal work multiple-film (5 films) equi-inclination Weissenberg photographs were taken of a crystal of approximate dimensions 0.5 × 0.12 × 0.12 mm<sup>3</sup> with rotation about [100] (layer lines 0–7) and [010] (layer line 0), using CuK $\alpha$  radiation.

The relative intensities of the reflexions were estimated visually by comparison with a standard scale (obtained by the rotating sector method) and were corrected for absorption, extinction, Lorentz and polarization effects. Errors due to anomalous dispersion were taken into consideration but the correction did not affect the result. The |F<sub>o</sub>|-values were brought on to an absolute scale by comparison with the finally calculated structure factors. A total of 1593 independent reflexions was obtained.

*Computing methods.* Absorption, extinction, Lorentz and polarization corrections, Fourier summations, structure factor least-squares refinements, calculations of interatomic distances and angles, calculations of planes to fit sets of atoms and plotting of the crystal structure were performed on the electronic computer IBM 360/65, using the set of crystallographic programmes, *viz.* DATAP2, DRF, LALS, LINUS, DISTAN, PLANEFIT, and ORTEP, in use at this department.<sup>8</sup>

The atomic scattering factors for potassium, molybdenum, and oxygen used in the calculations of the structure factors were taken from Vol. III of the *International Tables for X-Ray Crystallography*, 1962.

## CRYSTAL DATA

Crystal data have been reported previously by Stomberg.<sup>9</sup> K<sub>6</sub>Mo<sub>7</sub>O<sub>22</sub>(O<sub>2</sub>)<sub>2</sub>·8H<sub>2</sub>O is orthorhombic with

$$\begin{array}{l} a = 8.487(2) \text{ \AA} \\ b = 19.047(5) \text{ \AA} \\ c = 19.974(5) \text{ \AA} \\ V = 3228.8 \text{ \AA}^3 \end{array}$$

$$\begin{array}{l} Z = 4 \\ D_{\text{obs}} = 3.08 \text{ g/cm}^3 \\ D_{\text{calc}} = 3.01 \text{ g/cm}^3 \\ \text{Space group} = C2cm \end{array}$$

### STRUCTURE DETERMINATION

*Atomic positions.* Owing to the relatively large number of interatomic vectors, a comparison of the vector set with that obtained for the normal heptamolybdate ion, the structure of which has been determined by Lindqvist<sup>10</sup> and later confirmed by Shimao<sup>11</sup> (Fig. 1), was thought worth-while.

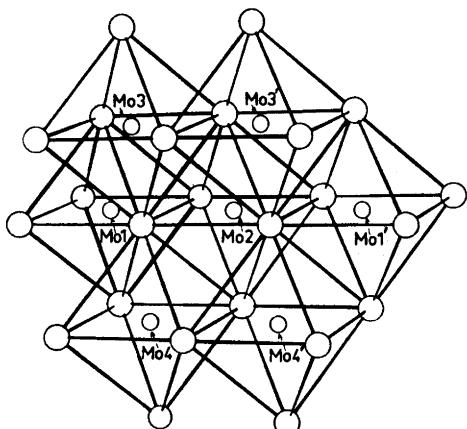


Fig. 1. Idealized structure of the heptamolybdate ion, showing the octahedral arrangement of ligands about molybdenum.

The coordinates of some dominant peaks in the Patterson synthesis are listed in Table 1a together with the observed peak heights and lengths of interatomic vectors. In Table 1b some interatomic distances within the heptamolybdate ion are given.<sup>10</sup> As is apparent from the two tables, there are obvious similarities in vector lengths. The relative orientation of the vectors was also found to be comparable. It therefore seemed likely that the molybdenum atoms were arranged in the same way in the peroxoheptamolybdate as in the normal heptamolybdate. Comparison between expected and observed lengths of vectors indicates that the three molybdenum atoms Mo(1)–Mo(2)–Mo(1') are situated in a straight line parallel to the *c*-axis. Judging from the appearance of the heptamolybdate ion, it is obvious that the correct space group is *C2cm*, with Mo(2) occupying the four-fold position *4b* and the remaining molybdenum atoms occupying three eight-fold positions *8c*. At this stage the *z*-coordinates of all molybdenum atoms were known. The *x*-coordinates were obtained by identifying interatomic vectors Nos. III and V (Table 1b) with Patterson peaks Nos. 4 and 5 (Table 1a), respectively. (Owing to the symmetry of space group *C2cm*, the *x*-coordinate of Mo(2) is fixed at zero.) By identifying Patterson vectors with corresponding expected vectors between molybdenum atoms

*Table 1a.* Coordinates of some dominant peaks in the Patterson synthesis, together with observed peak heights and lengths of interatomic vectors.

Peak No.	<i>u</i>	<i>v</i>	<i>w</i>	Peak height (arbitrary units)	Length of interatomic vector (Å)
1	0	0	0	999	0
2	0	0	0.17	347	3.34
3	0.14	0.22	0	115	4.28
4	0.15	0.14	0.09	95	3.40
5	0	0	0.34	94	6.81
6	0.29	0.08	0.09	82	3.35

*Table 1b.* Some interatomic distances within the heptamolybdate ion. In the last column the corresponding Patterson vectors for the peroxyheptamolybdate ion are given.

Vector No.	Defining atoms	Length of vector (mean value) (Å)	Relative weight	Patterson vector No.
I	Mo(1) - Mo(2)	3.36	4	2
II	Mo(1) - Mo(3)	3.32	2	9
III	Mo(1) - Mo(4)	3.32	2	6
IV	Mo(3) - Mo(4)	4.28	2	4
V	Mo(1) - Mo(1')	6.83	1	7

occupying positions 8c of space group *C2cm* the *y*-coordinates were obtained. The molybdenum parameters thus are:

	Position	<i>x</i>	<i>y</i>	<i>z</i>
Mo(1)	8c	0.0	0.135	0.08
Mo(2)	4b	0	0.135	1/4
Mo(3)	8c	0.29	0.06	0.165
Mo(4)	8c	0.14	0.275	0.165

A Fourier summation of the observed structure factors in which the phases of the Fourier coefficients were determined by the contributions from the molybdenum atoms alone was undertaken. This showed large peaks at the above positions and minor peaks, which were taken to be potassium and water sites. Probable coordinates for the oxygen atoms surrounding the molybdenum atoms according to the heptamolybdate model were also found. On introducing these atoms into a structure factor calculation an *R*-value of 0.25 was obtained. Since the crystal under investigation contained 1.67 peroxy groups per heptamolybdate ion instead of the stoichiometric amount 2, there were assumed to be, on average, 0.165 oxygen atoms and 0.835 peroxy groups at each peroxy group site.

*Structure refinement.* The structure was refined by the structure factor least squares method using 1593 observed reflexions. For each reflexion the weight  $w$  was computed according to  $w = (a + |F_o| + c|F_o|^2 + d|F_o|^3)^{-1}$  with  $a = 10.0$ ,  $c = 0.005$ , and  $d = 0$ . Anisotropic temperature parameters were included

Table 2a. Atomic coordinates (expressed as fractions of the cell edges) and isotropic thermal parameters for  $K_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$ , with the standard deviations of the last significant figures in parentheses. Space group  $C2cm$ ,  $Z = 4$ .

Atom	$x$	$y$	$z$	$B$ ( $\text{\AA}^2$ )
Mo(1)	0.0547(6)	0.1404(1)	0.0818(1)	
Mo(2)	0 <sup>a</sup>	0.1338(1)	1/4	
Mo(3)	0.3167(6)	0.0584(1)	0.1674(1)	
Mo(4)	0.1828(6)	0.2716(1)	0.1672(1)	
K(1)	0.6657(22)	0	0	4.7(2)
K(2)	0.8253(17)	0.3534(5)	1/4	2.9(2)
K(3)	0.5366(12)	0.4046(3)	0.1041(3)	3.4(1)
K(4)	0.5504(14)	0.2056(4)	0.0329(3)	3.8(1)
O(1)	-0.091(5)	0.084(2)	0.029(2)	4.4(6)
O(2)	-0.130(6)	0.154(2)	0.033(2)	5.4(8)
O(1,2)	-0.143(12)	0.114(5)	0.043(4)	0.7(12)
O(3)	-0.120(4)	0.119(1)	0.180(1)	3.1(4)
O(4)	0.172(4)	0.159(1)	0.019(1)	3.6(4)
O(5)	0.187(3)	0.159(9)	0.168(1)	1.9(3)
O(6)	0.131(3)	0.047(1)	0.108(1)	2.4(3)
O(7)	0.009(4)	0.239(1)	0.108(1)	3.4(4)
O(8)	0.121(5)	0.053(2)	1/4	3.0(5)
O(9)	0.018(4)	0.235(1)	1/4	1.6(4)
O(10)	0.447(4)	0.088(2)	0.111(1)	4.1(5)
O(11)	0.409(4)	0.088(1)	1/4	2.3(4)
O(12)	0.340(4)	-0.032(1)	0.171(1)	3.7(5)
O(13)	0.328(4)	0.280(1)	0.112(1)	3.3(4)
O(14)	0.303(4)	0.273(1)	1/4	2.4(5)
O(15)	0.091(3)	0.354(1)	0.174(1)	2.5(3)
O(16)	0.508(6)	0.412(2)	1/4	4.4(7)
O(17)	0.602(7)	0.213(2)	1/4	4.7(8)
O(18)	0.266(4)	0.480(2)	0.138(1)	4.8(6)
O(19)	0.953(4)	0.405(1)	0.050(1)	3.9(5)
O(20)	0.711(4)	0.280(1)	0.133(1)	3.9(5)

<sup>a</sup> Arbitrarily fixed.

Table 2b. Anisotropic temperature parameters  $\beta_{ij}$  (with the standard deviations of the last significant figures in parentheses). The expression used is  $\exp -(\beta_{11}h^2 + \beta_{22}k^2 + \beta_{33}l^2 + \beta_{12}hk + \beta_{13}hl + \beta_{23}kl)$ .

Atom	$\beta_{11}$	$\beta_{22}$	$\beta_{33}$	$\beta_{12}$	$\beta_{13}$	$\beta_{23}$
Mo(1)	0.0100(5)	0.00178(5)	0.00179(5)	0.0001(1)	0.0002(1)	0.00029(4)
Mo(2)	0.0057(6)	0.00128(6)	0.00174(6)	-0.0002(1)	0	0
Mo(3)	0.0104(5)	0.00143(5)	0.00181(5)	0.0007(1)	0.0003(1)	0.00009(4)
Mo(4)	0.0077(5)	0.00149(5)	0.00208(5)	0.0004(1)	0.0003(1)	0.00024(4)

Table 3. Observed and calculated structure factors for  $K_6Mo_7O_{23}(O_2)_2 \cdot 8H_2O$ . The columns are  $l$ ,  $|F_o|$ ,  $|F_c|$  and phase angle  $\alpha$  (expressed in radians), respectively.

$0 \ 0 \ L$	$0 \ 85 \ 85 \ -0.00$	$11 \ 89 \ 88 \ -0.00$	$15 \ 58 \ 54 \ -2.27$	$12 \ 82 \ 72 \ -2.91$	$9 \ 30 \ 20 \ 0.05$	$20 \ 89 \ 82 \ -2.69$
2 262 242 3.14	9 141 147 -0.00	12 53 62 -0.00	16 54 60 -1.97	13 123 126 -1.35	10 28 36 0.25	21 45 35 -1.48
4 250 267 3.14	10 40 30 -0.00	13 80 53 3.14	17 148 126 -2.93	14 92 74 -3.11	11 53 75 3.11	22 21 19 1.72
6 119 107 0.00	11 157 166 -0.00	14 37 33 -0.00	16 141 144 -0.92	15 38 35 -0.19	12 37 43 0.16	23 75 78 -2.29
8 56 41 -0.00	12 150 156 -0.00	15 62 61 -0.00	17 148 146 -1.66	16 78 79 -0.49	13 48 50 -0.22	24 57 73 0.35
10 125 135 3.14	13 191 177 3.14	16 56 56 -0.00	20 32 38 -1.38	17 62 69 -1.47	1 23 L	
12 831 649 -0.00	14 49 60 -0.00	17 35 33 3.14	21 54 60 -0.38	18 149 156 0.33	0 58 69 -0.53	2 8 L
14 534 449 3.14	15 65 57 3.14	18 0 1 3.14	22 25 25 -1.33	19 94 74 2.15	1 98 122 -1.95	0 324 364 0.84
16 85 65 3.14	16 98 98 -0.00	19 27 29 -0.00	23 30 21 0.49	20 24 23 -0.07	2 37 45 2.63	1 252 247 -1.33
18 64 49 0.00	17 67 66 -0.00	18 1 1 0.00	24 61 62 2.93	21 21 22 -0.21	3 27 31 2.49	2 110 122 -2.96
20 95 95 3.14	18 150 152 3.14	19 0 1 0.00	20 18 18 0.00	21 18 18 0.00	4 18 18 0.00	3 111 111 -2.12
22 120 110 3.14	19 18 18 0.00	0 0 18 L	0 18 L	0 18 L	5 94 104 2.21	1 161 161 -1.91
24 207 190 -0.00	0 27 41 0.00	1 5 L	1 13 L	1 13 L	6 42 42 -2.09	5 234 242 2.74
$0 \ 2 \ L$	$0 \ 85 \ 85 \ -0.00$	$1 21 \ 0 \ 3 \ 0.00$	$2 81 \ 89 \ 3.14$	$3 166 \ 506 \ -0.88$	$7 \ 66 \ 91 \ -1.35$	$8 227 \ 226 \ 2.33$
0 205 216 3.14	22 0 5 0.00	3 59 56 -0.00	2 83 68 2.54	2 116 124 0.41	7 247 274 0.08	
1 406 384 3.14	24 20 35 -0.00	4 88 95 3.14	3 147 152 0.94	3 77 69 1.06	2 0 L	8 126 137 -1.82
2 45 30 -0.00	5 0 12 0.00	5 10 42 3.14	4 114 110 2.58	4 60 59 -1.39	2 1 357 3.60	9 127 129 0.61
3 171 171 3.14	5 12 32 -0.00	5 12 32 0.00	5 12 32 0.00	5 12 32 0.00	2 444 453 0.00	10 126 126 -0.00
4 26 33 3.14	0 364 376 3.14	6 78 70 3.14	7 148 186 -2.01	7 326 289 2.74	8 156 139 -0.04	12 268 294 0.86
5 251 267 3.14	1 202 181 -0.00	9 0 0 -0.00	8 0 10 2.41	8 47 41 1.36	10 173 189 0.79	13 128 141 -1.26
6 72 67 -0.00	2 256 245 -0.00	10 45 40 3.14	9 103 111 -2.12	9 130 124 -2.30	12 149 139 2.35	14 38 46 2.71
7 63 7 3.14	3 0 12 3.14	11 0 12 0.00	10 53 44 1.62	10 47 47 0.59	14 87 84 1.96	15 38 47 -2.33
8 19 14 0.00	4 112 127 -0.00	12 29 29 -0.00	11 276 276 2.34	11 122 124 -2.25	13 149 152 -1.02	16 64 62 -1.00
9 22 22 0.00	5 448 453 3.14	13 44 44 -0.00	12 130 130 0.00	13 149 152 -0.00	14 277 231 0.00	17 98 88 0.06
10 17 192 3.00	13 44 44 0.00	14 51 57 3.14	13 268 247 -0.86	14 144 145 0.94	15 90 86 -0.35	19 65 65 -0.91
11 168 168 -0.00	7 312 338 -0.00	15 63 66 -0.00	14 102 120 0.67	14 48 46 0.87	22 0 15 1.40	19 95 97 -0.25
12 24 21 3.14	8 118 141 0.00	16 43 40 3.14	15 123 110 1.14	15 0 6 0.64	22 22 26 2.40	20 65 61 -1.73
13 213 232 3.14	9 52 59 0.00	16 51 57 3.14	15 268 247 -0.86	14 144 145 0.94	15 90 86 -0.35	21 0 8 2.37
14 75 73 0.00	10 97 112 0.00	0 20 L	17 163 175 0.80	17 125 121 -0.65	2 2 L	22 31 34 -2.77
15 118 101 3.14	11 75 61 -3.14	0 55 38 -0.00	18 106 106 -0.83	18 106 107 -2.26	0 532 455 -1.71	23 30 38 2.76
16 145 145 -0.00	1 30 30 3.14	0 6 0 -0.00	19 106 106 0.00	19 92 92 2.28	2 199 199 2.06	2 10 L
17 100 98 3.14	2 108 82 -0.00	2 108 82 -0.00	20 0 12 1.06	2 108 198 1.16	3 102 112 1.56	0 139 117 -0.14
18 72 64 -0.00	14 57 43 0.00	3 44 32 0.00	21 62 65 -2.40	1 67 56 2.92	5 528 453 -2.37	2 76 71 61 -2.15
20 42 35 -0.00	16 28 31 -0.00	5 154 166 -0.00	23 87 95 2.38	1 67 56 2.92	5 528 453 -2.37	7 184 184 0.00
21 87 65 -0.00	17 163 157 3.14	6 84 51 3.14	24 43 47 -2.02	1 132 130 -2.05	6 397 371 -1.56	7 96 84 -1.90
22 25 24 0.00	7 216 207 3.14	7 216 207 3.14	1 132 130 -2.05	7 184 184 0.00	7 397 371 -1.56	7 96 84 -1.90
23 29 29 0.00	10 149 149 -0.00	8 0 6 -0.00	1 132 130 -2.05	1 132 130 -2.05	8 249 251 1.57	5 131 134 -1.33
24 35 31 3.14	20 61 65 -0.00	9 37 31 3.14	0 554 485 0.14	9 17 0 0.26	6 281 278 0.58	
25 40 43 3.14	21 9 6 3.14	10 57 52 -0.00	1 77 87 -0.49	6 183 166 2.44	10 180 192 1.57	7 131 132 1.63
23 25 41 0.00	23 51 48 -0.00	11 0 16 -0.00	2 30 24 0.08	7 63 74 3.13	13 135 132 0.06	8 60 53 2.32
23 25 18 3.14	12 0 8 3.14	12 0 8 3.14	3 93 76 -2.26	8 101 108 -1.92	12 182 192 1.51	9 53 51 2.86
0 181 200 3.14	13 44 43 3.14	13 44 43 3.14	4 77 69 1.40	9 100 87 0.67	13 79 72 2.41	10 92 95 -2.41
$0 \ 181 \ 200 \ L$	0 12 L	0 12 L	0 12 L	0 12 L	0 12 L	0 12 L
2 73 97 -3.14	0 144 167 3.14	0 22 L	6 163 163 -2.16	11 126 126 -0.15	15 92 96 -1.06	17 184 184 0.00
3 186 197 -0.00	0 153 171 -0.00	7 159 171 -0.00	7 159 171 -0.00	12 181 189 0.89	16 120 124 1.42	13 172 186 -3.10
4 170 192 3.14	2 119 104 -0.00	1 65 46 3.14	8 152 167 -2.94	13 65 48 2.99	17 199 213 2.56	14 121 132 -2.73
5 61 502 -0.00	3 168 180 -0.00	2 63 51 3.14	9 44 44 -0.16	14 77 59 -0.75	19 94 87 -1.06	15 34 36 -0.44
6 749 607 -0.00	4 0 0 0.03	3 54 50 3.14	10 133 131 -3.00	15 69 61 -2.93	19 144 130 0.64	16 62 67 3.13
7 157 178 3.14	5 118 127 -0.00	4 24 28 3.14	11 119 130 2.88	16 71 71 -0.84	20 98 92 1.52	17 36 37 3.14
8 44 44 -0.00	5 64 60 -0.00	5 64 60 -0.00	12 252 252 0.00	12 252 252 0.00	22 37 34 2.94	18 29 39 0.41
9 0 0 0.00	13 129 124 -0.14	6 72 79 -2.14	13 129 124 -0.09	14 75 86 2.50	15 23 24 1.88	19 29 39 0.41
10 59 51 3.14	8 68 60 -0.00	7 35 45 3.14	14 43 40 -2.47	19 19 23 2.96	23 73 71 0.18	20 26 15 1.93
11 200 200 -0.00	9 97 97 3.14	8 17 16 0.00	15 0 5 2.29	19 19 23 2.96	24 67 73 -1.74	21 0 5 2.29
12 90 122 3.14	9 103 98 -0.00	9 50 50 -0.00	15 56 60 -2.70	1 17 L	22 31 35 -2.71	
13 123 133 3.14	11 84 67 3.14	10 16 0 0.00	17 0 16 0.65	0 107 107 -2.85	2 4 L	
14 80 80 0.00	12 93 92 3.14	0 24 L	18 112 110 -2.59	0 107 107 -2.05	2 12 L	
15 68 68 0.00	0 38 136 3.14	1 73 79 -1.08	2 0 12 -2.24	1 439 410 0.41	0 56 59 -2.65	
16 58 54 3.14	14 61 49 -0.00	1 34 39 3.14	20 72 68 -2.92	3 37 34 -2.16	2 121 137 -0.76	1 211 231 -0.51
17 125 119 0.00	15 62 64 -0.00	2 46 59 -0.00	21 27 22 3.14	4 101 98 -0.16	3 123 137 0.55	2 64 59 1.99
18 223 215 -0.00	16 0 12 3.14	2 30 30 -2.28	5 132 132 -2.58	4 237 238 0.76	3 111 109 0.80	
19 165 165 3.14	17 42 32 -0.00	1 1 L	6 58 58 1.57	5 54 61 1.84	4 170 156 -2.94	
20 25 26 3.14	18 46 56 -0.00	2 229 212 -1.29	7 150 150 0.48	6 249 260 1.03	5 336 316 1.07	
21 24 28 -3.14	19 50 34 3.14	2 229 212 -1.29	16 65 101 0.18	6 56 56 -0.34	6 151 146 0.38	
23 54 50 -0.00	4 161 171 -0.00	3 73 79 -1.08	7 73 79 -1.08	9 0 15 0.93	6 339 320 -0.11	
24 41 41 3.14	21 25 17 3.14	5 399 348 3.14	0 646 542 -1.55	10 47 37 -2.63	9 27 29 1.07	8 4 19 -2.58
25 46 56 3.14	22 13 16 -0.00	6 551 436 3.13	1 491 449 -2.98	11 60 58 -0.59	10 146 143 -1.20	5 50 59 -2.23
$0 \ 6 \ L$	$0 \ 14 \ L$	$0 \ 14 \ L$	$1 \ 9 \ L$	$1 \ 9 \ L$	$2 \ 4 \ L$	
0 269 266 3.14	0 391 386 -0.00	9 188 171 0.79	4 155 159 2.16	14 41 37 -2.71	13 213 220 0.58	
1 119 119 0.00	10 108 108 -0.00	5 188 188 3.04	5 188 188 3.04	15 108 108 -1.22	13 103 109 0.00	
2 223 223 0.00	2 211 211 3.14	5 345 345 3.14	1 12 12 0.00	1 12 12 0.00	2 211 211 3.14	
3 79 78 0.00	3 33 34 -0.00	12 234 216 1.21	7 195 204 -0.16	17 58 75 -2.53	16 31 32 2.03	15 42 32 1.75
4 324 283 -0.00	4 35 38 -0.57	12 234 216 2.18	7 195 204 -0.16	17 58 75 -2.53	16 31 32 2.03	15 42 32 1.75
5 23 13 -0.00	5 158 148 3.14	14 95 107 -1.60	9 46 46 0.79	14 39 44 -3.22	15 31 31 1.49	16 21 21 0.37
6 125 155 3.14	6 36 51 3.14	15 47 46 -2.32	10 110 113 1.52	1 13 140 1.01	2 6 L	
7 120 127 -3.14	7 131 134 -0.00	16 36 33 -1.44	11 136 142 0.09	0 173 182 2.34	20 32 34 1.25	
8 118 118 3.14	8 118 118 3.14	16 36 33 -1.44	12 136 142 0.09	0 173 182 2.34	20 32 34 1.25	
9 118 118 3.14	9 0 24 -0.00	16 149 149 2.70	12 211 243 -0.06	2 89 88 -0.34	2 38 28 -0.64	2 14 L
10 72 76 -0.00	10 74 70 3.14	19 138 128 -1.64	14 152 159 1.83	3 46 53 0.74	23 86 77 -2.56	0 134 108 1.11
11 179 179 3.14	11 204 219 3.14	16 52 46 -0.90	15 57 65 1.62	11 120 119 2.03	4 88 81 2.76	8 86 77 -1.77
12 21 11 -0.00	12 216 220 -0.00	21 33 21 0.41	16 79 72 0.99	5 112 107 1.10	5 226 224 -0.76	9 0 14 0.32
23 46 34 3.14	20 39 48 3.14	1 64 63 -0.10	17 60 62 2.94	6 135 140 1.01	6 110 122 0.26	10 30 30 1.89
23 46 34 3.14	20 39 48 3.14	5 59 63 -0.10	0 181 181 -2.98	15 36 46 0.72	9 152 151 -2.30	11 68 66 3.02
24 0 0 0.00	0 87 57 3.14	4 104 122 -1.12	1 191 191 1.44	1 21 L	10 105 106 2.61	14 62 57 0.89
$0 \ 8 \ L$	$0 \ 14 \ L$	$0 \ 14 \ L$	$1 \ 9 \ L$	$1 \ 9 \ L$	$2 \ 4 \ L$	
0 192 222 -0.00	3 98 99 3.14	5 456 409 3.10	2 101 102 -2.33	0 117 117 1.16	5 227 234 3.04	1 11 12 121 -2.00
1 327 340 3.14	4 70 56 -0.00	8 176 176 -1.95	3 138 127 0.21	0 117 109 0.41	11 315 315 -2.26	15 0 11 2.23
2 322 322 3.14	6 118 118 3.14	9 64 63 -0.10	4 103 95 -2.83	1 108 98 -0.02	12 181 186 0.34	16 0 15 1.78
3 263 257 3.14	6 44 32 -0.00	10 93 99 -0.22	4 103 95 -2.83	2 23 30 0.11	13 112 116 0.40	17 80 78 0.05
4 87 46 -0.00	7 0 9 -0.00	11 0 22 -0.69	8 80 89 -0.68	3 37 28 -0.78	15 105 107 1.20	19 70 76 -0.97
5 115 118 0.00	8 0 24 3.14	12 276 245 2.99	9 38 38 -0.72	6 131 132 2.66	17 96 103 0.23	20 27 37 1.77
6 277 307 3.14	9 31 38 -0.00	13 67 63 0.38	10 32 31 1.80	7 45 40 -0.68	8 0 14 1.89	2 16 L
7 23 15 -0.00	10 36 43 3.14	14 151 160 -1.86	11 117 119 -0.92	8 0 9 0.51	19 77 74 2.14	0 139 130 -1.56

Table 3. Continued.

1 146 143 -2.12	20 68 52 2.66	6 78 72 -0.40	8 183 190 -1.76	21 28 42 2.41	10 118 114 1.59	3 71 64 1.26
2 106 96 2.24	21 62 54 0.53	7 136 114 -1.91	9 160 160 1.79	11 136 142 0.36	4 196 171 2.79	
3 97 89 -2.32	22 38 30 -0.17	8 71 60 -2.42	10 113 122 -1.70	4 12 L	5 142 121 2.77	
4 100 111 1.06	23 92 120 0.36	9 108 99 -1.73	11 219 222 0.99	12 97 71 2.92	6 194 189 0.25	
5 137 112 1.94	24 42 49 -2.22	10 143 120 -1.96	12 194 200 1.67	13 117 118 2.75	7 103 99 2.74	
6 111 132 -1.81	11 143 123 -2.04	11 143 123 -1.88	13 194 200 -2.04	14 88 64 1.49	8 102 97 2.54	
7 98 105 0.77	3 5 L	12 146 141 0.44	14 88 77 -1.70	15 77 64 -0.53	7 103 97 2.54	
8 93 97 1.17	0 165 168 -2.13	13 127 131 -0.09	15 127 126 -1.45	16 88 64 -0.53	8 102 97 2.54	
9 42 44 1.48	1 182 188 1.47	14 57 49 -3.00	16 65 74 -1.83	9 218 222 -1.35	10 93 70 2.65	
10 69 57 2.66	2 129 133 -1.61	15 54 53 1.53	17 80 70 3.04	10 203 214 1.35	11 98 78 0.79	
11 144 111 1.18	3 135 164 1.39	16 47 31 -2.32	18 162 162 1.53	11 164 143 2.15	12 123 125 -0.72	
12 91 91 -1.11	4 145 151 -2.24	17 51 44 1.65	19 162 162 2.15	20 70 54 0.25	13 37 45 -2.86	
13 94 111 -2.11	5 151 156 -2.04	18 59 54 -2.04	20 70 54 2.15	21 65 55 2.47	14 93 97 1.40	
14 68 58 1.55	6 248 291 0.67	19 26 30 -0.93	21 121 97 2.74	22 15 25 1.75	15 0 6 2.30	
15 63 53 -2.09	7 146 152 2.04	20 26 30 -0.93	22 31 30 -1.39	16 49 37 1.15	17 31 31 0.77	
16 60 68 0.79	8 130 127 -2.80	3 15 L	17 80 70 3.04	19 63 56 1.60	18 90 91 2.79	
17 55 61 2.84	9 150 156 -2.07	0 115 96 0.54	23 65 74 0.95	20 70 54 2.25	19 45 53 1.95	
18 56 75 -2.17	10 47 30 -1.26	1 131 119 -0.34	24 6 L	21 65 55 2.47	22 15 25 1.75	
2 18 L	11 130 127 -2.00	2 131 119 -0.34	2 22 20 -1.87	23 65 74 0.95	24 5 L	
0 289 291 -3.00	12 57 44 0.86	3 59 54 -2.80	4 140 146 -0.09	14 33 34 2.21	5 13 L	
1 111 117 2.25	13 105 103 1.62	4 103 89 -0.08	5 22 66 0.11	15 78 70 1.45	6 139 26 -2.70	
2 65 61 -0.46	14 40 52 0.32	5 101 101 2.99	6 140 146 -0.09	16 33 34 2.21	7 244 254 -3.06	
3 0 21 0.41	15 104 102 1.26	6 150 137 -2.33	7 151 161 1.39	17 78 82 1.31	8 139 26 -2.70	
4 81 74 0.86	16 0 18 1.25	7 139 132 0.11	8 161 175 1.92	18 78 82 1.31	9 139 26 -2.70	
5 53 51 -1.22	17 65 59 0.13	8 47 51 -0.59	9 165 157 0.30	19 78 82 1.31	10 139 26 -2.70	
6 52 50 -1.23	18 65 59 0.13	9 47 51 -0.59	10 172 172 0.29	20 25 30 1.75	11 139 26 -2.70	
7 77 81 1.16	19 70 59 0.94	10 59 54 -2.34	8 140 146 -0.09	21 35 34 2.21	12 139 26 -2.70	
8 81 74 1.03	20 27 25 -2.58	11 97 87 2.50	9 40 35 -0.80	13 66 67 1.26	13 139 26 -2.70	
9 0 23 2.77	21 69 63 -1.71	12 80 81 0.30	10 55 55 -1.10	14 25 30 1.75	14 139 26 -2.70	
10 53 52 -0.37	22 28 27 0.16	13 94 99 -0.23	11 111 101 1.76	15 66 55 1.93	15 139 26 -2.70	
11 71 65 -0.94	23 53 51 -1.93	14 96 86 -1.46	12 172 266 -2.00	16 55 36 -0.57	16 139 26 -2.70	
12 151 162 -2.44	24 52 50 -0.32	15 101 101 2.99	13 129 123 1.27	17 56 53 2.37	17 139 26 -2.70	
13 58 52 -1.10	25 52 50 -0.32	16 150 137 -2.33	14 166 175 1.92	18 66 53 2.37	18 139 26 -2.70	
14 59 59 -0.33	0 121 133 1.93	17 90 87 -2.86	15 166 175 1.92	19 66 53 2.37	19 139 26 -2.70	
15 28 31 0.03	1 92 86 -3.06	18 60 77 -2.34	16 56 50 2.24	20 66 53 2.37	20 139 26 -2.70	
16 23 31 1.06	2 228 226 -0.87	19 34 33 -2.95	17 50 35 1.85	21 66 53 2.37	21 139 26 -2.70	
2 22 L	23 41 33 -2.95	3 17 L	18 38 16 0.49	22 66 53 2.37	22 139 26 -2.70	
0 225 253 -0.05	4 256 253 -0.15	0 156 144 -0.44	19 62 66 -1.77	23 35 35 0.32	23 139 26 -2.70	
1 235 253 -0.05	5 164 157 -2.76	20 67 58 2.34	20 82 78 1.27	24 35 35 0.32	24 139 26 -2.70	
2 235 253 -0.05	6 164 157 -2.76	21 59 58 1.16	21 82 78 1.27	25 35 35 0.32	25 139 26 -2.70	
3 152 144 0.29	7 141 162 3.03	3 65 53 -2.44	22 40 50 -0.31	26 35 35 0.32	26 139 26 -2.70	
2 88 76 1.07	8 238 246 -0.26	4 112 98 -2.29	23 17 19 2.66	27 35 35 0.32	27 139 26 -2.70	
3 31 33 1.78	9 79 85 0.42	5 39 20 -2.34	24 10 12 2.23	28 35 35 0.32	28 139 26 -2.70	
4 80 59 0.88	10 48 44 0.35	6 227 244 0.27	25 10 12 2.23	29 35 35 0.32	29 139 26 -2.70	
5 0 10 -0.33	7 19 77 -0.37	7 10 12 2.23	26 10 12 2.23	30 35 35 0.32	30 139 26 -2.70	
6 80 74 -1.42	12 105 93 2.41	8 78 75 2.75	27 10 12 2.23	31 35 35 0.32	31 139 26 -2.70	
7 0 13 2.41	13 105 93 2.41	9 78 75 2.75	28 10 12 2.23	32 35 35 0.32	32 139 26 -2.70	
8 60 49 2.35	14 123 124 0.94	10 74 77 -2.57	3 164 166 2.18	33 35 35 0.32	33 139 26 -2.70	
9 57 55 -1.73	15 48 42 2.27	11 108 97 0.53	4 46 44 -1.30	34 35 35 0.32	34 139 26 -2.70	
10 72 70 1.12	16 135 139 -0.47	12 90 84 -0.68	5 269 270 1.22	35 35 35 0.32	35 139 26 -2.70	
11 118 129 -2.77	17 106 111 0.23	13 123 113 -2.78	6 98 92 -1.48	36 35 35 0.32	36 139 26 -2.70	
12 42 42 -0.68	18 123 124 -2.89	14 51 52 -2.56	7 314 337 -0.26	37 35 35 0.32	37 139 26 -2.70	
13 64 64 0.22	19 90 90 -3.04	15 36 31 -0.83	8 164 166 -1.19	38 35 35 0.32	38 139 26 -2.70	
2 22 L	20 130 96 -0.56	16 47 53 -2.93	9 164 166 0.91	39 35 35 0.32	39 139 26 -2.70	
1 40 22 -0.81	21 40 22 -0.81	10 87 82 -2.44	7 123 116 1.16	40 35 35 0.32	40 139 26 -2.70	
0 113 113 1.09	22 30 21 1.15	11 146 131 2.46	8 106 106 -1.29	41 35 35 0.32	41 139 26 -2.70	
1 58 57 0.75	23 19 23 -1.17	0 158 127 -2.33	12 62 66 0.93	42 35 35 0.32	42 139 26 -2.70	
2 24 18 -1.86	1 62 75 1.52	1 167 168 -1.31	13 62 66 0.93	43 35 35 0.32	43 139 26 -2.70	
3 23 22 -2.84	3 32 35 1.72	3 167 168 -1.31	14 62 66 0.93	44 35 35 0.32	44 139 26 -2.70	
4 58 57 -0.94	4 32 35 1.72	4 164 166 -1.31	15 62 66 0.93	45 35 35 0.32	45 139 26 -2.70	
5 73 88 -0.49	5 102 102 1.02	5 164 166 -1.31	16 62 66 0.93	46 35 35 0.32	46 139 26 -2.70	
6 106 122 2.89	1 102 97 2.05	6 164 166 -1.31	17 59 159 -1.09	47 35 35 0.32	47 139 26 -2.70	
7 70 81 0.99	2 82 99 2.05	7 164 166 -1.31	18 77 70 -1.97	48 35 35 0.32	48 139 26 -2.70	
8 55 56 -1.01	3 245 212 -1.89	8 164 166 -1.31	19 99 97 -1.97	49 35 35 0.32	49 139 26 -2.70	
9 16 22 0.35	5 258 264 -2.54	9 164 166 -1.31	20 30 31 -2.58	50 35 35 0.32	50 139 26 -2.70	
3 1 L	10 24 31 -0.01	0 182 180 -0.79	21 41 39 -0.83	51 35 35 0.32	51 139 26 -2.70	
0 428 447 0.35	8 78 83 -0.53	1 164 166 -1.31	22 0 2 2.71	52 35 35 0.32	52 139 26 -2.70	
1 38 48 0.56	9 102 102 1.54	12 61 57 -2.15	23 29 29 0.25	53 35 35 0.32	53 139 26 -2.70	
2 179 242 2.81	10 59 52 -0.79	13 47 48 1.55	24 0 2 2.71	54 35 35 0.32	54 139 26 -2.70	
3 90 93 -1.54	11 34 25 1.51	14 24 31 -0.01	0 182 180 -0.79	55 35 35 0.32	55 139 26 -2.70	
4 117 147 -1.77	12 92 95 1.01	15 124 125 2.30	5 102 102 1.95	56 35 35 0.32	56 139 26 -2.70	
5 137 147 -2.96	13 53 51 -0.86	3 164 166 -1.31	1 164 166 -1.31	57 35 35 0.32	57 139 26 -2.70	
6 261 262 -1.42	4 51 36 -0.86	4 164 166 -1.31	2 164 166 -1.31	58 35 35 0.32	58 139 26 -2.70	
7 412 427 0.58	5 102 102 1.54	5 164 166 -1.31	3 164 166 -1.31	59 35 35 0.32	59 139 26 -2.70	
8 70 64 1.89	6 19 0 -0.96	6 164 166 -1.31	4 164 166 -1.31	60 35 35 0.32	60 139 26 -2.70	
9 169 179 1.37	7 19 82 -0.87	7 164 166 -1.31	5 164 166 -1.31	61 35 35 0.32	61 139 26 -2.70	
10 120 111 2.31	8 73 65 1.39	8 164 166 -1.31	6 164 166 -1.31	62 35 35 0.32	62 139 26 -2.70	
11 51 61 0.66	9 99 88 -0.33	9 164 166 -1.31	7 164 166 -1.31	63 35 35 0.32	63 139 26 -2.70	
12 203 331 2.04	10 23 30 -0.32	10 164 166 -1.31	8 164 166 -1.31	64 35 35 0.32	64 139 26 -2.70	
13 88 88 -0.44	21 61 49 2.54	11 164 166 -1.31	9 164 166 -1.31	65 35 35 0.32	65 139 26 -2.70	
14 94 97 2.60	22 18 29 -2.21	12 82 17 -0.64	10 164 166 -1.31	66 35 35 0.32	66 139 26 -2.70	
15 81 79 -1.45	13 59 51 -0.00	11 95 101 -0.85	11 164 166 -1.31	67 35 35 0.32	67 139 26 -2.70	
16 0 8 1.16	14 28 31 -0.03	12 89 99 -0.74	12 164 166 -1.31	68 35 35 0.32	68 139 26 -2.70	
17 149 159 -2.48	0 381 365 -2.96	13 67 63 -2.04	13 164 166 -1.31	69 35 35 0.32	69 139 26 -2.70	
18 72 65 -0.93	100 100 94 -0.57	14 115 111 -1.31	14 164 166 -1.31	70 35 35 0.32	70 139 26 -2.70	
19 10 10 0.00	3 84 82 -0.75	15 64 57 -2.11	15 164 166 -1.31	71 35 35 0.32	71 139 26 -2.70	
20 0 23 1.38	4 91 95 -1.54	16 174 166 -1.31	16 164 166 -1.31	72 35 35 0.32	72 139 26 -2.70	
21 63 33 1.88	5 399 404 -2.30	2 73 60 -0.99	17 164 166 -1.31	73 35 35 0.32	73 139 26 -2.70	
22 56 40 2.94	6 153 152 -0.44	3 137 120 -1.14	0 51 58 -0.59	74 35 35 0.32	74 139 26 -2.70	
23 0 5 0.27	10 67 66 2.50	4 99 89 2.42	1 56 64 -1.54	75 35 35 0.32	75 139 26 -2.70	
24 67 64 0.44	14 39 41 -0.85	5 100 90 3.12	2 49 54 2.24	76 35 35 0.32	76 139 26 -2.70	
25 44 44 2.99	15 39 41 -0.85	6 70 68 -0.49	3 31 36 -1.76	77 35 35 0.32	77 139 26 -2.70	
26 39 41 2.99	16 118 120 -0.68	7 75 68 -0.58	4 31 36 -1.76	78 35 35 0.32	78 139 26 -2.70	
27 46 47 0.78	18 119 132 -2.24	8 80 92 -1.64	5 32 50 1.41	79 35 35 0.32	79 139 26 -2.70	
28 29 26 -3.00	10 33 29 0.74	9 72 68 2.48	6 164 166 -1.31	80 35 35 0.32	80 139 26 -2.70	
29 11 98 95 0.67	11 98 95 0.67	10 90 126 -2.60	7 164 166 -1.31	81 35 35 0.32	81 139 26 -2.70	
30 23 33 40 -2.58	4 2 L	12 175 192 -1.79	8 164 166 -1.31	82 35 35 0.32	82 139 26 -2.70	
31 13 106 114 0.57	5 2 L	13 164 166 -1.31	9 164 166 -1.31	83 35 35 0.32	83 139 26 -2.70	
32 138 37 2.54	6 174 166 -1.31	14 80 92 -2.39	3 114 142 -0.18	84 35 35 0.32	84 139 26 -2.70	
33 271 293 -2.82	7 174 166 -1.31	15 72 68 -1.65	4 92 105 -0.36	85 35 35 0.32	85 139 26 -2.70	
34 111 111 -0.60	8 221 277 -1.61	16 72 68 -1.65	5 114 119 2.46	86 35 35 0.32	86 139 26 -2.70	
35 135 135 -1.50	9 230 280 -1.71	17 26 19 3.08	6 164			

Table 3. Continued.

6 122 132 -1.49	8 124 125 -0.43	12 87 70 -2.78	2 63 38 2.38	16 42 44 -0.86	7 7 1	8 81 62 2.89
7 61 58 -2.82	9 132 139 -0.79	13 0 10 -0.39	14 115 127 -0.74	4 50 55 1.13	0 146 27 2.14	10 52 56 -0.08
8 71 70 -2.05	10 0 10 -0.39	14 115 127 -0.74	4 50 55 1.13	18 33 30 2.00	1 36 27 1.46	10 52 56 -0.08
9 109 104 2.54	11 142 151 -1.73	15 57 47 -0.43	5 60 43 0.20	19 60 76 -1.11	2 91 91 3.08	11 60 30 -1.40
10 75 76 0.99	12 83 83 2.79	16 0 10 -1.56	6 69 65 -1.61		3 44 45 -2.79	12 52 45 -2.12
11 62 67 0.65	13 91 96 1.17	17 77 86 -2.76	7 59 39 -2.27		4 99 94 -0.10	13 54 55 1.77
12 52 54 -0.77	14 104 104 -0.58	16 43 57 2.07	8 59 39 -2.27	0 21 37 -2.25	5 50 34 -0.23	14 74 92 -0.23
13 43 47 2.81	15 71 72 2.68		9 60 55 2.36	1 64 79 -2.31	6 64 58 -2.31	15 40 23 1.75
14 67 62 1.00	16 60 63 -0.22	6 12 L	10 32 28 2.87	2 81 91 -0.73	7 64 58 2.85	
15 92 91 -0.82	17 0 9 -0.68	0 46 34 -2.60	11 63 66 0.93	3 85 87 -0.33	8 102 89 -0.46	7 13 L
16 48 48 1.62	18 63 67 -2.72	0 46 34 -2.61	12 43 57 -3.97	4 108 122 -2.80	9 30 22 0.56	0 92 41 -2.48
17 74 84 -1.43	19 36 47 1.80	2 132 96 -0.54	13 33 60 -1.92	5 43 45 -0.58	10 65 64 -2.80	1 145 113 1.26
18 34 34 -0.56	20 33 49 -0.50	3 112 104 -2.25	4 40 44 -2.76	6 123 155 1.88	11 31 24 -1.73	2 65 54 2.02
19 32 49 1.99		4 40 44 -2.76	5 18 10 6 L	7 7 1	12 83 70 2.11	3 147 113 2.56
20 39 42 1.82	6 8 L	5 159 131 1.35	0 130 121 -0.50	8 91 78 -0.73	13 0 0 0	4 36 36 -0.59
21 54 70 2.03	0 218 191 1.45	6 58 28 0.60	1 24 27 2.70	9 66 50 2.48	14 38 38 -2.97	5 73 72 -1.13
	1 195 173 -2.49	7 157 149 -1.52	2 37 34 -1.03	10 94 91 -0.72	15 28 25 -3.06	6 94 101 -1.30
6 4 L	2 58 57 -2.47	8 45 48 2.16	3 42 21 0.07	11 39 37 -0.13	15 42 57 -0.21	7 27 32 1.94
0 161 159 -0.60	3 110 101 -1.21	9 84 82 -1.00	4 81 91 2.92	12 41 33 -1.06	17 23 27 0.61	8 46 30 1.55
1 149 114 2.40	4 118 106 -2.66	10 52 52 0.11	5 93 56 -3.02	13 51 49 2.57		9 100 117 -0.59
2 98 99 -0.83	5 120 105 0.59	11 44 46 0.50	6 100 99 0.50	14 49 49 -0.43	7 9 L	10 75 72 1.47
3 90 105 1.97	6 87 81 3.04	12 34 28 2.64	7 90 86 0.77	15 65 71 -0.80	0 219 212 -1.46	11 75 72 -0.44
4 166 185 2.84	7 108 101 2.73	13 35 30 -0.52	8 71 85 2.92	16 44 54 -2.55	1 91 62 -2.24	12 47 37 1.91
5 120 127 0.16	8 139 155 -0.51	14 50 55 -0.47	9 38 25 2.81	17 33 29 -1.07	2 108 78 1.79	13 53 63 1.18
6 205 216 0.85	9 115 112 2.26	15 55 62 2.43	18 70 60 1.63	3 186 160 -0.67		
117 114 1.29	10 55 52 3.44	16 26 25 -2.98	4 72 60 1.20	4 72 60 1.20	7 15 L	
8 144 144 -0.99	11 146 146 -0.79	17 55 59 1.39	5 80 56 -2.47	5 36 36 -2.00	0 130 106 1.55	
9 43 38 -0.40	2 127 130 1.60		1 47 49 2.61	0 197 171 -1.64	6 215 210 1.59	1 71 46 0.32
10 118 116 -0.83	13 97 104 -2.57	6 14 L	2 46 57 1.03	1 150 144 -1.77	7 33 36 0.04	2 84 92 -2.31
11 191 92 -0.02	14 44 45 -2.96	0 113 98 0.96	3 38 52 2.72	2 73 67 -0.30	8 86 85 1.69	3 42 48 -0.77
12 98 92 -0.67	15 50 56 -0.79	1 171 155 0.03	4 49 50 2.44	3 171 180 2.54	9 101 116 2.72	4 94 88 -0.82
13 116 114 2.21	16 63 60 -0.39	2 103 106 2.55	7 1 L	4 86 75 2.07	10 85 77 1.73	5 27 22 -2.45
14 61 53 -0.97	17 59 45 0.05	3 122 114 2.46	0 164 222 1.36	5 170 178 1.29	11 42 26 0.76	6 63 65 1.57
15 12 24 -0.20	18 38 44 2.40	4 70 57 -0.50	1 116 177 -1.02	6 125 125 -1.03	12 42 42 -1.47	7 25 22 -0.46
16 72 71 2.96	19 38 47 -2.78	5 96 68 3.08	2 70 98 -2.78	14 134 134 -0.58	13 35 38 -2.22	8 92 92 -0.59
17 65 70 0.48		6 74 59 -0.80	3 104 108 -0.42	8 82 74 2.48	14 58 66 2.04	9 45 51 2.52
18 86 98 0.61	6 10 L	7 63 68 -0.02	4 92 121 -1.03	9 115 120 -0.53	15 79 89 -0.49	10 62 71 2.45
19 55 48 -3.12	0 165 140 2.91	8 70 65 -0.78	5 132 147 1.93	10 49 35 -0.14	15 47 48 1.48	11 34 29 -2.75
20 65 65 3.01	1 97 88 -0.14	9 62 43 -3.68	6 36 32 1.54	11 114 105 1.57		
	2 100 100 1.54	10 120 120 -1.03	7 76 76 -1.03	7 11 L	7 17 L	
6 6 L	3 123 97 -0.63	11 116 113 2.95	8 90 95 -0.91	13 91 96 -1.59	0 83 59 -0.83	
0 137 129 2.87	4 0 28 2.94	12 50 58 0.62	9 154 156 2.71	14 66 66 1.38	1 102 79 1.85	1 22 37 2.27
1 103 191 1.28	5 188 180 -2.71	13 88 104 0.01	10 66 71 -2.89	15 80 91 2.40	2 108 93 -0.24	2 22 13 -1.40
2 74 78 0.78	6 136 116 2.26	14 47 59 2.61	11 125 133 1.67	16 43 57 2.43	3 57 57 1.05	3 82 76 -0.51
3 120 122 2.58	7 180 182 0.36	15 41 39 2.90	12 103 103 1.52	17 68 87 1.34	4 83 73 2.52	4 51 45 2.74
4 170 170 0.04	8 49 48 2.41	16 99 99 0.71	13 116 125 -1.76	18 29 47 -1.49	5 88 57 1.90	5 67 56 -1.90
5 91 91 -0.11	10 123 117 -0.23	6 16 L	14 83 96 -2.63	6 89 75 2.20	6 34 43 1.86	
6 104 100 -2.73	11 74 62 -3.09	0 103 97 -1.11	15 80 83 -0.44	7 92 82 1.65	7 49 59 1.27	
7 72 72 1.45	11 121 99 -1.97	1 121 99 -1.97				

Table 4. Bond distances and angles in  $K_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$ . The numbers in parentheses are the standard deviations of the last significant figures.

Distance (Å)	Distance (Å)
Mo(1) - O(1) - O(2) - O(1,2) - O(3) - O(4) - O(5) - O(6) - O(7)	1.96(4) 1.86(5) 1.91(10) 2.49(3) 1.64(3) 2.08(2) 1.97(2) 1.98(2) 1.38(6) 1.76(3) 2.33(2) 1.86(3) 1.93(2)
O(1) - Mo(1) - O(2) - O(3) - O(4)	42(2) 88(1) 95(1)
Mo(3) - O(5) - O(6) - O(8) - O(10) - O(11) - O(12)	2.20(2) 1.99(2) 2.34(3) 1.68(3) 1.91(3) 1.73(2)
Mo(4) - O(5) - O(7) - O(9) - O(13) - O(14) - O(15)	2.16(2) 1.99(3) 2.28(2) 1.66(3) 1.95(2) 1.75(4)
Angle (°)	Angle (°)
O(1) - Mo(1) - O(2) - O(3) - O(4)	73(1) 72(1) 92(1)
O(5) - Mo(3) - O(6) - (8) - O(10)	7 17 L 7 17 L 7 17 L

Table 4. Continued.

-O(5)	152(1)	-O(11)	87(1)
-O(6)	81(1)	-O(12)	156(1)
-O(7)	123(1)	O(6)-Mo(3)-O(8)	82(1)
O(2)-Mo(1)-O(3)	86(2)	-O(10)	99(1)
-O(4)	95(2)	-O(11)	151(1)
-O(5)	150(1)	-O(12)	90(1)
-O(6)	123(2)	O(8)-Mo(3)-O(10)	163(1)
-O(7)	81(2)	-O(11)	72(1)
O(3)-Mo(1)-O(4)	177(1)	-O(12)	90(1)
-O(5)	72(1)	O(10)-Mo(3)-O(11)	102(1)
-O(6)	81(1)	-O(12)	107(1)
-O(7)	80(1)	O(11)-Mo(3)-O(12)	102(1)
O(4)-Mo(1)-O(5)	106(1)	O(5)-Mo(4)-O(7)	73(1)
-O(6)	101(1)	-O(9)	72(1)
-O(7)	97(1)	-O(13)	95(1)
O(5)-Mo(1)-O(6)	76(1)	-O(14)	90(1)
-O(7)	76(1)	-O(15)	154(2)
O(6)-Mo(1)-O(7)	198(1)	O(7)-Mo(4)-O(9)	83(1)
O(3)-Mo(2)-O(3')	106(2)	-O(13)	101(1)
-O(5)	82(1)	-O(14)	154(1)
-O(5')	172(1)	-O(15)	90(2)
-O(8)	101(1)	O(9)-Mo(4)-O(13)	165(1)
-O(9)	102(1)	-O(14)	73(1)
O(5)-Mo(2)-O(5')	90(1)	O(9)-Mo(4)-O(15)	87(1)
-O(8)	78(1)	O(13)-Mo(4)-O(14)	100(1)
-O(9)	75(1)	-O(15)	107(2)
O(8)-Mo-O(9)	141(2)	O(14)-Mo(4)-O(15)	99(1)

for all molybdenum atoms. The refinement converged after about ten cycles to the parameters given in Table 2, the ultimate *R*-value being 0.097. Observed and calculated structure factors are given in Table 3. Calculated bond distances and angles with their standard deviations are given in Table 4 and some packing distances in Table 5. All bond distances were found to be within the normal range. The results obtained from the refinement were checked by calculating a three-dimensional electron density difference map. This showed only small residual maxima, the largest maximum having a magnitude of about 30 % of the height of an oxygen peak in the  $F_o$ -synthesis.

#### DESCRIPTION AND DISCUSSION

The crystal structure of  $K_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$ , illustrated in Fig. 2, consists of diperoxoheptamolybdate(VI) ions, potassium ions, and lattice water molecules. As can be seen from the packing distances in Table 5, there are some short distances between water oxygen atoms and other oxygen atoms indicating possible hydrogen bonds. In the structure determination no evidence for a ninth water molecule, as suggested by the chemical analysis, was found. There is, however, space enough for another water molecule and a possible explanation might be that the ninth water molecule is statistically distributed. There is no regular oxygen co-ordination around the potassium ions.

Table 5. Packing distances in  $K_6Mo_{22}(O_4)_2 \cdot 8H_2O$ . Distances less than 3.5 Å are included.  
The number in parentheses after the atom symbol denotes:

(1)	$x$	$y$	$z$	(5)	$\frac{1}{2} + x$	$\frac{1}{2} + y$	$z$
(2)	$1 + x$	$y$	$z$	(6)	$-\frac{1}{2} + x$	$\frac{1}{2} + y$	$z$
(3)	$\frac{1}{2} + x$	$\frac{1}{2} - y$	$z$	(7)	$-1 + x$	$y$	$z$
(4)	$-\frac{1}{2} + x$	$\frac{1}{2} - y$	$z$				

	Distance (Å)		Distance (Å)
$K(1)(1) - O(1)(2)$	2.67	$K(4)(1) - O(13)(1)$	2.84
$-O(2)(2)$	3.46	$-O(19)(4)$	2.81
$-O(10)(1)$	3.35	$-O(20)(1)$	2.80
$-O(18)(3)$	2.90	$O(16)(1) - O(8)(5)$	2.85
$-O(19)(4)$	2.74	$-O(12)(5)$	3.40
$K(2)(1) - O(9)(2)$	2.79	$-O(14)(1)$	3.16
$-O(12)(5)$	2.70	$-O(18)(1)$	3.31
$-O(15)(2)$	2.72	$O(17)(1) - O(3)(2)$	3.28
$-O(16)(1)$	2.92	$-O(11)(1)$	2.90
$-O(17)(1)$	3.27	$-O(14)(1)$	2.78
$-O(20)(1)$	2.90	$-O(20)(1)$	2.82
$K(3)(1) - O(1)(3)$	2.87	$O(18)(1) - O(1)(5)$	3.18
$-O(2)(3)$	3.28	$-O(3)(5)$	2.94
$-O(4)(3)$	2.97	$-O(6)(5)$	3.41
$-O(6)(5)$	2.82	$-O(10)(6)$	3.44
$-O(12)(5)$	3.15	$-O(15)(1)$	2.92
$-O(13)(1)$	2.96	$-O(19)(7)$	3.48
$-O(16)(1)$	2.93	$O(19)(1) - O(4)(3)$	3.02
$-O(18)(1)$	2.79	$-O(7)(2)$	3.41
$-O(20)(1)$	2.86	$-O(10)(3)$	3.22
$K(4)(1) - O(2)(2)$	2.89	$-O(12)(5)$	2.87
$-O(2)(3)$	3.36	$-O(15)(2)$	2.91
$-O(4)(1)$	3.35	$O(20)(1) - O(2)(2)$	3.39
$-O(4)(3)$	2.97	$-O(4)(3)$	3.27
$-O(7)(3)$	3.02	$-O(7)(2)$	2.69
$-O(10)(1)$	2.86	$-O(13)(1)$	3.28

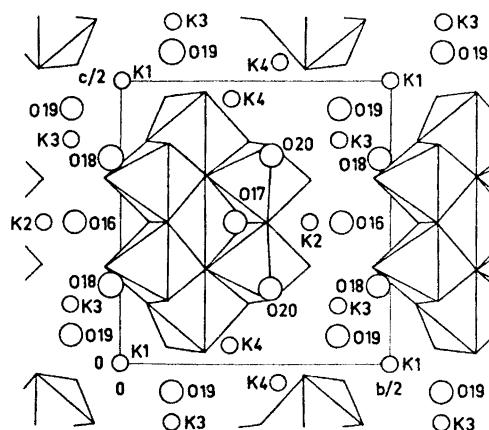
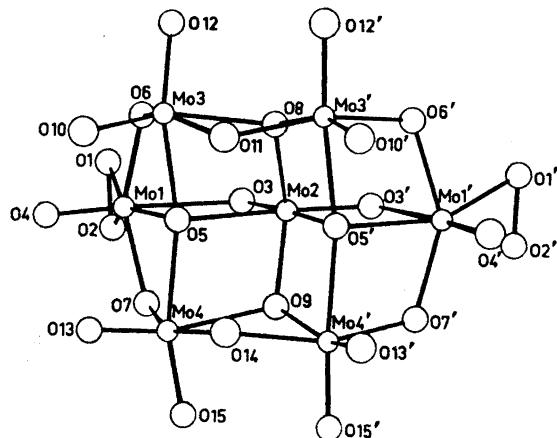


Fig. 2. The packing of the ions and water molecules in  $K_6Mo_{22}(O_4)_2 \cdot 8H_2O$  as viewed along the  $x$ -direction. The  $[Mo_7O_{22}(O_4)_2]^{6-}$  ion is shown schematically.

Fig. 3. The  $[\text{Mo}_7\text{O}_{22}(\text{O}_2)_2]^{6-}$  ion.

The  $[\text{Mo}_7\text{O}_{22}(\text{O}_2)_2]^{6-}$  complex ion is shown in Fig. 3. It is evident that the diperoxoheptamolybdate ion has the same general appearance as the normal heptamolybdate ion,<sup>10</sup> the difference being that two peroxy groups replace two oxygen atoms, one at either end of the heptamolybdate ion. The two molybdenum atoms coordinated to the peroxy groups are 7-coordinated by the pentagonal bipyramidal arrangement of ligand atoms frequently encountered in transition metal peroxy compounds. The structure of the diperoxoheptamolybdate ion can be described as being built up from five octahedra and two pentagonal bipyramids. As can be seen from Fig. 4, the atoms O(3) and O(4) are apically situated, while O(1), O(2), O(5), O(6), and O(7) form the equatorial plane. The two oxygen atoms O(1) and O(2) of the peroxy group are situated at 1.91 Å, on the average, from the central molybdenum atom. This implies that these Mo—O bonds are single bonds and their lengths agree well with Mo—O<sub>peroxy</sub> distances found in other 7-coordinated peroxomolybdates (see Table 6). The remaining three equatorial oxygen atoms are almost equally

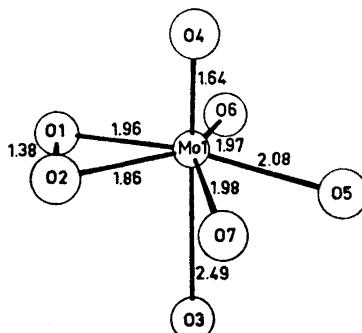
Fig. 4. The configuration about the 7-coordinated molybdenum atoms in the complex ion  $[\text{Mo}_6\text{O}_{22}(\text{O}_2)_2]^{6-}$ .

Table 6. Comparison between corresponding distances in  $K_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$  and other 7-coordinated peroxomolybdates.

Compound	Mo—O <sub>bridging</sub> (Å)	Mo—O <sub>peroxy</sub> (Å)	M=O (Å)	(O—O) <sub>peroxy</sub> (Å)	Mo—equatorial plane (Å)	Ref.
$K_2[O(MoO(O_2)_2(H_2O))_2] \cdot 2H_2O$	1.92—1.93	1.94—1.98	1.66	1.46—1.53	0.38—0.39	12
$(pyH)_2[O(MoO(O_2)_2(H_2O))_2]$	1.91	1.96—1.98	1.68	1.44—1.46	0.40	13, 14
$(pyH)_2[(O_2)_2OMo(OOH)_2MoO(O_2)_2]$	2.05—2.39	1.92—1.96	1.67	1.47—1.48	0.40	13, 14
$K_2[MoO(O_2)_2(C_2O_4)]$		1.93—1.96	1.68	1.44—1.47	0.35	15
$(NH_4)_3F[MoO(O_2)F_4]$		1.91	1.67	1.36	0.23	16
$K_2[MoO(O_2)F_4] \cdot H_2O$		1.94—1.95	1.64	1.44	0.18	17
$K_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$	1.97—2.49	1.86—1.96	1.64	1.38	0.31	This paper

Table 7. Comparison between corresponding distances in  $K_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$  and other heptamolybdates.

Defining atoms	Distances (Å) in				
	$(NH_4)_6Mo_7O_{24} \cdot 4H_2O$	$(NH_4)_6Mo_7O_{24} \cdot 4H_2O$	$K_6Mo_7O_{24} \cdot 4H_2O$	$K_6Mo_7O_{22}(O_2)_2 \cdot 8H_2O$	
Mo(1)—Mo(2)	3.43	{ 3.35 3.48	{ 3.45 3.40		3.40
Mo(1)—Mo(3)	3.21	{ 3.21, 3.35	{ 3.20, 3.26		3.21
Mo(1)—Mo(4)		{ 3.21, 3.27	{ 3.16, 3.19		3.22
Mo(2)—Mo(3)	3.41	{ 3.29, 3.39	{ 3.42, 3.44		3.47
Mo(2)—Mo(4)		{ 3.36, 3.45	{ 3.41, 3.38		3.47
Mo(3)—Mo(3')	3.26	{ 3.27	{ 3.25		3.30
Mo(4)—Mo(4')		{ 3.28	{ 3.24		3.31
Mo(1)—(O(1), O(2))	1.74				{ 1.96 1.86
Mo(1)—O(3)	2.42				2.49
Mo(1)—O(4)	1.72				1.64
Mo(1)—O(5)	2.16				2.08
Mo(1)—O(6)					{ 1.97
Mo(1)—O(7)	1.92				{ 1.98
Mo(2)—O(3)	1.75				1.76
Mo(2)—O(5)	2.26				2.33
Mo(2)—O(8)	1.90				{ 1.86
Mo(2)—O(9)					{ 1.93
Mo(3)—O(5)					{ 2.20
Mo(4)—O(5)	—				{ 2.16
Mo(3)—O(6)					{ 1.99
Mo(4)—O(7)	1.97				{ 1.99
Mo(3)—O(8)					{ 2.34
Mo(4)—O(9)	2.18				{ 2.28
Mo(3)—O(10)					{ 1.68
Mo(4)—O(13)	1.73				{ 1.66
Mo(3)—O(11)					{ 1.91
Mo(4)—O(14)	1.95				{ 1.95
Mo(3)—O(12)					{ 1.73
Mo(4)—O(15)	1.71				{ 1.75
Mo—O, distances: 1.51, 1.61—2.45, 2.62					
Ref.	22	10	23		This paper

remote from the central molybdenum atom ( $1.97 - 2.08 \text{ \AA}$ ). The Mo(1)–O(4) bond, which is  $1.64 \text{ \AA}$ , is significantly shorter, indicating considerable double bond character, while the Mo(1)–O(3) distance is significantly longer, *i.e.*  $2.49 \text{ \AA}$ , and is thus a rather weak bond. The observed  $(\text{O}-\text{O})_{\text{peroxo}}$  distance is rather short ( $1.38 \text{ \AA}$ ) compared with the value  $1.49 \text{ \AA}$  found in hydrogen peroxide and many metal peroxides (see Table 6 in Ref. 18). It cannot, however, be claimed to be significantly shorter since the e.s.d. is rather large, ( $0.06 \text{ \AA}$ ), but short  $(\text{O}-\text{O})_{\text{peroxo}}$  distances have been observed in several compounds, *e.g.*  $[\text{CrO}(\text{O}_2)_2\text{py}]$  ( $1.40 \text{ \AA}$ ),<sup>19</sup>  $[\text{CrO}(\text{O}_2)_2\text{phen}]$  ( $1.40 \text{ \AA}$ ),<sup>20</sup>  $[\text{CrO}(\text{O}_2)_2\text{dipy}]$  ( $1.40 \text{ \AA}$ ),<sup>21</sup> and  $(\text{NH}_4)_3\text{F}[\text{MoO}(\text{O}_2)\text{F}_4]$  ( $1.36 \text{ \AA}$ ).<sup>16</sup> Comparison between corresponding distances in  $\text{K}_6\text{Mo}_7\text{O}_{22}(\text{O}_2)_2 \cdot 8\text{H}_2\text{O}$  and other 7-coordinated peroxomolybdates is made in Table 6. The distances between atoms in the diperoxoheptamolybdate ion (except Mo–O<sub>peroxo</sub>) agree well with corresponding distances in the normal heptamolybdates (see Table 7).

Within the limits of experimental error all five equatorial atoms in the pentagonal bipyramid lie in a plane. The equation of this plane, **A**, as determined by the least-squares method, is

$$\mathbf{A}: \quad 0.6860 \text{ } X + 0.1967 \text{ } Y - 0.7005 \text{ } Z = -0.6122$$

where *X*, *Y*, and *Z* are the atomic coordinates expressed in  $\text{\AA}$ , referred to the original axes. The distances from certain atoms to the plane are:

<b>A</b> –O(1)	–0.01	$\text{\AA}$	<b>A</b> –O(7)	0.05	$\text{\AA}$
O(2)	–0.03		Mo(1)	0.31	
O(5)	–0.05		O(3)	–2.16	
O(6)	0.04		O(4)	1.94	

The molybdenum atom is thus displaced  $0.31 \text{ \AA}$  from the equatorial plane in the direction of the double-bonded oxygen atom, O(4). A similar displacement of the metal atom from the equatorial plane has been observed in a number of 7-coordinated transition metal oxoperoxo compounds. Some examples are cited in Table 6. The atoms Mo(1), Mo(1'), Mo(2), O(3), O(3'), O(4), O(4'), O(5), and O(5') all lie in a plane, the equation of which is

$$\mathbf{B}: \quad 0.2840 \text{ } X - 0.9588 \text{ } Y + 0.0063 \text{ } Z = -2.4218$$

The distances of the atoms defining plane **B** from the plane **B** are:

<b>B</b> –Mo(1)	0.00	$\text{\AA}$	<b>B</b> –O(4)	0.06	$\text{\AA}$
Mo(1')	–0.04		O(4')	0.00	
Mo(2)	–0.01		O(5)	0.00	
O(3)	0.02		O(5')	–0.02	
O(3')	0.00				

The distances of selected atoms from the plane **B** and the angle between the line connecting two opposite atoms and the plane **B** are given in Table 8. It can be noticed that the differences between corresponding distances are less than  $0.1 \text{ \AA}$  and the angles differ less than  $5^\circ$  from a right angle, which indicates

Table 8. Some distances of selected atoms from the plane **B** (see text) and the angle between the line  $X - Y$  and the plane **B**.  $X$  and  $Y$  denote atoms on opposite sides of the plane **B**.

Atom $X - Y$	Distance <b>B</b> — $X$ (Å)	Distance <b>B</b> — $Y$ (Å)	Angle (°)
Mo(3)—Mo(4)	2.14	2.08	88.8
O(1)—O(2)	0.68	0.69	85.2
O(6)—O(7)	1.90	1.91	90.0
O(8)—O(9)	1.78	1.79	87.3
O(10)—O(13)	1.90	1.89	88.7
O(11)—O(14)	1.84	1.80	87.7
O(12)—O(15)	3.84	3.79	89.0

that the plane **B** is approximately a mirror plane. The angle between the two mirror planes (the plane **B** and the plane with the equation  $Z = 4.9935$ ) in the complex ion is  $89.9^\circ$ . From the above evidence it can be concluded that the complex ion has approximately  $C_{2v}$  symmetry, which is the most probable symmetry of the free ion in solution. In most 7-coordinated peroxy complexes, e.g.  $(\text{NH}_4)_3\text{F}[\text{MoO(O}_2\text{)}_4\text{}]^{16}$ ,  $[\text{Cr(O}_2\text{)}_2(\text{NH}_3)_3]^{24}$ ,  $\text{K}_3[\text{Cr(O}_2\text{)}_2(\text{CN})_3]^{25}$  and  $[\text{CrO(O}_2\text{)}_2(\text{C}_{12}\text{H}_8\text{N}_2)]^{20}$  there is a mirror plane perpendicular to the equatorial plane. As the angle between the planes **A** and **B** is  $89.9^\circ$  this is the case here, too, within the limits of experimental error.

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#### REFERENCES

1. Baerwald, C. *Beiträge zur Kenntnis des Molybdäns*, Diss., Berlin 1885.
2. Hansson, A. and Lindqvist, I. *Acta Chem. Scand.* **3** (1949) 1430.
3. Sturdivant, J. H. *J. Am. Chem. Soc.* **59** (1937) 630.
4. Gagliotti, V. *Gazz. Chim. Ital.* **61** (1931) 257.
5. Stomberg, R. and Trysberg, L. *Acta Chem. Scand.* **23** (1969) 314.
6. Stomberg, R., Trysberg, L. and Larking, I. *Acta Chem. Scand.* **24** (1970) 2678.
7. Trysberg, L. *To be published*.
8. Modified by Lindqvist, O. and Lindgren, O. and in use at this department. POWDER was originally written by Lindqvist, O. and Wengelin, F., DATAP2 by Coppens, P., Leiserowitz, L. and Rabinowich, D., LALS by Gantzel, R., Sparks, K. and Trueblood, K., DRF and DISTAN by Zalkin, A., LINUS by Hamilton and Ibers, PLANEFIT by Wengelin, F. and ORTEP by Johnson, C.
9. Stomberg, R. *Acta Chem. Scand.* **22** (1968) 2024.
10. Lindqvist, I. *Arkiv Kemi* **2** (1950) 325.
11. Shima, E. *Bull. Chem. Soc. Japan* **40** (1967) 1609.
12. Stomberg, R. *Acta Chem. Scand.* **22** (1968) 1076.
13. Mitschler, A., Le Carpentier, J. M. and Weiss, R. *Chem. Commun.* **20** (1968) 1260.
14. Weiss, R., Carpentier, J. M., Mitschler, A. and Schlupp, R. *Acta Cryst. Suppl. A* **25** (1969) 171.
15. Stomberg, R. *Acta Chem. Scand.* **24** (1970) 2024.
16. Larking, I. and Stomberg, R. *Acta Chem. Scand.* **24** (1970) 2043.

17. Grandjean, D. and Weiss, R. *Bull. Soc. Chim. France* **8** (1967) 3044.
18. Stomberg, R. *Arkiv Kemi* **24** (1965) 283.
19. Stomberg, R. *Arkiv Kemi* **22** (1964) 29.
20. Stomberg, R. *Arkiv Kemi* **24** (1965) 111.
21. Stomberg, R. and Ainalem, I. B. *Acta Chem. Scand.* **22** (1968) 1439.
22. Evans, H. T., Jr. *J. Am. Chem. Soc.* **90** (1968) 3275.
23. Gatehouse, B. M. and Leverett, P. *Chem. Commun.* **15** (1968) 901.
24. Stomberg, R. *Arkiv Kemi* **22** (1964) 49.
25. Stomberg, R. *Arkiv Kemi* **23** (1965) 401.

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