

## The Crystal Structure of the Basic Mercury(II) Perchlorate $\text{Hg}_2\text{OOHClO}_4$

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The crystal structure of  $\text{Hg}_2\text{OOHClO}_4$  has been determined from three-dimensional X-ray data using visually estimated intensities from Weissenberg photographs. The unit cell is monoclinic with  $a = 11.078 \text{ \AA}$ ,  $b = 14.269 \text{ \AA}$ ,  $c = 7.224 \text{ \AA}$ , and  $\beta = 100.5^\circ$ . The space group is No. 14:  $P2_1/c$ . Each Hg atom forms two short Hg—O bonds with lengths of 2.0 Å and with the O—Hg—O angle close to  $180^\circ$ . Other Hg—O contacts are longer than about 2.7 Å. The structure can be described as built up from infinite one-dimensional complexes in which the Hg atoms are joined by the covalently bonded oxygens. The characteristic OHg<sub>3</sub> groups, previously found in several other structures, can be distinguished in these complexes.

In connection with an X-ray investigation of the structures of the polynuclear hydrolysis complexes of mercury(II) in aqueous perchlorate solutions,<sup>1</sup> it was found of interest to determine the structures of the basic salts that could be crystallized from such solutions. Of particular interest is the coordination of the mercury atom in the crystals and the type of bridging between the metal atoms in the polynuclear complexes. The structure of the basic perchlorate  $\text{Hg}_5\text{O}_2(\text{OH})_2(\text{ClO}_4)_4(\text{H}_2\text{O})_x$ , which is the least basic of those obtained, has been described in a previous paper.<sup>2</sup> The crystal structure of the most basic of the salts,  $\text{Hg}_2\text{OOHClO}_4$ , is given in the present paper, and an intermediate phase,  $\text{Hg}_7\text{O}_4(\text{OH})_2(\text{ClO}_4)_4$ , will be discussed in a following paper.

### EXPERIMENTAL

*Preparation of crystals.* Solutions obtained by dissolving an excess of HgO in  $\text{HClO}_4$  were used for the preparation of the crystals. Needlelike or rod-shaped crystals suitable for X-ray work crystallize spontaneously from a solution which is 3.1 M in  $\text{Hg}^{2+}$  and 4.8 M in  $\text{ClO}_4^-$ . The crystals are stable outside the mother liquor but decompose to HgO when washed with water.

*Analysis.* The crystals were separated from the mother liquor by centrifuging and were dried between filter papers. Dilute perchloric acid was used to dissolve the crystals before analysis.

Mercury was determined by reducing with  $H_3PO_3$  and precipitating and weighing as  $Hg_2Cl_2$ . Perchlorate was determined by passing a portion of a solution through a cation exchanger and titrating the eluate with  $NaOH$ , correcting for the amount of  $HClO_4$  used to dissolve the crystals. The density was calculated from the apparent loss of weight in benzene.

The results of the analysis are compared in Table 1 with values calculated for the stoichiometric composition  $4HgO \cdot Cl_2O_7 \cdot H_2O$ . A basic mercury(II) perchlorate, probably identical with the one described here, has been prepared previously by Hayek and Schnell.<sup>3</sup> They assumed the composition to be  $4HgO \cdot Cl_2O_7$ , and the results of their analysis are given in Table 1 for comparison.

Table 1. Analytical data.

Found	Calculated for $4HgO \cdot Cl_2O_7 \cdot H_2O$	Found by Hayek and Schnell <sup>3</sup>
% $HgO$	79.0	81.3
% $Cl_2O_7$	18.2	17.1
% $H_2O$	2.8 (diff.)	1.7
Density (g $cm^{-3}$ )	6.1 <sub>3</sub>	6.28

For a direct estimation of the number of non-perchlorate oxygens a Karl Fischer titration<sup>4</sup> was carried out. It can be expected that basic oxygens ( $O^{2-}$  and  $OH^-$ ) will react as water in this titration and the result will give the total number of oxygens not belonging to the perchlorate groups. Eight different titrations gave an average value of 0.9,<sub>4</sub> such oxygens per mercury atom. It will be shown in the following, that the crystal structure determination indicates that the correct formula is  $Hg_2OOHClO_4$ . This is consistent with the number of oxygens estimated from the Karl Fischer titration and corresponds to the stoichiometric composition  $4HgO \cdot Cl_2O_7 \cdot H_2O$ .

*Unit cell and space group.* Weissenberg photographs taken along two of the axes of the unit cell showed the symmetry to be monoclinic. More accurate values for the unit cell dimensions than those obtained from the Weissenberg photographs were determined by a least squares refinement using the line positions on a powder photograph taken in a Guinier camera.  $CuK\alpha$  radiation ( $\lambda = 1.5405 \text{ \AA}$ ) was used with  $KCl$  ( $a = 6.2929 \text{ \AA}$ ) as internal standard. Observed and calculated line positions for the first part of the powder photograph are given in Table 2. The unit cell dimensions were found to be:

$$a = 11.07_{\pm} \text{ \AA}, b = 14.26_{\pm} \text{ \AA}, c = 7.22_{\pm} \text{ \AA}, \beta = 100.5^\circ$$

The calculated density, assuming four formula weights  $4HgO \cdot Cl_2O_7 \cdot H_2O$  in the unit cell, is 6.28. The observed value is 6.1<sub>3</sub> (Table 1). Systematically absent reflections are  $h0l$  for  $l = 2n+1$  and  $0k0$  for  $k = 2n+1$ . This is consistent with the centrosymmetric space group No. 14,  $P2_1/c$ .

*Intensity data.* Intensity data were collected in a Weissenberg camera with the use of  $MoK\alpha$  radiation. Crystals with as far as possible cylindrical cross sections, with the largest dimension not exceeding 0.10 mm, were selected. Photographs were taken around the  $c$  axis ( $hk0 - hk8$ ) and the  $b$  axis ( $h0l - h4l$ ). Intensities were determined by visual comparison with an intensity scale prepared by timed exposures of one of the reflections of the same crystal. Intensities for about 2350 independent reflections were determined and were used for the structure determination. Lorentz and polarization factors were applied in the usual way and all intensities were recalculated to a common scale with the use of reflections appearing on more than one photograph.

*Computer programs.* The following programs were used to carry out the calculations:

DRF. Lp corrections, structure factor calculations and Fourier summations. Originally written by A. Zalkin, Berkeley, USA. Modified by R. Liminga and J.O. Lundgren, Uppsala, Sweden.

Table 2. Calculated and observed  $\sin^2\theta$  values for the first lines of a Guinier powder photograph of  $\text{Hg}_2\text{OOHClO}_4$ .

$hkl$	$(\sin^2\theta)_{\text{calc}}$	$(\sin^2\theta)_{\text{obs}}$	$I_{\text{obs}}$
110	0.00792	0.00789	vvw
020	0.01166	0.01165	vw
011	0.01467	0.01465	m
111	0.01680	0.01677	s
200	0.02000	0.01998	w
111	0.02255	0.02251	m
210	0.02292	0.02290	vvw
021	0.02341	0.02342	vw
121	0.03129	0.03126	w
220	0.03166	0.03163	w
221	0.03767	0.03766	m
031	0.03799	0.03796	vw
300	0.04501	0.04498	s
310	0.04792	0.04792	vw
221	0.04917}	0.04910	vvw
112	0.04920}		
012	0.04995	0.04999	m
140	0.05163	0.05163	s
231	0.05224	0.05221	vw
202	0.05554	0.05555	vvw
320	0.05666	0.05661	w
102	0.05778	0.05780	s
022	0.05869	0.05873	s
141	0.06051	0.06053	w
240	0.06663	0.06663	w
222	0.06719	0.06723	w
311	0.06830	0.06835	w
330	0.07123	0.07122	vvw
241	0.07264	0.07262	vvw
331	0.07437	0.07444	w
150	0.07785}	0.07781	vs
312	0.07771}		
400	0.08001	0.08013	vvw
232	0.08177	0.08179	m
411	0.08319	0.08299	vw
132	0.08401}	0.08416	s
241	0.08414}		
322	0.08645	0.08646	w
222	0.09019	0.09013	vvw
420	0.09167}	0.09170	vw
421	0.09193}		
250	0.09286	0.09279	vw
042	0.09366	0.09362	vvw
341	0.09477	0.09482	vvw
251	0.09887	0.09891	w
232	0.10476		
060	0.10491}	0.10489	vw
113	0.10512}		

LALS. Full matrix least squares refinement. Originally written by P. K. Gantzel, R. A. Sparks and K. N. Trueblood, Los Angeles, USA. Modified by A. Zalkin, Berkeley, USA, and by J.-O. Lundgren, R. Liminga and C. I. Brändén, Uppsala, Sweden.

DISTAN. Calculations of interatomic distances and bond angles. Written by A. Zalkin, Berkeley, USA, and modified by A. G. Nord and B. G. Brandt, Stockholm, Sweden.

### STRUCTURE DETERMINATION

The three-dimensional Patterson function showed that the 16 Hg atoms in the unit cell must occupy the general four-fold positions. Possible parameter values were deduced from the Harker sections. A systematic comparison of calculated Hg–Hg vectors with peaks in the three-dimensional Patterson function, sufficiently high to be identified as possible Hg–Hg vectors, led to an apparently unique set of parameter values for the four four-fold Hg positions in the unit cell.

A least squares refinement of the derived positions using all observed reflections gave an *R* factor of 0.20 and led to reasonable temperature factors for the four independent Hg atoms. On the basis of the derived parameter values a three-dimensional difference map was calculated from which the chlorine atoms and most of the oxygen atoms could be located. A new least squares refinement followed by a three-dimensional difference map led to the positions of the remaining oxygen atoms.

With all atoms included, a new least squares refinement using all observed reflections and with individual isotropic temperature factors for all atoms lowered the *R* factor to 0.16. The scattering factors used were those given by Cromer and Waber<sup>5</sup> for the neutral atoms. Corrections were made for the real part of the anomalous dispersion according to Cromer.<sup>6</sup> The weighting scheme was that suggested by Hughes.<sup>7</sup> A further least squares refinement

*Table 3.* Final parameters for  $\text{Hg}_2\text{OOHClO}_4$ . All atoms are in position 4(e) in space group No. 14;  $P2_1/c$ . Standard deviations are given within brackets.

Atom	<i>x</i>	<i>y</i>	<i>z</i>	<i>B</i>
Hg <sub>1</sub>	0.3207 (2)	0.2484 (1)	0.9784 (2)	1.1 (0)
Hg <sub>2</sub>	0.2649 (2)	0.0487 (1)	0.2020 (2)	1.2 (0)
Hg <sub>3</sub>	0.6744 (2)	0.1842 (1)	0.9093 (2)	1.5 (0)
Hg <sub>4</sub>	0.9654 (2)	0.1114 (1)	0.8376 (2)	1.5 (0)
Cl <sub>1</sub>	0.9604 (10)	0.1384 (8)	0.3462 (15)	1.7 (2)
O <sub>1</sub>	0.0179 (54)	0.0951 (44)	0.2192 (83)	4.5 (14)
O <sub>2</sub>	0.8802 (44)	0.1973 (38)	0.2621 (68)	2.7 (8)
O <sub>3</sub>	0.8921 (47)	0.0891 (40)	0.4314 (73)	4.1 (12)
O <sub>4</sub>	0.0495 (49)	0.1865 (40)	0.4756 (73)	3.1 (10)
Cl <sub>2</sub>	0.3999 (11)	0.4777 (9)	0.2354 (15)	1.8 (2)
O <sub>5</sub>	0.3056 (36)	0.4359 (30)	0.1011 (53)	1.6 (7)
O <sub>6</sub>	0.5195 (63)	0.4575 (53)	0.2045 (97)	4.5 (15)
O <sub>7</sub>	0.6071 (56)	0.0779 (50)	0.2629 (84)	4.5 (15)
O <sub>8</sub>	0.4032 (74)	0.4336 (63)	0.4399 (114)	5.8 (19)
O <sub>9</sub>	0.7805 (27)	0.4141 (22)	0.3069 (39)	1.9 (6)
O <sub>10</sub>	0.3341 (30)	0.1834 (23)	0.2254 (43)	1.7 (6)
O <sub>11</sub>	0.5754 (37)	0.2685 (30)	0.0350 (54)	3.1 (10)
O <sub>12</sub>	0.1422 (36)	0.3822 (29)	0.3815 (54)	2.9 (9)

Table 4. Observed and calculated structure factors.

0 k 0	5 k 0	14	74	-74	13	180	-184	14	61	-59	3	61	-76	16	99	-95	
0 1800	0 254 -255	15	< 52	10	14	85	80	12	< 41	-23	6	100	-100	17	< 58	22	
2 125 -119	1 62 93	16	132	102	15	51	-50	16	109	-123	6	211	278	18	< 50	-29	
4 98 -31	2 199 241	17	< 55	38	16	< 12	9	17	104	108	6	76	75	19	149	174	
6 288 -259	3 52 -34	18	15	-115	17	121	142	18	52	46	7	< 50	-40	1	119	-144	
8 73 -21	4 229 -247	10	k 0	18	127	134	19	< 48	-26	8	< 34	-7	1	119	-144		
10 19 -131	5 53 -75	0	100	-95	19	< 45	33	20	143	-177	2	49	57				
12 < 40 -18	6 < 32 17	11	112	107	20	< 49	41	21	114	142	5	35	36	4	< 77	36	
14 378 -433	7 442 -524	2	57	-50	21	57	66			11	37	36	4	167	198		
16 265 -284	8 127 133	3	189	203	1	k 1	1	90	-62	12	< 39	26	5	67	56		
18 < 50 + 11	9 165 174	4	88	95	1	42	-253	2	100	-117	14	106	-133	7	< 38	21	
20 136 -157	10 170 189	5	98	-92	2	252	200	3	355	-392	15	< 44	-21	8	< 39	1	
22 11	55 42	6	< 13	8	3	112	85	5	< 27	-30	17	< 47	-28	10	< 39	7	
0 < 12 9	12 92	7	183	157	4	150	-105	5	< 27	-30	18	< 54	-28	11	142	135	
1 60 -5	13 127 125	8	< 45	19	5	295	-257	6	66	71	18	< 44	-28	11	142	135	
2 191 -139	14 125 145	9	143	-117	6	197	-175	7	63	46	19	89	-107	12	< 45	28	
3 < 14 -10	15 147 -161	10	< 47	3	7	179	179	8	150	107	10	39	-17	5	68	64	
4 473 -499	17 < 50 53	11	110	88	9	366	343	10	63	54	1	41	40	14	< 46	37	
5 625 -597	18 < 82 89	13	< 51	53	10	74	-44	11	251	264	2	116	-109	15	< 47	51	
6 87 -74	19 < 54 18	14	< 52	29	11	< 33	12	175	-167	3	338	-330	16	< 49	61		
7 150 -109	20 < 85 15	15	119	-57	12	236	-227	13	89	96	4	44	-17	17	< 49	29	
8 189 -157	21 < 81 104	16	< 55	-10	13	163	152	14	< 39	-17	5	68	-64	18	< 52	12	
9 422 -416	22 < 60 51	17	113	-78	14	14	179	9	201	-195	19	129	-142	10	167	190	
10 167 -190	23 < 109 -132	18			15	< 40	-14	15	< 42	-13	7	< 31	19				
11 227 -239	19 < 110 110	19			16	< 40	-14	15	< 42	-13	7	< 31	19				
12 139 -160	20 < 247 -215	20			16	< 40	-14	15	< 42	-13	7	< 31	19				
13 49 -57	21 184 209	22	1	54	18	< 45	40	19	85	-90	11	211	211	3	61	54	
14 142 -142	23 157 159	24	221	181	20	< 45	40	19	85	-90	11	211	211	3	61	54	
15 127 -134	24 < 348 -422	3	115	100	19	< 47	13	21	140	-161	1	102	-150	12	< 38	22	
16 77 -77	3 165 208	4	< 44	28	26	16	75	54	1	102	-150	13	79	-84	5	< 35	8
17 72 -50	4 < 32 6	5	< 44	41	21	140	-161	1	102	-150	14	133	130	6	244	-207	
18 126 -135	5 < 67 6	6	< 44	15	15	-1 k 1	3	149	174	15	48	-52	7	< 37	15		
19 132 -136	6 < 34 7	7	107	107	2	< 14	310	4	212	-257	16	43	55	8	180	-159	
20 < 154 -144	7 200 -227	8	129	-106	2	< 14	5	5	101	-112	7	86	90	9	< 39	13	
21 124 -138	8 111 108	9	< 48	49	79	5	16	194	216	18	< 48	-4	10	145	126		
22 57 -50	9 125 145	10	109	-74	4	421	-365	7	< 29	17	19	79	-69	11	< 41	21	
23 59 -70	10 90 94	11	< 50	16	16	124	-127	9	226	-225	12	43	47				
24 61 -27	12 117 127	13	117	-30	6	126	-127	9	45	-44	7	30	38	13	115	-101	
25 133 -161	12 209 203	13	< 53	10	7	157	157	10	46	-46	1	< 30	38	14	114	-104	
26 148 -148	14 155 -236	15	< 55	-49	9	68	-48	12	243	267	3	162	212	15	< 48	19	
0 218 -236	15 125 -147	16	102	94	10	258	-224	13	162	146	4	91	-123	16	89	76	
1 101 -102	17 110 -101	18	70	84	73	12	115	115	101	-101	15	6	< 33	44	18	< 51	9
2 49 -56	18 197 -235	19	< 55	-23	13	153	-153	10	204	-204	8	48	-50	9	95	87	
3 337 -302	20 57 -57	20	0	71	55	14	< 37	11	17	48	-74	10	175	-163	10	1 k 1	
4 67 -27	21 82 84	21	< 47	16	12	53	50	6	< 27	4	9	81	103	10	64	-48	
5 377 -328	22 122 312	23	5	64	-55	18	103	104	-4 k 1	326	326	13	63	73	4	< 38	3
6 91 -299	24 0 90	25	106	181	19	134	134	1	327	326	15	57	-39	5	58	55	
7 317 -332	26 1 114	27	130	5	30	< 45	30	207	-109	2	255	240	14	57	-39	55	
8 117 -87	27 2 80 102	28	126	113	8	154	-150	11	120	-122	15	48	-52	7	< 47	31	
9 126 -66	28 3 329 359	29	7	200	-171	1	65	-83	5	117	108	4	91	-123	16	89	76
10 135 -65	30 4 41 45	31	8	117	-103	2	104	-83	6	117	108	5	46	-52	7	< 40	15
11 119 -119	32 5 157 -63	33	9	90	72	3	26	-76	6	356	298	18	74	67	9	91	-100
12 149 -148	34 6 260 240	35	11	< 52	4	5	58	-51	9	80	78	19	91	71	10	57	-52
13 77 -48	36 8 47 -16	37	12	53	70	5	< 27	4	9	129	-115	1	80	91	12	50	37
14 79 -79	38 9 134 -127	39	13	77	70	7	28	-28	15	12	85	3	194	-172	14	80	-79
15 82 -65	40 10 88 -88	41	8	20	7	28	-28	15	12	85	7	339	274	14	80	-79	
16 80 -64	42 11 159 -159	43	9	156	156	4	< 50	22	10	103	-103	11	121	-127	10	57	-52
17 80 -64	44 12 155 -155	45	10	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
18 79 -79	46 13 155 -155	47	11	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
19 62 -62	48 14 155 -155	49	12	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
20 77 -77	50 15 155 -155	51	13	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
21 75 -68	52 16 155 -155	53	14	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
22 75 -68	54 17 155 -155	55	15	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
23 75 -68	56 18 155 -155	57	16	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
24 75 -68	58 19 155 -155	59	17	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
25 75 -68	60 20 155 -155	61	18	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
26 75 -68	62 21 155 -155	63	19	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
27 75 -68	64 22 155 -155	65	20	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
28 75 -68	66 23 155 -155	67	21	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
29 75 -68	68 24 155 -155	69	22	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
30 75 -68	70 25 155 -155	71	23	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
31 75 -68	72 26 155 -155	73	24	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
32 75 -68	74 27 155 -155	75	25	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
33 75 -68	76 28 155 -155	77	26	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
34 75 -68	78 29 155 -155	79	27	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
35 75 -68	80 30 155 -155	81	28	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
36 75 -68	82 31 155 -155	83	29	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
37 75 -68	84 32 155 -155	85	30	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
38 75 -68	86 33 155 -155	87	31	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
39 75 -68	88 34 155 -155	89	32	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
40 75 -68	90 35 155 -155	91	33	156	156	5	< 50	22	10	103	-103	11	121	-127	10	57	-52
41 75 -68	92 36 155 -155	93	34	156	156	5	< 50	22	10</								

Table 4. Continued.

16	113	-109	3	106	193	10	< 90	76	6	< 97	36	7	71	-60	12	127	-153	14	< 134	-121	
12	k 1	4	85	60	11	< 94	-105	7	156	130	8	146	158	13	164	194	15	< 77	12		
1	83	-82	5	244	250	12	< 98	-30	8	< 101	-80	9	198	-196	14	< 71	-33	16	138	-187	
2	70	-61	6	290	282	13	114	-121	9	< 102	26	10	94	84	15	< 74	23	16	77	12	
3	73	-91	7	340	360	10	< 105	-26	11	210	207	11	207	-202	16	< 77	12	12	127	-111	
4	64	-65	8	520	-504	0	< 5	k 2	11	127	-139	13	146	146	14	< 8	k 3	1	127	-111	
9	9	-25	10	< 82	42	1	137	-121	-9	k 2	14	68	69	-4	k 3	2	87	-84	87	-84	
7	44	-5	11	86	-83	2	388	359	1	346	391	15	< 71	45	1	242	3	88	-97		
8	< 45	-2	12	169	-166	3	320	287	2	346	375	16	< 74	33	2	147	4	114	134		
9	73	-58	4	< 2	k 2	5	227	-284	3	< 86	34	17	< 77	-1	3	321	5	62	51		
10	< 47	4	0	210	-182	6	122	-104	4	< 88	36	4	18	-108	5	296	238	7	< 5	12	
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-12	k 1	2	413	345	8	< 79	27	6	165	-165	-11	-1	k 3	7	76	-60	9	< 68	-22		
1	114	116	3	602	545	9	110	-115	7	155	153	1	193	-248	8	80	-63	10	< 71	0	
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3	< 41	20	6	202	-151	11	215	-215	9	149	-134	3	168	-174	10	133	126	5	62	51	
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5	42	40	8	71	-21	6	12	-104	5	110	-110	50	6	65	-55	12	77	51	1	112	-128
-12	k 1	1	2	413	345	9	76	-46	0	164	185	13	< 112	14	14	< 69	-32	2	< 25	8	
6	150	-99	10	204	-145	1	165	182	14	142	-170	8	195	-142	15	72	72	4	140	154	
7	< 43	33	11	345	286	3	170	-188	-10	k 2	10	123	103	16	125	-110	5	57	-57		
8	78	-65	12	202	-177	271	342	0	< 40	-38	10	195	184	5	k 3	6	164	-186			
9	101	80	13	210	-190	1	118	150	1	147	127	2	103	128	7	35	35	83			
10	116	88	14	160	138	5	< 81	5	2	52	61	13	70	57	3	131	-153	9	148	170	
11	46	47	15	< 103	-37	7	84	56	3	56	14	151	135	4	48	27	10	145	138		
12	< 47	10	16	-141	8	193	-218	4	93	154	15	111	94	5	12	161	11	92	86		
13	69	-58	17	216	-225	18	117	126	9	< 90	33	6	< 112	16	5	83	78	9	k 3	3	
14	13	k 1	19	149	115	10	206	-247	7	142	149	18	180	-80	4	86	-86	2	< 63	9	
1	47	45	3	k 2	0	-6	k 2	8	< 106	18	19	166	-169	9	188	-248	3	< 64	28		
3	< 44	56	0	168	161	4	362	453	10	176	-176	2	111	123	11	< 65	-10	4	108	-31	
4	< 44	-28	1	250	244	2	93	-78	5	216	209	-10	k 2	3	210	-219	12	151	-193		
5	45	26	2	224	-248	3	252	-259	0	174	228	3	< 50	5	150	-152	2	92	-76		
6	106	103	3	232	-259	5	174	-24	2	52	50	1	91	62	4	147	7	155	149		
7	< 46	21	4	355	401	4	58	50	1	174	228	5	261	269	1	137	-150	9	< 72	-60	
8	74	75	5	164	-188	7	169	-195	3	< 92	20	6	150	-152	2	92	-76	10	91	-84	
9	< 47	14	6	< 67	-51	6	199	-195	3	137	147	7	75	-73	3	130	113	-k 3	1	127	10
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1	42	6	12	178	171	13	< 98	32	9	147	146	12	63	-56	8	279	-249	5	94	-100	
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3	63	64	14	< 101	-35	15	179	123	2	111	-111	14	123	-125	12	125	123	6	130	-123	
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5	28	48	17	181	194	7	k 2	2	2	43	42	16	130	131	12	65	71	11	10	-69	
6	13	-16	18	205	-257	3	116	-55	4	48	1	< 23	-35	14	104	107	11	121	214		
7	< 45	-16	3	146	136	1	161	-186	2	149	-116	5	149	-116	6	k 3	12	174	214		
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3	< 42	6	126	-86	10	151	-151	6	74	146	15	10	125	-205	8	< 61	29	1	180	196	
4	300	207	10	< 149	141	11	101	-77	8	< 106	140	11	125	-270	9	92	-86	2	96	108	
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9	147	-113	16	262	-299	18	0	< 105	18	1	267	-287	14	75	77	7	77	7	77	-63	
10	79	-61	17	< 113	-37	1	134	132	2	112	-112	3	103	-102	16	12	112	10	112	103	
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12	< 205	37	0	118	106	2	150	-225	9	< 51	27	11	176	-144	10	64	58	2	86	69	
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14	267	-207	2	137	-99	0	130	-157	4	115	-103	6	259	223	6	< 60	32	12	k 3		
15	< 103	-47	3	207	-177	1	141	-152	5	175	169	7	65	-43	1	127	-157	2	48	46	
16	224	-233	5	< 84	0	281	35	7	128	120	9	129	-134	8	64	58	2	86	69		
0	136	-142	6	694	-567	4	258	-260	8	< 48	44	10	87	-67	9	132	137	3	< 70	-31	
1	151	-197	8	93	-79	6	86	27	10	164	-133	12	135	130	11	128	120	3	114	-128	
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3	< 43	15	10	303	263	6	140	-141	16	147	180	13	130	139	13	130	139	3	114	-127	
4	< 48	-33	11	< 88	16	9	< 95	-96	13	239	225	15	< 74	4	< 74	32	8	< 76	-32		
5	< 52	12	12	< 92	-17	10	98	116	14	< 147	16	217	-220	1	< 49	31	9	134	152		
6																					

Table 4. Continued.

0 $\times$ 4	11	198	-211	0	6 $\times$ 4	8	106	78	7	70	67	13	116	112	10	77	75		
0	56	56	11	151	158	0	< 51	13	8	< 72	-	8	114	151	152	11	53	- 58	
1	10	193	13	< 66	67	1	102	104	10	< 72	-	11	14	15	15	12	- 52		
2	50	- 45	14	< 69	- 16	2	97	- 103	11	< 76	-	45	10	61	- 61	16	- 76		
3	119	- 132	15	135	- 152	3	286	- 343	12	< 78	-	36	9	< 40	- 3	12	- 52		
4	350	372	16	< 75	6	4	13	75	13	123	135	12	235	- 226	- 7 k 5	- 48			
5	297	274	17	< 78	94	5	< 55	16	- 9	k 4	13	< 47	- 16	1	205	213			
6	213	- 199	18	< 81	- 92	6	103	- 145	0	156	- 175	14	75	57	3	65	- 48		
7	379	333	19	94	- 118	7	< 79	20	2	86	- 90	16	< 52	- 49	4	35	- 241		
8	129	111	- 3 k 4	-	-	8	< 59	28	2	143	- 174	16	86	63	5	35	- 158		
9	< 51	- 35	-	-	-	9	< 63	- 40	2	120	- 124	17	< 56	- 25	6	35	- 38		
10	309	- 280	0	56	37	10	< 65	49	4	135	147	18	< 58	- 49	7	63	- 24		
11	210	- 184	1	139	146	11	121	- 136	5	155	- 160	19	149	155	8	41	- 246		
12	129	- 115	2	46	43	12	70	90	6	143	- 145	20	89	- 79	9	43	- 105		
13	< 4	- 46	3	170	- 151	15	135	153	7	91	- 81	1	15	45	10	45	- 125		
14	< 67	- 35	4	421	425	14	< 55	- 25	8	231	235	1	78	89	11	48	- 96		
15	176	- 190	5	< 39	1	5	< 77	44	9	81	- 87	2	200	- 143	12	98	- 102		
16	< 73	75	6	318	- 261	16	< 80	12	10	94	- 98	3	35	- 45	13	115	- 125		
17	< 75	75	7	137	- 132	17	143	155	11	103	- 83	4	46	- 41	14	51	- 54		
18	88	- 83	8	< 59	28	12	170	170	5	45	- 55	15	62	- 55	16	< 55	- 42		
19	111	- 109	9	< 52	- 29	- 6 k 4	-	-	10	493	- 433	6	189	- 186	17	< 59	- 12		
20	11	77	11	77	- 53	1	128	131	0	51	- 40	7	< 34	- 7	17	98	95		
21	1 k 4	-	11	77	- 53	2	123	- 115	9	< 101	-	55	29	10	88	- 50	115		
22	43	- 27	12	95	- 77	3	110	- 102	2	< 68	- 48	9	98	- 101	1	151	- 144		
23	108	- 502	13	128	- 112	4	137	133	2	143	- 155	1	193	- 195	3	65	- 53		
24	33	35	3	170	- 151	5	60	269	221	4	< 69	- 50	11	44	- 51	2	25	- 212	
25	148	151	6	< 73	35	6	231	- 193	5	< 70	- 35	12	111	- 119	4	46	- 11		
26	99	- 114	7	171	- 121	105	77	140	6	78	- 95	13	48	- 41	4	148	- 63		
27	100	- 95	16	< 79	58	8	104	- 82	8	181	208	15	< 52	- 30	5	166	- 136		
28	114	- 121	20	142	- 175	10	345	- 304	10	205	211	7	86	- 77	9	< 51	- 43		
29	128	- 116	11	92	73	- 10 k 4	-	-	11	92	- 91	1	118	- 92	1	39	- 30		
30	201	- 191	4	1 k 4	-	12	155	157	0	69	- 69	1	15	- 51	2	61	- 71		
31	< 56	2	0	55	85	13	145	137	1	133	220	1	87	67	9	315	- 243		
32	72	- 69	1	347	- 394	14	< 35	- 25	2	49	34	2	< 27	21	10	193	- 159		
33	204	- 192	2	67	71	15	< 74	18	3	89	- 99	3	105	- 124	12	46	- 50		
34	< 67	17	3	143	137	16	< 77	23	4	< 62	- 24	4	38	- 38	12	46	- 50		
35	351	322	4	146	16	17	126	106	5	63	- 67	5	63	56	13	118	- 92		
36	< 73	- 11	6	129	143	18	91	- 95	6	109	- 108	5	571	358	1	39	- 30		
37	101	- 93	7	211	- 221	7	140	- 147	8	140	- 147	9	82	227	10	193	- 159		
38	73	- 76	8	< 55	65	0	55	29	9	< 69	- 28	9	38	- 40	17	57	- 25		
39	< 82	81	9	< 57	6	1	193	- 214	10	< 71	- 13	10	162	- 157	18	59	- 45		
40	99	- 101	10	142	- 134	25	61	- 11	73	- 76	26	11	151	- 104	20	110	- 115		
41	510	- 439	11	< 63	- 60	3	150	- 156	12	< 75	- 76	11	114	- 112	11	41	- 45		
42	84	- 84	13	229	- 233	5	89	- 95	14	< 80	- 89	14	140	- 134	5	213	- 205		
43	133	- 161	14	< 71	- 72	4	142	105	12	< 125	- 125	10	151	- 140	10	50	- 45		
44	216	- 232	15	133	162	7	125	151	16	< 130	- 130	15	151	- 145	11	49	- 47		
45	4	121	- 114	8	184	224	0	54	66	17	< 56	31	3	171	- 187	12	99	- 107	
46	247	- 240	- 4 k 4	-	-	10	68	21	3	115	90	19	58	- 16	3	39	- 15		
47	6	421	389	0	178	- 184	10	66	21	4	121	- 140	20	117	- 124	6	41	- 47	
48	117	- 89	1	311	290	11	< 70	72	32	< 74	- 74	45	20	117	17	43	- 47		
49	391	- 302	2	< 34	25	12	< 72	72	32	< 74	- 74	45	20	117	17	43	- 47		
50	83	70	3	< 57	- 58	13	124	- 143	7	< 76	- 76	29	1	61	- 67	8	44		
51	365	291	4	121	- 121	11	< 74	74	21	< 77	- 77	34	1	61	- 67	10	47		
52	11	- 154	5	324	267	8	< 74	74	21	< 77	- 77	34	2	31	- 26	10	47		
53	103	- 92	6	340	276	0	73	67	9	< 76	79	3	256	- 275	11	148	- 171		
54	13	63	7	78	70	1	129	166	10	86	112	4	95	- 91	1	50	- 50		
55	8	480	375	1	256	306	10	68	112	5	< 11	12	12	12	11	49	- 49		
56	145	- 67	9	151	121	3	63	- 41	1	64	- 61	6	164	- 165	15	52	- 52		
57	133	126	10	118	146	4	128	117	1	94	- 105	8	64	- 65	15	54	- 54		
58	< 72	- 35	11	171	- 139	5	94	76	3	217	235	8	84	- 91	10	100	- 100		
59	< 77	- 55	12	62	- 62	6	226	185	4	< 66	- 66	9	140	- 142	10	56	- 54		
60	108	- 102	13	65	4	7	124	- 118	5	< 67	- 67	10	98	- 99	1	55	- 55		
61	170	- 181	14	66	77	8	42	- 47	5	< 68	- 68	11	232	- 240	2	121	- 122		
62	< 80	- 9	15	226	- 244	10	83	- 74	7	< 80	- 80	13	75	- 75	11	46	- 46		
63	101	- 89	17	77	- 77	11	< 65	65	5	140	- 139	15	73	- 73	10	48	- 38		
64	171	- 182	18	210	- 217	1	56	- 47	1	113	133	8	126	- 126	10	< 50	- 5		
65	< 42	- 4	0	217	217	3	61	11	- 12 k 4	-	9	145	- 129	11	51	- 45			
66	313	314	1	150	- 140	2	132	- 133	1	112	- 112	8	145	- 139	10	45	- 45		
67	< 48	- 4	2	166	167	3	< 61	11	- 12 k 4	-	10	90	- 75	1	39	- 29			
68	264	- 267	3	189	- 228	4	143	- 154	1	68	- 55	11	188	- 153	2	86	- 95		
69	283	269	4	162	- 173	9	63	63	2	150	159	3	204	- 180	3	40	- 39		
70	97	- 97	5	< 52	- 52	10	64	104	3	134	165	12	194	- 180	4	41	- 39		
71	< 62	- 21	7	26	- 27	8	135	- 151	5	< 70	- 70	13	82	- 82	5	150	- 158		
72	101	124	8	211	- 249	9	< 69	4	6	105	- 113	15	51	- 52	6	65	- 64		
73	< 68	63	9	< 60	- 28	10	71	87	7	< 73	- 73	16	176	- 156	7	71	- 70		
74	133	127	10	113	129	12	< 73	46	8	166	190	17	63	- 40	8	46	- 26		
75	< 74	11	11	< 65	79	12	< 75	45	6	< 76	- 76	16	16	- 85	9	175	- 201		
76	86	- 66	14	246	246	14	60	11	89	64	8	96	- 108	10	42	- 35	3	51	- 24
77	8	113	- 91	3	259	258	7	< 59	4	7	121	- 112	9	113	116	9	106	- 86	
78	9	192	- 137	4	101	105	8	135	- 121	1	114	- 114	10	86	- 86	2	44	- 39	
79	104	- 175	13	182	- 181	17	185	- 201	2	130	159	3	106	- 105	11	45	- 45		
80	261	- 256	14	< 72	- 32	- 8 k 4	-	-	1	14	- 14	4	143	149	1	134	- 141		
81	< 25	30	16	< 78	0	207	- 237	- 13 k 4	1	130	159	3	105	- 120	1	258	- 272		
82	57	68	17	91	94	2	114	125	2	70	- 63	11	106	- 105	2	160	- 145		
83	202	- 170	0	441	- 446	4	< 54	5	4	133	165	12	97	119	3	99	- 75		
84																			

Table 4. Continued.

3	< 47	26	8	68	54	-5 k 6	8	253	-229	1	< 51	37	3	< 24	-29	2	< 35	27				
4	< 48	30	9	57	- 50	0	210	6	9	118	- 127	2	< 51	- 52	4	180	- 183					
5	123	126	10	171	148	1	290	-304	10	< 48	- 15	3	< 51	- 49	5	150	- 140					
6	108	- 119	11	82	62	2	37	29	11	< 50	- 21	4	< 52	- 5	6	32	3					
7	51	- 54	12	< 45	20	3	139	130	12	77	- 72	5	< 52	- 37	7	84	70					
8	62	- 75	14	20	- 55	4	49	- 59	13	59	- 59	6	101	122	8	46	53					
9	138	- 160	12	116	116	5	131	121	14	61	- 45	7	< 58	- 59	8	79	75					
10	< 53	- 55	15	118	106	6	46	33	15	187	198	8	< 55	- 91	10	122	116					
11	101	- 109	7	155	- 171	9	77	74	8	123	- 128	3	< 24	- 21	10	45	37					
12	k 5	- 35	16	103	82	7	310	276	9	< 6	- 60	9	< 60	- 24	11	45	37					
13	70	- 68	17	190	- 177	8	208	-180	10	69	86	12	95	- 103	11	68	63					
14	125	133	3	k 6	- 177	9	120	- 91	1	121	129	0	x 7	- 13	< 49	7	8 k 7					
15	98	116	0	215	196	10	< 41	1	2	< 49	8	1	< 61	- 80	14	< 52	- 11					
16	51	8	1	156	141	11	< 41	10	3	< 50	32	2	< 22	- 20	15	< 54	- 42					
17	52	22	2	186	110	12	87	- 78	4	< 50	55	3	< 25	- 7	20	79	- 74					
18	54	10	4	< 34	5	13	229	- 220	8	< 51	55	4	< 44	- 40	4	4 k 7	2					
19	55	41	5	93	97	14	113	- 105	6	< 51	20	5	129	- 130	1	88	- 78					
20	57	45	6	215	- 230	16	74	69	8	< 86	88	7	85	- 75	2	52	- 54					
21	101	- 109	7	155	- 171	17	131	- 130	9	77	74	8	123	- 128	3	53	40					
22	-13 k 5	8	140	158	- 6	6	104	- 137	0	39	14	0	x 41	33	10	103	- 9					
23	97	- 102	10	146	- 132	1	193	191	1	266	- 86	33	11	39	38	6	97	- 95				
24	0	k 6	11	< 47	- 56	2	65	68	2	< 41	17	12	< 48	2	20	16	2	82	74			
25	118	142	13	99	95	4	< 41	4	3	< 41	15	13	< 50	44	8	< 67	10					
26	18	9	5	64	64	5	143	147	4	< 213	209	14	69	78	9	156	133					
27	3	5	99	- 88	6	105	- 104	5	207	185	1	1 k 7	11	136	127	13	87	- 84				
28	189	- 241	15	< 57	8	7	86	- 86	6	212	- 175	9	197	202	4	64	65					
29	27	- 27	17	< 59	46	8	115	124	7	92	92	2	119	132	1	89	- 80					
30	29	3	18	83	80	9	128	136	9	85	- 97	4	168	175	2	111	- 112					
31	257	- 281	19	< 65	- 27	10	79	- 50	28	10	176	- 198	5	125	- 177	3	158	- 142				
32	250	- 277	11	117	126	11	< 51	51	11	104	- 101	6	64	55	49	4	87	78				
33	74	54	0	< 21	- 25	13	< 53	41	0	< 9 k 6	7	37	- 4	5	192	- 144	1	- 9 k 7				
34	122	- 111	11	14	68	14	< 55	- 1	0	< 53	52	8	< 39	6	50	- 49	1	99	105			
35	134	- 112	2	125	- 145	15	< 151	- 154	15	< 53	- 11	9	< 42	47	7	80	74	2	142	- 141		
36	45	- 15	3	223	- 232	- 6 k 6	2	53	- 43	128	111	121	124	9	165	159	3	52	- 55			
37	85	44	4	< 26	7	0	45	- 45	5	132	- 126	11	22	10	68	65	6	45	- 8			
38	59	53	1	101	87	1	93	- 93	4	85	- 82	13	67	- 67	11	68	55	2	45	- 8		
39	55	24	2	121	- 119	3	94	- 94	5	53	- 53	14	94	- 98	12	107	113	7	47	- 47		
40	134	121	6	538	409	4	143	- 143	8	< 57	- 44	15	52	- 52	13	50	- 14	8	48	26		
41	61	- 61	9	95	67	5	289	- 237	8	< 57	- 55	16	102	- 104	14	56	45	9	49	19		
42	206	10	11	< 37	- 5	6	249	- 204	10	98	- 76	1	< 1 k 7	11	114	- 111	10	71	- 28			
43	65	44	11	177	- 160	7	115	86	10	75	- 76	1	< 156	138	1	34	- 30	12	117	- 118		
44	65	- 115	12	155	145	8	342	- 300	- 10 k 6	207	- 255	3	50	51	3	< 41	26	14	67	69		
45	1 k 6	14	< 50	- 54	10	147	- 140	10	57	- 55	151	- 151	5	37	29	1	10 k 7	5	88	82		
46	137	168	15	75	64	11	176	- 171	2	< 44	- 35	6	101	- 89	6	67	61	5	88	82		
47	263	- 232	16	< 55	14	12	167	151	1	131	- 149	7	35	21	7	< 45	28	- 10 k 7	1			
48	225	- 210	17	85	77	13	76	- 63	4	< 45	45	8	68	- 72	8	< 47	7	1	< 44	16		
49	133	165	18	65	- 65	14	< 51	- 57	5	107	101	9	19	- 19	9	48	- 26	2	< 45	27		
50	98	- 92	20	< 45	37	15	65	- 55	5	65	80	10	37	- 44	10	20	- 28	5	< 45	55		
51	15	21	21	< 65	17	17	< 56	- 27	8	< 49	- 21	11	49	- 55	11	52	- 5	1	< 46	- 7		
52	36	49	22	150	- 190	18	102	- 100	9	< 51	12	179	12	54	- 78	5	62	- 75	6	149	169	
53	81	171	4	k 6	- 177	7	105	75	80	10	75	1	115	135	3	91	- 91	11	114	- 111		
54	63	- 58	0	273	259	0	213	204	11	98	- 123	15	15	- 29	14	97	- 116	7	< 49	26		
55	181	175	1	169	- 162	1	88	- 71	12	< 55	68	16	< 56	- 58	15	< 59	8	99	103			
56	151	- 152	2	103	- 91	12	< 41	- 19	13	14	103	103	18	58	45	16	121	- 119	9	< 52	35	
57	144	87	3	110	106	3	134	126	15	101	- 116	18	67	94	- 5 k 7	11	55	- 49	1	< 55	- 54	
58	117	- 115	4	115	114	4	74	- 74	17	101	90	1	115	135	3	91	- 91	11	115	- 114		
59	120	- 107	5	23	44	5	100	- 102	16	70	- 68	1	163	189	2	66	- 50	12	112	- 110		
60	169	172	6	48	49	6	47	- 58	17	101	90	1	115	135	3	91	- 91	11	114	- 113		
61	124	85	7	141	- 142	7	123	- 117	17	101	90	1	163	189	2	66	- 50	12	112	- 110		
62	170	- 110	8	99	86	8	< 49	- 11	0	< 55	- 53	3	114	124	2	66	- 50	12	110	- 109		
63	-1 k 6	9	< 50	- 54	1	4	125	- 122	5	< 55	- 53	116	- 136	1	128	147	2	66	- 50	12	114	- 113
64	196	210	10	266	- 252	1	131	- 148	13	68	- 68	15	< 55	- 47	1	128	- 124	3	51	- 34		
65	159	- 159	11	145	145	2	38	- 30	4	< 47	- 34	15	35	15	- 2 k 7	24	26	6	58	- 59		
66	288	188	12	< 48	35	12	< 55	- 13	4	< 56	9	7	< 34	9	43	- 2 k 7	6	80	79			
67	103	- 134	13	< 50	- 40	13	< 57	- 58	5	< 95	87	8	< 41	- 21	10	44	- 43	7	< 52	51		
68	223	- 252	14	115	- 112	14	76	- 76	8	< 43	- 29	10	72	4	5	< 29	13	6	64	- 63		
69	75	69	15	146	162	15	66	- 60	10	10	42	23	11	4	59	- 56	10	54	- 51			
70	14	14	16	14	14	16	10	10	7	23	- 27	13	19	189	1	112	- 112	6	106	- 106		
71	165	175	16	181	169	15	50	- 50	3	< 50	34	2	33	- 14	8	77	- 77	5	< 55	- 17		
72	127	127	11	106	- 98	16	137	111	7	< 51	28	1	128	146	2	66	- 50	1	< 53	33		
73	69	75	12	192	- 173	16	65	- 68	5	< 51	29	3	117	136	5	29	- 24	2	54	- 54		
74	271	- 278	13	206	188	17	160	195	6	< 100	- 111	7	11	44	- 14	3	124	- 124	6	124	- 124	
75	56	55	14	< 49	20	5	156	- 154	8	< 54	- 51	10	11	44	- 14	3	124	- 124	6	124	- 124	
76	152	152	15	51	- 1	8	9	9	10	69	- 67	192	198	1	124	- 124	6	124	- 124	6	124	- 124
77	156	156	15	51	- 1	8	9	9	10	69	- 67	192	198	1	124	- 124	6	124	- 124	6	124	- 124
78	177	- 177	17	204	- 204	14	74	- 74	10	91	100	7	< 56	48	7	< 40	- 8	8	117	- 113		
79	36	- 41	18	141	148	3	< 47	- 3	25	0	88	- 112	10	9	< 50	- 153	1	124	- 214	2	124	- 214
80	209	- 199	8	< 45	- 22	0	101	106	11	< 60	- 78	11	11	44	- 32	3						

Table 4. Continued.

0	1 k 8	3 x 8	2	166	163	10	< 62	0	15	< 67	85	7	-14 k 8	1	262	214				
1	< 175	201	0	172	-145	3	58	58	11	< 64	29	16	132	100	3	104	-89			
1	< 29	13	1	82	66	4	< 48	37	12	136	126	10	k 8	8	235	-161				
2	86	-85	2	88	-81	5	43	-45	1	80	-78	0	< 63	47	1	221	147			
3	178	211	3	65	-65	6	70	60	0	< 39	-75	1	< 63	-52						
4	117	138	4	64	89	7	69	94	1	133	207	2	< 63	-66	-15 k 8	1	85	-98		
5	70	-84	5	64	8	136	-31	2	269	207	3	< 63	-53	0	59	-55				
6	< 39	1	6	< 45	7	9	< 55	-47	3	56	46	4	91	66	1	67	61			
7	81	84	7	213	-249	10	85	-58	4	180	-187	-10 k 8	7	141	145					
8	107	-103	8	< 49	46	11	55	-48	4	156	156	10	b 0.10	9	91	-108				
9	87	-83	9	124	131	12	< 104	-86	6	< 45	-2	1	78	14	7	123	136			
10	106	-119	10	< 53	5	13	< 53	-17	7	< 41	23	2	229	215	13	172	124			
11	127	-128	11	< 55	52	14	< 55	-32	8	< 49	24	3	93	-69	11	55	33			
13	117	-113	12	95	95	15	< 67	-39	9	60	4	105	-101	10	150	-171				
14	89	-105	13	< 5	98	16	79	-62	10	90	90	5	95	95	1	< 56	18			
15	71	-46	0	219	191	-5 k 8	11	56	-57	6	< 24	35	9	66	70	1	< 57	41		
16	110	103	1	133	-128	0	140	169	1	147	-143	13	< 60	14	7	83	29			
17	105	-107	2	55	-45	5	70	-83	14	< 58	7	55	-2	159	-172	3	< 58	-22		
18	79	-49	3	97	111	4	71	64	3	74	78	9	< 58	52	4	48	4			
	-1 k 8	4	4	72	-71	16	149	-120	10	< 60	-8	4	154	-161						
0	435	-324	6	250	181	5	251	-285	17	< 69	-26	12	152	-157						
1	63	121	6	155	-121	6	56	35	18	27	120	13	< 55	39	1	204	-223			
2	143	119	7	167	-166	8	71	< 43	27	< 45	20	8 k 8	14	67	31	9	< 64	-44		
3	< 27	6	7	171	74	8	< 45	-20	10	192	0	150	-123	15	< 69	-56				
4	134	-164	9	193	216	9	173	-192	1	< 56	2	16	76	1	< 47	22				
5	147	-163	10	121	-103	10	79	75	1	< 56	2	16	76	2	303	-231				
6	91	89	11	< 51	51	11	193	208	2	67	56	17	71	40	3	< 45	196			
7	120	-128	12	< 54	51	12	< 55	26	3	< 70	40	18	116	129	14	143	141			
8	< 42	-1	13	< 56	56	4	< 55	20	3	< 57	17	17	11	11	5	135	-111			
9	56	-53	14	98	92	15	< 58	-93	5	< 58	9	0	97	-84						
10	112	117	15	110	-125	15	12	103	6	< 59	49	1	< 60	-23	1	56	10			
11	87	90	16	64	74	15	12	7	50	128	2	< 66	1	70	-84	1	< 60	-40		
	77	-71	4	4 k 8	6 k 8	0	104	-85	-8 k 8	3	< 66	-14	1	< 66	-14					
12	126	-80	0	< 45	10	1	< 49	8	0	< 43	52	4	< 67	-15						
14	171	178	1	< 42	4	1	< 49	8	0	< 43	52	4	< 67	-15						
15	< 60	-28	2	200	-178	2	50	21	1	< 70	-61	5	< 67	-20	105	94	3	< 63	-76	
16	157	-135	3	152	149	3	122	-114	2	< 117	111	6	< 68	21	5	77	4			
	20 k 8	4	114	124	4	87	77	73	3	< 103	107	7	< 68	21	3	95	-108			
0	205	-197	5	< 46	5	24	< 52	24	4	< 113	119	-11 k 8	5	< 55	30	b 5 12				
1	79	65	6	46	27	5	< 52	24	5	127	-131	0	< 53	50	105	125	0	< 123		
2	230	-196	7	76	93	7	187	-175	6	66	49	1	< 53	-41	1	232	-181			
3	< 55	7	8	< 51	36	8	< 56	-45	7	164	155	2	< 53	22	2	< 70	73			
4	47	-34	9	< 53	30	9	86	80	8	< 57	72	3	99	91	2	148	-136			
5	147	-162	10	< 55	39	10	68	-58	9	132	-137	4	< 56	9	3	109	-97			
6	80	67	11	76	70	-6 k 8	121	125	11	< 137	133	6	< 57	35	5	93	102			
7	39	-39	0	315	330	12	55	42	7	209	211	2	110	-96	b 1 10	0	156	157		
8	114	-137	1	< 54	23	9	9	8	8	< 59	-7	5	127	-103	0	156	157			
9	67	-67	14	73	50	2	< 54	23	9	119	99	h 2 9	1	64	-83	2	64	-83		
10	< 23	15	< 66	-33	3	< 37	14	0	55	-45	9	100	94	10	< 54	8	3	101	-101	
11	92	92	16	68	78	4	39	44	1	< 49	56	11	< 64	41	10	< 54	8	4	60	-10
12	114	-108	17	80	79	5	95	86	2	< 60	50	12	< 65	-13	13	< 54	8	5	74	-83
13	78	72	18	92	-106	6	162	-168	3	< 60	61	13	94	-86	14	< 54	8	5	74	-83
14	129	138	7	214	-214	10	10	-101	5	< 66	-9	15	64	-59	17	63	84			
15	62	0	-4 k 8	-290	64	6	< 67	5	79	71	-12 k 8	2	< 66	-96	b 4 9					
16	100	-107	1	122	161	9	121	-117	6	< 62	-6	0	94	96	1	51	26			
	2	94	110	10	149	-132	7	72	-44	1	89	-88	127	-125	1	127	125			
	-2 k 8	3	57	58	11	< 54	-34	8	65	-54	2	131	-132	4	48	39				
0	367	300	4	192	-225	12	< 56	-32	3	209	227	-13 k 8	4	< 50	-51					
1	< 15	-26	5	< 35	11	13	55	-37	1	80	-76	0	< 58	-39	1	125	107			
2	< 22	6	73	68	14	14	-150	1	80	-76	0	< 50	-7	0	< 50	9	114	99		
3	130	170	7	42	47	15	< 63	-1	2	120	-103	1	< 50	11	2	60	-60			
4	65	66	8	92	93	16	118	-112	2	100	-90	2	109	105	2	< 51	-47	319	311	
5	216	-254	9	< 46	16	7 k 8	29	-23	3	147	-143	3	< 52	-44	117	109				
6	< 36	-6	10	170	161	0	< 53	-13	4	< 48	22	3	< 61	-52	4	< 53	19	1	< 60	-19
7	59	-51	11	< 52	17	1	65	-44	6	116	-118	5	< 62	25	5	54	-55	0	< 61	95
8	60	-84	12	75	-69	2	127	-156	7	183	-181	6	< 63	-35	6	117	-97	1	105	105
9	166	-168	13	< 54	14	3	54	11	8	129	121	7	< 64	-44	7	55	-47			
10	81	-88	14	145	156	4	88	-89	8	26	45	8	< 65	19	b 2 10	0	141	-111		
11	180	201	15	143	-138	5	55	-55	10	< 58	-55	9	< 66	33	2	129	-163	0	< 66	-67
12	< 53	-12	16	144	-150	6	56	-18	11	< 59	-32	10	< 67	-1	2	56	48	1	< 66	-67
13	< 56	-37	7	58	37	12	< 61	32	11	< 68	-73	13	< 65	154	2	135	154			
14	115	-126	5	5	58	7	58	37	12	< 61	32	11	< 68	-73	2	127	109			
15	< 61	48	0	137	-128	8	< 59	-5	13	< 63	43	12	< 75	-72	5	85	-76			
16	99	102	1	< 46	34	9	< 60	-22	14	< 133	-126	15	< 70	-58	5	85	-76			

using anisotropic temperature factors for the mercury atoms resulted in a final  $R$  factor of 0.117 for the 2350 observed reflections. In the final cycle all shifts in parameters were less than one tenth of the calculated standard deviations.

The final parameter values are given in Table 3, and a comparison between observed and calculated structure factors is given in Table 4. Because of the presence of absorption errors in the observed  $F$  values the anisotropic temperature factors have no physical meaning and for this reason, only the isotropic temperature factors are given in Table 3.

The final parameter values were used for the calculation of a three-dimensional electron density map and a corresponding difference map. In the electron density map the peak heights were between 320 and 366 e/ $\text{\AA}^3$  for the mercury atoms and 50 and 54 e/ $\text{\AA}^3$  for the chlorine atoms. The average peak

height for the oxygens was  $15 \text{ e}/\text{\AA}^3$  with a lowest value (for  $O_6$ ) of  $10 \text{ e}/\text{\AA}^3$ . In the difference map all peaks, except in the immediate vicinity of the mercury positions, were below  $4 \text{ e}/\text{\AA}^3$ .

### DISCUSSION OF THE STRUCTURE

Interatomic distances and bond angles are given in Table 5. Projections of the structure along the  $a$  and  $c$  axes are shown in Fig. 1.

Each mercury in the structure forms two short bonds to surrounding oxygens with bond lengths of 1.93 to 2.10 Å, (average value 2.02 Å). The bonds to the non-bridging oxygens (average bond length 1.95 Å) are shorter,

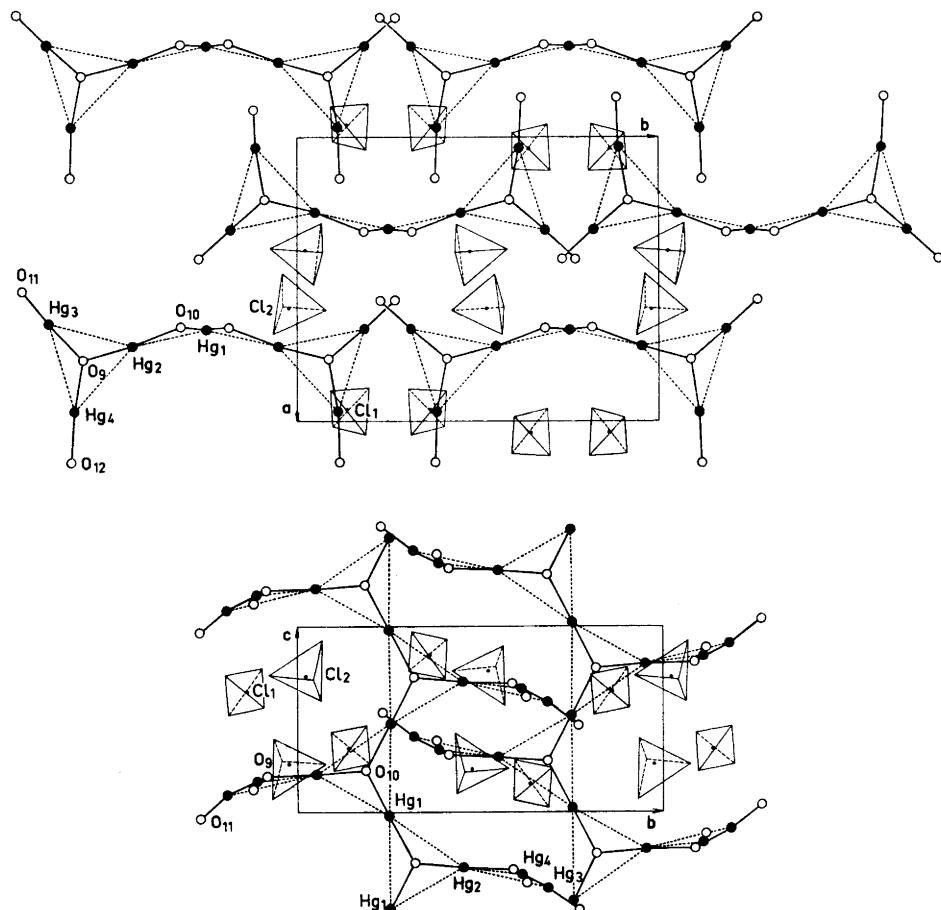


Fig. 1. Projections of the structure along the  $c$  and  $a$  axes. Full-drawn lines indicate covalent  $\text{Hg}-\text{O}$  bonds. Mercury atoms, which share covalently bonded oxygens, are connected by dotted lines.

and probably significantly so, than the bonds to the bridging oxygens (average bond length 2.04 Å). The corresponding O–Hg–O angles are close to 180° (Table 5). Other Hg–O distances are larger than about 2.7 Å and probably

Table 5. Interatomic distances and angles.

Hg–O distances (< 3.5 Å)

Hg <sub>1</sub> –O <sub>10</sub>	1.99 (3) Å	Hg <sub>2</sub> –O <sub>9</sub>	1.98 (3) Å
–O <sub>10</sub>	2.10 (3)	–O <sub>10</sub>	2.06 (3)
–O <sub>12</sub>	2.71 (4)	–O <sub>12</sub>	2.65 (4)
–O <sub>8</sub>	2.78 (9)	–O <sub>8</sub>	2.66 (8)
–O <sub>11</sub>	2.79 (4)	–O <sub>6</sub>	2.70 (7)
–O <sub>5</sub>	2.83 (4)	–O <sub>1</sub>	2.84 (6)
–O <sub>4</sub>	3.14 (5)	–O <sub>5</sub>	2.85 (4)
Hg <sub>3</sub> –O <sub>11</sub>	1.96 (4) Å	Hg <sub>4</sub> –O <sub>12</sub>	1.93 (4) Å
–O <sub>9</sub>	2.05 (3)	–O <sub>9</sub>	2.06 (3)
–O <sub>11</sub>	2.81 (4)	–O <sub>1</sub>	2.72 (6)
–O <sub>6</sub>	2.88 (7)	–O <sub>2</sub>	2.91 (5)
–O <sub>2</sub>	3.10 (5)	–O <sub>3</sub>	2.92 (5)
–O <sub>7</sub>	3.17 (6)	–O <sub>1</sub>	2.99 (6)
–O <sub>2</sub>	3.17 (5)	–O <sub>4</sub>	3.13 (5)
–O <sub>8</sub>	3.49 (8)	–O <sub>4</sub>	3.14 (6)

O–Hg–O angles

O <sub>10</sub> –Hg <sub>1</sub> –O <sub>10</sub>	171.8° (18)	O <sub>9</sub> –Hg <sub>2</sub> –O <sub>10</sub>	172.8° (12)
O <sub>9</sub> –Hg <sub>3</sub> –O <sub>11</sub>	172.9° (14)	O <sub>9</sub> –Hg <sub>4</sub> –O <sub>12</sub>	171.9° (15)

Hg–Hg distances (< 4.5 Å)

Hg <sub>1</sub> –Hg <sub>2</sub>	3.386 (2) Å	Hg <sub>2</sub> –Hg <sub>1</sub>	3.386 (2) Å
–Hg <sub>2</sub>	3.507 (2)	–Hg <sub>4</sub>	3.398 (3)
–2Hg <sub>1</sub>	3.612 (3)	–Hg <sub>1</sub>	3.507 (2)
–Hg <sub>3</sub>	4.141 (3)	–Hg <sub>3</sub>	3.514 (3)
–Hg <sub>4</sub>	4.345 (3)	–Hg <sub>4</sub>	3.943 (5)
Hg <sub>3</sub> –Hg <sub>2</sub>	3.514 (3) Å	Hg <sub>4</sub> –Hg <sub>2</sub>	3.398 (3) Å
–Hg <sub>4</sub>	3.515 (3)	–Hg <sub>3</sub>	3.515 (3)
–2Hg <sub>3</sub>	4.070 (3)	–Hg <sub>4</sub>	3.942 (4)
–Hg <sub>1</sub>	4.141 (3)	–Hg <sub>2</sub>	3.943 (5)
		–Hg <sub>1</sub>	4.345 (3)

Hg–O distances involving O<sub>9</sub>–O<sub>12</sub> (< 4.5 Å):

O <sub>9</sub> –Hg <sub>2</sub>	1.98 (3) Å	O <sub>10</sub> –Hg <sub>1</sub>	1.99 (3) Å
–Hg <sub>4</sub>	2.05 (3)	–Hg <sub>2</sub>	2.06 (3)
–Hg <sub>3</sub>	2.05 (3)	–Hg <sub>1</sub>	2.10 (3)
–Hg <sub>3</sub>	4.38 (3)	–Hg <sub>3</sub>	4.21 (3)
–Hg <sub>4</sub>	4.45 (3)		
O <sub>11</sub> –Hg <sub>3</sub>	1.96 (4) Å	O <sub>12</sub> –Hg <sub>4</sub>	1.93 (4) Å
–Hg <sub>1</sub>	2.79 (4)	–Hg <sub>2</sub>	2.65 (4)
–Hg <sub>3</sub>	2.81 (4)	–Hg <sub>1</sub>	2.71 (4)
–Hg <sub>1</sub>	4.48 (4)	–Hg <sub>4</sub>	4.14 (4)
		–Hg <sub>1</sub>	4.26 (4)

Table 5. Continued.

Hg—O—Hg angles			
$Hg_3 - O_9 - Hg_3$	121.0° (16)	$Hg_1 - O_{10} - Hg_1$	123.9° (16)
$Hg_2 - O_9 - Hg_4$	114.7 (15)	$Hg_1 - O_{10} - Hg_2$	113.2° (15)
$Hg_3 - O_9 - Hg_4$	117.8° (15)	$Hg_1 - O_{10} - Hg_2$	114.7 (15)
Cl—O distances in the perchlorate groups			
$Cl_1 - O_1$	1.36 (6) Å	$Cl_2 - O_5$	1.42 (4) Å
—O <sub>2</sub>	1.29 (5)	—O <sub>6</sub>	1.41 (7)
—O <sub>3</sub>	1.27 (6)	—O <sub>7</sub>	1.43 (7)
—O <sub>4</sub>	1.41 (6)	—O <sub>8</sub>	1.60 (8)

correspond to non-bonding contacts. The formation of two linear covalent bonds from the mercury atom has been found in many other structures.<sup>8</sup> The corresponding Hg—O bond lengths are usually found to be close to 2.0 Å.<sup>9</sup>

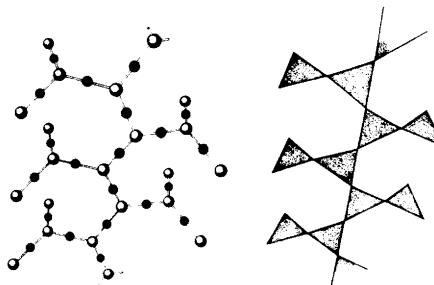
Two types of covalently bonded oxygen atoms are present in the structure. The oxygens O<sub>9</sub> and O<sub>10</sub> are each bound to three Hg atoms at distances between 1.98 and 2.10 Å, and O<sub>11</sub> and O<sub>12</sub> are each bound to only one Hg atom at distances of 1.96 Å and 1.93 Å. Besides being covalently bound to one Hg atom each of O<sub>11</sub> and O<sub>12</sub> is also in non-bonding contact with two other Hg atoms at distances varying between 2.65 and 2.81 Å (Table 5).

In addition to the 8 negative charges from the perchlorate groups, 24 more are needed to neutralize the positive charges of the 16 Hg atoms in the unit cell. These must be provided by the 16 covalently bound oxygen atoms (O<sub>9</sub>—O<sub>12</sub>). It seems reasonable to assume that O<sub>9</sub> and O<sub>10</sub>, which are each bound to three Hg atoms, represent O<sup>2-</sup>, and O<sub>11</sub> and O<sub>12</sub>, which are each bound to only one Hg atom, represent OH<sup>-</sup>. The correct formula for the compound should then be written Hg<sub>2</sub>OOHClO<sub>4</sub>.

The shortest Hg—Hg distances range from 3.39 to 3.61 Å (average value 3.50 Å) and occur between those mercury atoms, that are joined by the covalently bound oxygens O<sub>9</sub> and O<sub>10</sub>. The next shortest Hg—Hg distances are longer than about 4.0 Å (Table 5.)

If only the mercury atoms and the covalently bound oxygen atoms are considered, the structure can be described as being built up from infinite one-dimensional complexes as illustrated in Figs. 1 and 2. Characteristic features in these complexes are the OHg<sub>3</sub> groups consisting of three Hg atoms at the corners of a triangle with an oxygen (O<sub>9</sub> or O<sub>10</sub>) slightly above the center of

Fig. 2. A perspective view of one of the infinite one-dimensional complexes which can be distinguished in the structure when only the mercury atoms and the covalently bound oxygens are considered. Small filled circles indicate mercury atoms. Large circles indicate the oxygens O<sub>9</sub> and O<sub>10</sub>, which are each bonded to three Hg atoms, or O<sub>11</sub> and O<sub>12</sub>, which are each bonded to only one Hg atom. To the right, the Hg<sub>3</sub>-triangles of the OHg<sub>3</sub>-groups are separately drawn.



the triangle. The complexes can be described as built up from such triangles sharing corners as shown in Fig. 2. Similar  $\text{OHg}_3$  groups can be distinguished in several other basic salts of mercury. In  $\text{Hg}_3\text{OCl}_4$  discrete  $\text{OHg}_3\text{Cl}_3^+$  ions occur<sup>10</sup> with  $\text{Hg}-\text{Hg}$  distances of 3.53 Å and  $\text{Hg}-\text{O}$  distances of 2.05 Å, which are close to the values found here. The oxygen atom in the  $\text{OHg}_3\text{Cl}_3^+$  ion is about 0.3 Å above the plane formed by the three  $\text{Hg}$  atoms.<sup>11</sup> This is found also in the present structure, where the  $\text{O}_9$  and  $\text{O}_{10}$  atoms are about 0.3 Å (0.25 Å and 0.31 Å, respectively) above the plane of the three  $\text{Hg}$  atoms to which they are bound.

The average values for the  $\text{Cl}-\text{O}$  and  $\text{O}-\text{O}$  distances in the perchlorate groups are of the magnitude expected. The variations of the individual distances from the calculated mean are consistent with the estimated standard deviations.

As will be shown in a following paper the structure of  $\text{Hg}_2\text{OOHClO}_4$  is closely related to that of the less basic  $\text{Hg}_7\text{O}_4(\text{OH})_2(\text{ClO}_4)_4$ . The less basic salt is found also to be built up from infinite one-dimensional complexes, which can, in fact, be described as being formed by the condensation of two of the infinite complexes in  $\text{Hg}_2\text{OOHClO}_4$ .

*Acknowledgements.* The work has been supported by *Statens Naturvetenskapliga Forskningsråd (Swedish Natural Science Research Council)*. Computer time has been made available by the *Computer Division of the National Swedish Office for Administrative Rationalisation and Economy*.

We wish to thank Mrs. Sissel Lindman for assistance in the work, and Dr. Derek Lewis for linguistic corrections.

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Received May 25, 1971.