# The Crystal Structure of Nb<sub>12</sub>O<sub>29</sub>(o-rh)

#### ROLF NORIN

Institute of Inorganic and Physical Chemistry, University of Stockholm, Stockholm, Sweden

The crystal structure of  $\mathrm{Nb_{12}O_{29}(o\text{-rh})}$  has been studied using single-crystal X-ray methods. The unit cell has the dimensions:

$$\begin{array}{ll} a &= (28.90 \pm 0.02) \text{ Å} \\ b &= (3.835 \pm 0.002) \text{ Å} \\ c &= (20.72 \pm 0.02) \text{ Å} \\ V &= 2296 \text{ Å}^3 \end{array}$$

and contains 4 units of  $\mathrm{Nb_{12}O_{29}}$ . The structure proposed has the symmetry Amma and may be described in terms of regular  $\mathrm{NbO_{6}}$ -octahedra, which share edges and corners to form an infinite three-dimensional framework.

A monoclinic modification of  $Nb_{12}O_{29}$  has been identified from its powder pattern.

The present study has been carried out in continuation of previous work in the field of the structural chemistry of niobium oxides conducted by members of this research group  $^{1-3}$ . A phase analysis of this metal oxide system  $^2$  performed within this research programme has demonstrated the existence of a few previously unknown phases at high contents of oxygen. The present structure investigation is concerned with an oxide obtained from the "phase" reported to form at the approximate composition  $\mathrm{NbO}_{2.40}^2$ . Actually all the samples of this composition hitherto prepared have invariably been found to contain two different phases which, however, both ideally have the composition  $\mathrm{Nb}_{12}\mathrm{O}_{29}$  ( $\mathrm{NbO}_{2.42}$ ).

In the course of the present study it was found that the phase investigated is isostructural with the mixed titanium niobium oxide phase  ${\rm Ti_2Nb_{10}O_{29}}$  (o-rh) recently reported by Wadsley <sup>4</sup>. The powder pattern of the phase coexisting with the former indicates that it is isostructural with the monoclinic modification of  ${\rm Ti_2Nb_{10}O_{29}(mon)}$ .

#### EXPERIMENTAL

The crystals used in this study were prepared in two different ways. In the first preparation an appropriate mixture of  $\mathrm{Nb}_2\mathrm{O}_5$  (purity 99.9 %) and  $\mathrm{NbO}_2$  (prepared by reducing  $\mathrm{Nb}_2\mathrm{O}_5$  in a stream of hydrogen) was pressed into small tablets and melted

in an electric arc furnace in an argon atmosphere. The powdered sample was then tempered 14 days in evacuated silica tubes at  $1100^{\circ}$ C. In the second preparation the oxide mixture was not melted but tempered in the same way for 60 days. The Guinier powder patterns of the two preparations were identical, but in the first case the crystals were bigger and better suited for single crystal work. The crystals of the samples NbO<sub>2.40</sub> were black and formed aggregates which were easy to cleave into small rods.

To determine the oxygen content weighed samples were heated in a stream of oxygen at  $700^{\circ}$ C to constant weight, forming Nb<sub>2</sub>O<sub>5</sub>. No deviation was found from the synthesis compositions of the samples.

Table 1. Powder photograph of the sample NbO<sub>2.40</sub> containing Nb<sub>12</sub>O<sub>29</sub>(o-rh) and Nb<sub>12</sub>O<sub>29</sub>(mon). CuK $\alpha$  radiation.  $\lambda_{\text{Cu}K\alpha}=1.5418$  Å.

|  |  | ]           | Nb <sub>12</sub> O <sub>29</sub> (o-rh)                                   |                | $\mathrm{Nb_{12}O_{29}(mon)}$ |  |              |
|--|--|-------------|---|----------------|-------------------------------|--|--------------|
| $I_{ m obs}$                               | $\begin{vmatrix} \sin^2\Theta \times 10^5 \\ \text{obs} \end{vmatrix}$ | $h \ k \ l$ | $\begin{vmatrix} \sin^2\Theta \times 10^5 \\ \mathrm{calc} \end{vmatrix}$ | $p \ F^2$ calc | h k l                         | $\begin{vmatrix} \sin^2\!\Theta\!	imes\!10^5\  m calc \end{vmatrix}$ | $p F^2$ calc |
| w  | 286  | 200         | 285   | 1              | 100                           | 285  | 1 *          |
| $\mathbf{v}\mathbf{w}$                     | 603  |             |   | _              | $10\overline{2}$              | 601  | <b>2</b>     |
| $\mathbf{v}\mathbf{w}$                     | 625  | $1 \ 0 \ 2$ | 625   | 3              | 0.00                          | 272  | _            |
| vvw  | 652  |             | 7700  |                | 0 0 2                         | 652  | 1            |
| w  | 1143   | 400         | 1139  | 4              | 200                           | 1141   | 1 *          |
| ${f st}$                                   | 2221   | 004         | 2214  | 18             | $10\overline{4}$              | 2221   | 26 *         |
| $\mathbf{v}\mathbf{v}\mathbf{w}$           | 2281   | 104         | 2285  | 5              |                               | 2707   | - 4          |
| m  | 2566   | 600         | 2563  | 17             | 3 0 0                         | 2567   | 5 *          |
| $\mathbf{vst}$                             | 4185   | 011         | 4177  | 51             |                               |  | 10           |
| $\mathbf{vst}$                             | 4205   |             | 1212  |                | 011                           | 4205   | 19           |
| $\mathbf{m}$                               | 4251   | 111         | 4248  | 77             |                               | 4000   |              |
| $\mathbf{w}$                               | 4319   |             |   |                | $11\overline{1}$              | 4322   | 6            |
| $\mathbf{vvst}$                            | 4563   | 800         | 4557  | 127            | 400                           | 4563   | 27 *         |
| $\mathbf{v}\mathbf{v}\mathbf{w}$           | 4662   |             |   | - 0            | 111                           | 4658   | 5            |
| vvw  | 4819   | 3 1 1       | 4818  | 12             | 20=                           | 1000   | 2 4          |
| $\mathbf{vst}$                             | 4993   | 006         | 4982  | 63             | $20\ \overline{6}$            | 4993   | 2 *          |
| m  | 5063   | 106         | 5063  | 34             |                               | 7000   | - 4          |
| $\mathbf{st}$                              | 5289   | 013         | 5285  | 31             | 113                           | 5290   | 7 *          |
| $\mathbf{v}\mathbf{v}\mathbf{w}$           | 5678   |             |   |                | $\frac{2}{1}\frac{1}{1}$      | 5682   | 5            |
| $\mathbf{v}\mathbf{v}\mathbf{w}$           | 6378   |             |   |                | $50\overline{4}$              | 6378   | 10           |
| $\mathbf{v}\mathbf{v}\mathbf{w}$           | 6760   | 804         | 6771  | 7              |                               | -100   | 2 4          |
| $\mathbf{v}\mathbf{w}$                     | 7119   | $10\ 0\ 0$  | 7120  | 11             | 500                           | 7130   | 2 *          |
| vw   | 7271   |             |   |                | $\frac{311}{1}$               | 7276   | 11           |
| $\mathbf{v}\mathbf{v}\mathbf{s}\mathbf{t}$ | 7575   | $1 \ 1 \ 5$ | 7570  | 123            | $11\overline{5}$              | 7562)  | 36 *         |
|  |  |             |   |                | $2 1 \overline{5}$            | 7578)  | 15 *         |
| $\mathbf{v}\mathbf{w}$                     | 7668   | 711         | 7666  | 73             | 4.3.=                         | 0000   | 0.7          |
| $\mathbf{v}\mathbf{w}$                     | 8090   |             | 27.40   |                | 411                           | 8096   | 31           |
| $\mathbf{w}$                               | 8137   | 3 1 5       | 8140  | 17             | $31\overline{5}$              | 8164   | 26 *         |
| vvw  | 8472   | 706         | 8471  | 31             | 1                             | 1  |              |
| vvw  | 8740   | 8 1 1       | 8734  | 40             | 0.05                          | 0000   | ,            |
| $\mathbf{v}\mathbf{v}\mathbf{w}$           | 8892   | • 0 -       | 2020  | • •            | $60\overline{2}$              | 8903   | 1            |
| vvw  | 8915   | 108         | 8929  | 10             | 200                           | 0005   | ~            |
| $\mathbf{v}\mathbf{w}$                     | 9039   |             | 0000  |                | 206                           | 9025   | 5            |
| W  | 9269   | 5 1 5       | 9282  | 17             | 115                           | 9242   | 22 *         |
| $\mathbf{v}\mathbf{v}\mathbf{w}$           | 9426   | 0.0.3       | 0.500   | 0.4            | 411                           | 9440   | 6            |
| $\mathbf{v}\mathbf{w}$                     | 9535   | 806         | 9539  | 34             | 1                             | 1  |              |

<sup>\*</sup> Overlap.

The density of the crystals was determined from the apparent loss of weight in benzene. It was found to be  $(4.62 \pm 0.02)$  g cm<sup>-3</sup>.

#### UNIT CELL AND SPACE GROUP

A rod-shaped crystal about 0.3 mm in length and 0.05 mm in diameter was split from a larger one. It was rotated around the rod axis and rotation and Weissenberg photographs (h0l-h2l) were taken with CuK radiation. With another crystal, roughly cubic in shape and with an edge of about 0.2 mm, rotation and Weissenberg photographs (0kl) were taken. It was concluded that the crystals have orthorhombic symmetry and that the dimensions of the unit cell are about 28.9 Å, 3.84 Å and 20.7 Å. The reflexions were recorded photographically with the multiple film technique and the relative intensities were estimated visually by comparison with an intensity scale, obtained by photographing a suitable reflexion with different exposure times. Lorentz and polarisation factors according to  $Lu^5$  were applied to the observed intensities. The effect of temperature factor was found to be negligible when calculated by the ordinary procedure. Probably it cancels out with the specimen absorbtion.

More accurate values for the unit cell dimensions were calculated from a powder photograph, taken with  $\operatorname{Cu} K\alpha$  radiation in a Guinier focusing camera. KCl was used as an internal standard (see Table 1). In addition to the lines due to  $\operatorname{Nb}_{12}\operatorname{O}_{29}$  (o-rh), the photograph contained many extra ones that will be discussed later in this paper. The following cell dimensions were obtained:

$$a = (28.90 \pm 0.02) \text{ Å}$$
  
 $b = (3.835 \pm 0.002) \text{ Å}$   
 $c = (20.72 \pm 0.02) \text{ Å}$   
 $V = 2296 \text{ Å}^3$ 

The value found for the density of the heterogeneous sample suggests that there are 4 formula units in the unit cell. The reflexions systematically absent are:

$$hkl$$
 with  $k + l = odd$   
 $hk0$  with  $h = odd$ 

This is characteristic of the three space groups No. 63 Amma, No. 40 Am2a and No. 36  $A2_1ma.*$ 

At first only the space group of highest symmetry (Amma) was considered. Since it was possible to find a plausible structure assuming this space group, the low symmetry ones  $(Am2a \text{ and } A2_1ma)$  were not taken into account. In space group No. 63 Amma the following point positions are possible:

<sup>\*</sup> To facilitate a comparison with related substances, the space groups have been given in orientations differing from those given in the *International Tables for X-ray Crystallography* <sup>6</sup>.

```
 \begin{array}{c} (0,0,0;\ 0,\frac{1}{2},\frac{1}{2}) + \\ 4(a);\ 0,0,0;\ \frac{1}{2},0,0, \\ 4(b);\ 0,0,\frac{1}{2};\ \frac{1}{2},0,\frac{1}{2}, \\ 4(c);\ \pm (\frac{1}{4},0,z), \\ 8(d);\ 0,\frac{1}{4},\frac{1}{4};\ 0,\frac{1}{4},\frac{3}{4};\ \frac{1}{2},\frac{1}{4},\frac{1}{4};\ \frac{1}{2},\frac{1}{4},\frac{3}{4}, \\ 8(e);\ \pm (0,y,0);\ \pm (\frac{1}{2},y,0), \\ 8(f);\ \pm (x,0,z);\ \pm (\frac{1}{2}-x,0,z), \\ 8(g);\ \pm (\frac{1}{4},y,z);\ \pm (\frac{1}{4},\bar{y},z), \\ 16(h);\ \pm (x,y,z);\ \pm (\bar{x},y,\bar{z});\ \pm (\frac{1}{2}-x,y,z);\ \pm (\frac{1}{2}+x,y,\bar{z},). \end{array}
```

#### POSITIONS OF THE ATOMS

The fact that the values of  $[F(h0l)]^2$  were found to be identical with those of  $[F(h2l)]^2$  (with due regard for observational errors) indicated that all the atoms of the structure are situated in, or very close to, two planes normal to the y axis and at a distance of b/2 Å apart.

In order to find the niobium positions, the Patterson projection P(upw) and the Harker sections P(u0w) and  $P(u\frac{1}{2}w)$  were calculated from the  $|F|^2$  values of the layer lines h0l and h1l.\* The strongest maxima in P(upw) (Fig. 1) are arranged in rows parallel to the axes, and situated close to the corners of square nets with an edge length of about 3.8 Å, which is also the length of the b axis. This is in conformity with the distribution of a considerable number of the niobium atoms in approximately the same way as the metal atoms of a structure of the  $ReO_3$ -type. There are also peaks corresponding to vectors with a length of  $(n \times 3.8 + 2.9)$  Å where n = 0, 1, 2, 3. The Harker sections (Fig. 2 a & c) indicate that the atoms giving rise to these vectors are situated in planes b/2 Å apart. Furthermore, a = 28.9 Å  $\approx (6 \times 3.8 + 2 \times 2.9)$  Å and c = 20.7 Å  $\approx (4 \times 3.8 + 2 \times 2.9)$  Å.

All this leads to the suggestion that the structure is built up of sheets of  $NbO_6$ -octahedra sharing corners, the sheets being normal to the y axis and extending four octahedra in the x direction and three in the z direction (Fig. 3a). The unit cell contains four such sheets, two in each of the planes b/2 Å apart, the sheets being joined by octahedra edge sharing.

Three different possible arrangements result, and it is a matter of trial and error to find out which of these is the right one. An idealized picture of the structure thus arrived at is given in Fig. 3 b. It is built up of niobium atoms in 8(f) positions and oxygen atoms in 4(c) and 8(f) positions of space group Amma. From the Patterson projection P(upw) x and z parameters of the niobium positions could be determined. As the scattering factors for the metal atoms are dominant, the signs of the F-values could with few exceptions be determined from the contributions of these atoms only. In this way the electron density projection  $\varrho(xpz)$  was calculated \* (Fig. 4). In addition to the high metal atom peaks there are much lower ones midway

<sup>\*</sup> The electronic computer BESK was used to calculate 7,8 the Patterson and electron density projections and the Harker sections using the atomic scattering factors given by Vand, Eiland and Pepinsky <sup>10</sup>.

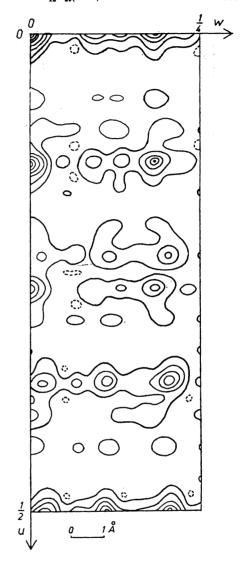


Fig. 1. The Patterson function P(upw). Dashed lines indicate negative values.

between those niobium peaks that are 3.8 Å apart, indicating the positions of the oxygen atoms linking the octahedra together by corners. Some other maxima are supposed to be due to termination effects, typical of structures of this kind  $^9$ . In order to trace the positions of the oxygen atoms situated above and below the niobium atoms, an electron density projection  $\varrho(xpz)$  with the metal atoms subtracted was calculated (Fig. 5). The oxygen atom positions obtained in this way are certainly rather approximate. However, they are in good accordance with reasonable geometrical requirements for the structure, giving fully plausible interatomic distances and coordination.

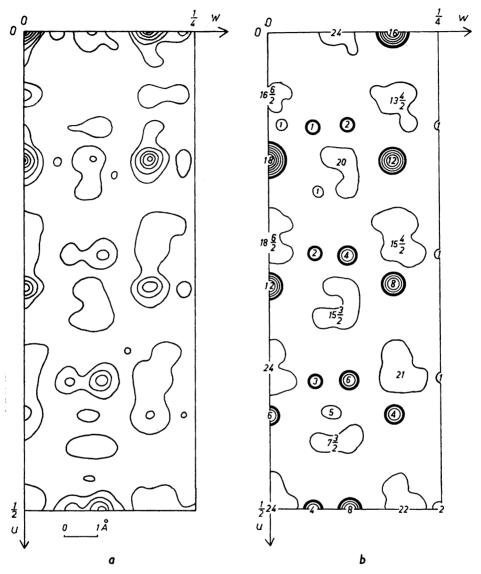
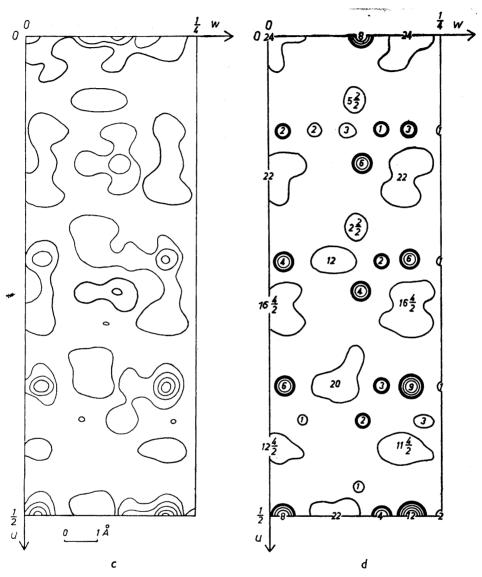


Fig. 2. a and c, the Harker sections P(u0w) and  $P(u\frac{1}{2}w)$ , respectively; b and d show areas containing the terminal points of the corresponding calculated Nb—Nb vectors as heavy circles, and irregular areas in which the Nb—O vectors end. The numbers of vectors end.

## REFINEMENT OF THE STRUCTURE

To refine the parameters of the structure, a least squares program <sup>11</sup> on the computer FACIT EDB was used. The refinement was started with the set of atomic positions derived as mentioned above. The atomic scattering



tors that terminate in the areas are given as integers for multiplicity eight and as half integers for multiplicity four.

factors used for niobium were derived from those given for Nb(0) to Nb(IV) by Thomas and Umeda <sup>12</sup>, and for oxygen those given by Suzuki <sup>13</sup>. For each atom, the coordinates and the "isotropic temperature factor" were refined together with the scale factor for each layer. Of the observed 169 structure

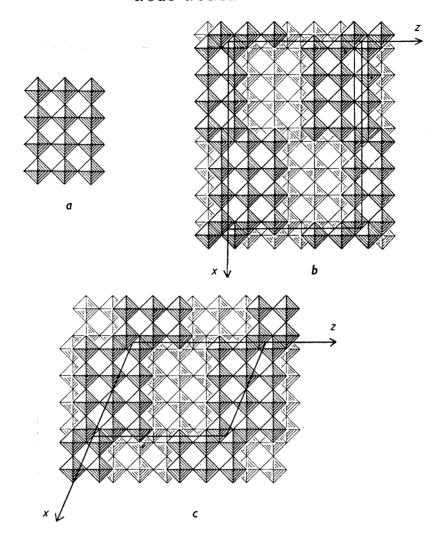


Fig.~3.~a. Sheet of twelve NbO<sub>6</sub>-octahedra with a lattice of ReO<sub>3</sub>-type; b and c. Idealized structures of orthorhombic and monoclinic Nb<sub>12</sub>O<sub>29</sub>, respectively, with one unit cell indicated.

factors, 165 were included in the minimizing of the residuals  $S = \sum_{kkl} w(|F_{\rm o}|) - |F_{\rm c}|)^2$ . For the weight w, the function:

$$w = \frac{1}{a + |F_{\rm o}| + c|F_{\rm o}|^2}$$

given by Cruickshank <sup>14</sup> was used with  $a=2|F_{\rm o}|_{\rm min}$  and  $c=2/|F_{\rm o}|_{\rm max}$ . During fifteen cycles of refinement the discrepancy factor R fell from 16.3 % to 11.6 %. At this stage, the average coordinate shift for the niobium atoms

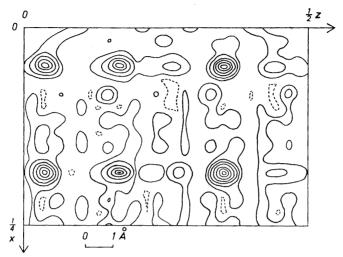


Fig. 4. Electron density projection on the xz plane. Dashed lines indicate negative values.

was  $0.1\sigma$  and for the oxygen atoms  $0.2\sigma$ . It was concluded, that the rather limited number of data did not merit further refinement of the structure.  $(|F_o| - |F_c|)$  syntheses were calculated <sup>15</sup>, <sup>16</sup> in the neighbourhood of each atomic position. No maximum or minimum with an absolute value greater than  $\frac{1}{3}$  of the lowest oxygen maximum was found. In Table 2 the final atomic parameters and their estimated errors  $2\sigma$  are listed together with the values of the "temperature factor". (Since no absorbtion correction was applied,

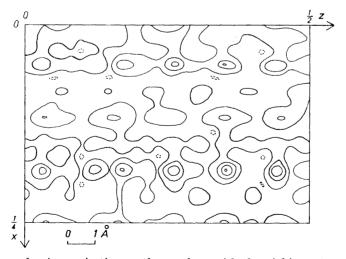


Fig. 5. Electron density projection on the xz plane with the niobium atoms subtracted. Dashed lines indicate negative values.

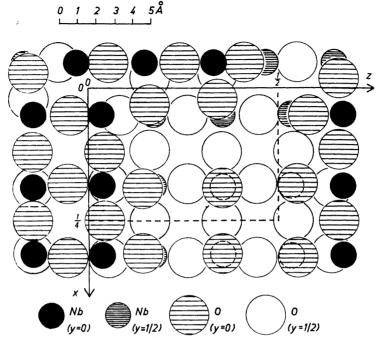


Fig. 6. Projection on the xz plane of the structure of  $\mathrm{Nb_{12}O_{29}}(\text{o-rh})$ . Dashed circles indicate the positions of niobium atoms at  $y=\frac{1}{2}$  completely overlapped by oxygen atoms at y=0.

Table 2. Fractional atomic parameters, their estimated errors  $2\sigma$  and "temperature factors" for Nb<sub>12</sub>O<sub>29</sub>(o-rh). Space group No. 63 Amma.

| 7               |                |                     |   |                                |       |  |  |  |
|-----------------|----------------|---------------------|---|--------------------------------|-------|--|--|--|
| Atom            | Point position | $x\pm 2\sigma$      | y | $z\pm 2\sigma$                 | B     |  |  |  |
|                 |                |                     |   |                                |       |  |  |  |
| $Nb_1$          | 8 <i>f</i>     | $0.049 \pm 0.001$   | 0 | $\boldsymbol{0.033 \pm 0.002}$ | +0.36 |  |  |  |
| $\mathbf{Nb_2}$ | 8 <i>f</i>     | $0.049 \pm 0.002$   | 0 | $0.670\pm0.002$                | +0.57 |  |  |  |
| $Nb_3$          | 8 <i>f</i>     | $0.049 \pm 0.001$   | 0 | $0.852 \pm 0.003$              | 0     |  |  |  |
| $Nb_4$          | 8 <i>f</i>     | $0.184 \pm 0.002$   | 0 | $\boldsymbol{0.034 \pm 0.002}$ | +0.52 |  |  |  |
| $Nb_5$          | 8 <i>f</i>     | $0.185 \pm 0.002$   | 0 | $0.669 \pm 0.002$              | +0.62 |  |  |  |
| $Nb_6$          | 8 7            | $0.187 \pm 0.001$   | 0 | $0.852 \pm 0.002$              | +0.16 |  |  |  |
| $O_1$           | 4 c            | 1/4                 | 0 | $0.04 \pm 0.01$                | -1.8  |  |  |  |
| $O_2$           | <b>4</b> c     | 1/4                 | 0 | $0.66 \ \ -0.02$               | +2.4  |  |  |  |
| $O_3$           | 4 c            | 1/4                 | 0 | $0.85 \ \pm 0.02$              | +1.3  |  |  |  |
| O <sub>4</sub>  | 8 <i>f</i>     | $0.05\pm0.01$       | 0 | 0.58 + 0.01                    | -2.3  |  |  |  |
| $O_5$           | 8 <i>†</i>     | $0.03 \pm 0.01$     | 0 | $0.16 \ \ -0.01$               | -0.2  |  |  |  |
| $O_6$           | 8 <i>f</i>     | $0.05 \ \pm 0.01$   | 0 | $0.76 \ \pm 0.01$              | -2.1  |  |  |  |
| $O_7$           | 8 <i>†</i>     | 0.02 + 0.01         | 0 | 0.34 + 0.02                    | +2.2  |  |  |  |
| $O_8$           | 8 <i>†</i>     | 0.05 + 0.01         | 0 | $0.95 \ \ -0.01$               | -1.4  |  |  |  |
| O <sub>9</sub>  | 8 <i>†</i>     | $0.12 \ \pm 0.01$   | 0 | 0.04 + 0.01                    | 0     |  |  |  |
| $O_{10}$        | 8 <i>†</i>     | $0.11 \ \ \pm 0.01$ | 0 | $0.66\pm0.01$                  | +0.4  |  |  |  |
| Oii             | 8 <i>f</i>     | $0.12  \pm 0.01$    | 0 | $0.85 \ \pm 0.02$              | +2.1  |  |  |  |
| O12             | 8 <i>f</i>     | $0.18 \pm 0.01$     | 0 | 0.55 + 0.01                    | -1.9  |  |  |  |
| O <sub>13</sub> | 8 <i>†</i>     | $0.19 \ \pm 0.01$   | Ô | $0.14 \pm 0.01$                | -1.1  |  |  |  |
| O <sub>14</sub> | 8 <i>†</i>     | $0.18 \ \pm 0.01$   | Ŏ | $0.76 \ \pm 0.01$              | -1.5  |  |  |  |
| O <sub>15</sub> | 8 <i>f</i>     | $0.19 \ \pm 0.01$   | Õ | $0.35 \ \pm 0.01$              | -1.0  |  |  |  |
| O <sub>16</sub> | 8 <i>f</i>     | $0.18 \pm 0.01$     | ŏ | $0.94 \pm 0.01$                | -1.2  |  |  |  |

Table 3. Interatomic distances and their standard deviations for Nb<sub>12</sub>O<sub>29</sub>(o-rh).

| Atom              | Number and kind of neighbouring atom.  | Distance in Å   | Atom  | Number and kind of neighbouring atom.   | Distance in Å   |
|-------------------|--|---|---|---|---|
| $Nb_1$            | Nb <sub>1</sub><br>Nb <sub>2</sub>   | $egin{array}{c} 3.15 \pm 0.03 \ 3.43 \pm 0.03 \ 3.70 \pm 0.02 \ \end{array}$                                | $O_3$   | $\begin{array}{c} 2\times \mathrm{O_{16}} \\ 4\times \mathrm{O_{15}} \\ \end{array}$  | $2.8 \pm 0.2 \\ 2.6 \pm 0.1 \\ 2.8 \pm 0.2$   |
|                   | $egin{array}{c} \mathrm{Nb_3} \\ \mathrm{O_4} \\ \mathrm{O_5} \\ \mathrm{O_9} \end{array}$                   | $egin{array}{c} 3.70 \ \pm 0.02 \ 2.15 \ \pm 0.03 \ 2.7 \ \pm 0.2 \ 2.1 \ \pm 0.1 \end{array}$              | $O_4$   | $egin{array}{cccc} 2 	imes O_{14} & & & & \\ 2 	imes O_{5} & & & & \\ & O_{10} & & & & \\ 2 	imes O_{9} & & & & \\ \end{array}$ | $egin{array}{c} 2.8 \pm 0.2 \ 2.6 \pm 0.1 \ 2.4 \pm 0.1 \ 2.9 \pm 0.1 \ \end{array}$    |
| $Nb_2$            | ${{ m O_8} \ (1)} \atop {{ m O_8} \ (2)} \atop { m Nb_3}$  | $egin{array}{ccc} 1.7 & \pm \ 0.1 \ 2.9 & \pm \ 0.1 \ 3.45 & \pm \ 0.02 \ \end{array}$                      |   | $egin{array}{cccc} 2 	imes { m O_8} & (1) \ { m O_4} \ 2 	imes { m O_8} & (2) \end{array}$                                      | $egin{array}{cccc} 3.2 \ \pm \ 0.1 \ 4.4 \ \pm \ 0.1 \ 3.6 \ \pm \ 0.1 \ \end{array}$   |
|                   | $2 	imes rac{{ m O_5}}{{ m O_6}}$   | $egin{array}{cccc} 2.01 & \pm & 0.04 \ 1.9 & \pm & 0.1 \ 1.8 & \pm & 0.1 \ \end{array}$                     | $\mathrm{O}_{\mathfrak{s}}$                                 | $egin{array}{c} \mathrm{O_7} \ 2 	imes \mathrm{O_6} \ (1) \ 2 	imes \mathrm{O_{10}} \end{array}$                                | $egin{array}{c} 2.6 \ \pm \ 0.2 \ 2.9 \ \pm \ 0.1 \ 3.0 \ \pm \ 0.1 \ \end{array}$      |
| $\mathrm{Nb}_3$   | $egin{array}{c} \mathrm{O_4} \\ \mathrm{O_7} \\ \mathrm{O_8} \end{array}$                                    | $egin{array}{cccc} 1.87 \pm 0.07 \ 2.0 \pm 0.2 \ 2.11 \pm 0.08 \ 2.0 \pm 0.1 \ \end{array}$                 |   | $egin{array}{c} \mathrm{O_s} \\ \mathrm{O_s} \\ \mathrm{O_7} \\ \mathrm{O_6} \left( \mathrm{2}  ight) \end{array}$              | $egin{array}{cccc} 3.6 \pm 0.2 \ 3.2 \pm 0.1 \ 2.4 \pm 0.1 \ 2.8 \pm 0.2 \end{array}$   |
|                   | O <sub>1</sub> O <sub>6</sub> O <sub>5</sub> -   | $egin{array}{cccc} 2.1 & \pm 0.1 \ 1.9 & \pm 0.1 \ 2.3 & \pm 0.1 \ \end{array}$                             | $O_6$   | $\begin{array}{c c} 2 \times O_7(1) \\ O_{11} \\ O_{10} \end{array}$  | $egin{array}{cccccccccccccccccccccccccccccccccccc$                                      |
| $Nb_4$            | $2	imes \mathop{ m Nb_5}_{ m O_{12}}_{ m O_{13}}$  | $egin{array}{c} 3.39 \ \pm \ 0.02 \ 1.95 \ \pm \ 0.02 \ 2.20 \ \pm \ 0.08 \ \end{array}$                    | O <sub>7</sub>  | $\begin{array}{c} O_7(2) \\ 2 \times O_6 \\ 2 \times O_8 \end{array}$   | $egin{array}{c} 2.9 \ \pm \ 0.2 \ 3.5 \ \pm \ 0.1 \ 3.2 \ \pm \ 0.1 \ \end{array}$      |
| 271               | $O_1$ $O_{16}$ $O_8$   | $egin{array}{cccc} 1.91 & \pm & 0.04 \ 2.0 & \pm & 0.1 \ 1.9 & \pm & 0.1 \ \end{array}$                     | O <sub>8</sub>  | $2	imes \stackrel{\circ}{	ext{O}_{11}} \ \stackrel{\circ}{	ext{O}_{9}} \ \stackrel{\circ}{	ext{O}_{11}}$                        | $egin{array}{c} 3.5 \ \pm \ 0.1 \ 2.7 \ \pm \ 0.2 \ 2.9 \ \pm \ 0.2 \ \end{array}$      |
| $\mathrm{Nb}_{5}$ | $2 	imes 	ext{O}_{13} \ 	ext{O}_{14} \ 	ext{O}_{2}$  | $egin{array}{c} 2.01 \pm 0.03 \ 1.89 \pm 0.08 \ 1.89 \pm 0.04 \ \end{array}$                                | O <sub>9</sub>  | $2	imes 	ext{O}_{10} 	ext{O}_{13} 	ext{O}_{13}$   | $egin{array}{c} 3.5 \ \pm \ 0.2 \ 3.2 \ \pm \ 0.1 \ 2.9 \ \pm \ 0.2 \ \end{array}$      |
| $Nb_6$            | $\begin{array}{c} O_{12} \\ O_{10} \\ 2 \times O_{15} \\ O_{16} \end{array}$                                 | $egin{array}{cccccccccccccccccccccccccccccccccccc$  | O <sub>10</sub>   | $\begin{array}{c} 2 \times O_{12} \\ O_{16} \\ O_{14} \\ 2 \times O_{13} \end{array}$   | $egin{array}{c} 2.6 \pm 0.1 \ 2.7 \pm 0.2 \ 2.9 \pm 0.2 \ 3.0 \pm 0.1 \ \end{array}$    |
| O <sub>1</sub>    | $\begin{array}{c} O_3 \\ O_{14} \\ O_{11} \\ 2 \times O_2 \end{array}$                                       | $egin{array}{cccc} 1.82 & \pm & 0.03 \ 1.92 & \pm & 0.09 \ 1.9 & \pm & 0.1 \ 3.1 & \pm & 0.2 \ \end{array}$ | O <sub>11</sub>   | $\begin{array}{c} O_{12} \\ O_{16} \\ 2 \times O_{15} \\ O_{14} \end{array}$  | $egin{array}{c} 3.0\ \pm\ 0.2\ 2.5\ \pm\ 0.2\ 2.8\ \pm\ 0.1\ 2.5\ \pm\ 0.2 \end{array}$ |
|                   | $egin{array}{c} 2	imes \mathrm{O_{13}} \ 4	imes \mathrm{O_{12}} \end{array}$                                 | $egin{array}{cccc} 2.7 & \pm & 0.1 \ 2.8 & \pm & 0.1 \end{array}$   | O <sub>12</sub>   | $egin{array}{cccc} 2 	imes O_{13} \ 2 	imes O_{16} \ 2 	imes O_{14} \ \end{array}$  | $egin{array}{c} 2.7 \ \pm \ 0.1 \ 3.0 \ \pm \ 0.1 \end{array}$                          |
| O <sub>2</sub>    | $\begin{array}{c} 2 \times O_{16}^{12} \\ 2 \times O_{14} \\ 4 \times O_{13} \\ 2 \times O_{12} \end{array}$ | $egin{array}{c} 2.9 \pm 0.1 \ 2.9 \pm 0.2 \ 2.6 \pm 0.1 \ 3.0 \pm 0.2 \ \end{array}$                        | $ \begin{array}{c} O_{13} \\ O_{14} \\ O_{15} \end{array} $ | $\begin{array}{c c} 2 \times O_{14} \\ 2 \times O_{15} \\ 2 \times O_{16} \end{array}$  | $egin{array}{c} 3.2 \pm 0.1 \ 2.7 \pm 0.1 \ 2.7 \pm 0.1 \end{array}$                    |

the latter values have little physical meaning). The structure of  $\mathrm{Nb}_{12}\mathrm{O}_{29}$  (o-rh) is illustrated in Fig. 6, the interatomic distances and their standard deviations are given in Table 3 and a comparison between calculated and observed structure factors in Table 4.

Table 4. Comparison between calculated and observed structure factors from Weissenberg photographs of  $\mathrm{Nb_{12}O_{20}(o\text{-}\mathrm{rh})}$ . CuK radiation.

| $\begin{array}{ c c c c c c c c c c c c c c c c c c c$                                    | $\boldsymbol{F}$                        |
|---|---|
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | obs                                     |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 23                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | $\frac{23}{32}$                         |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | $\begin{array}{c} 32 \\ 27 \end{array}$ |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | $\frac{27}{25}$                         |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | $\begin{array}{c} 23 \\ 27 \end{array}$ |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    |   |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 19                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 11                                      |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$                                     | 50                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | <b>3</b> 5                              |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    |   |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 32                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 24                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 28                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 37                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 19                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 19                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 23                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 16                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 19                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 16                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 12                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 34                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 68                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 20                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | 22                                      |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | <b>59</b>                               |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | <b>45</b>                               |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      | 18                                      |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      | <b>53</b>                               |
| $23 \ 0 \ 6 \   \ -22 \   \ 16 \   \ 11 \ 5 \   \ -36 \   \ 39 \   \ 12 \ 4 \   \ -8 \  $ | 48                                      |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      | 14                                      |
|   | 6                                       |
| $egin{array}{ c c c c c c c c c c c c c c c c c c c$                                      | 49                                      |
| $egin{array}{ c c c c c c c c c c c c c c c c c c c$                                      | 20                                      |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      |   |
| $egin{array}{c ccccccccccccccccccccccccccccccccccc$                                       | 9                                       |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      | 10                                      |
| $egin{array}{ c c c c c c c c c c c c c c c c c c c$                                      | 23                                      |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      | 31                                      |
| $egin{array}{ c c c c c c c c c c c c c c c c c c c$                                      |   |
| $egin{array}{c ccccccccccccccccccccccccccccccccccc$                                       | 24                                      |
| $egin{array}{c ccccccccccccccccccccccccccccccccccc$                                       | 30                                      |
| $egin{array}{ c c c c c c c c c c c c c c c c c c c$                                      | 18                                      |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      | 17                                      |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      | 17                                      |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      | 14                                      |
| $10010 \mid 10 \mid 11 \mid 1111 \mid -36 \mid 32 \mid 128 \mid -12 \mid$                 | 14                                      |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$                                     | 11                                      |
| 14 0 10   35   32   8 1 11   41   42   15 2 8   15  | $\overline{13}$                         |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                    | $\tilde{61}$                            |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $                                      |   |

Table 4. Continued.

| $h\ k\ l$  | F calc   | $F \  m obs$                          | $h \ k \ l$   | $F_{ m calc}$  | F<br>obs                               | h k l   | F<br>calc   | F obs                                  |
|--|--|---------------------------------------|---|--|--|---|---|--|
| 8 2 10<br>10 2 10<br>12 2 10<br>14 2 10<br>16 2 10<br>22 2 10<br>30 2 10 | $\begin{array}{c c} 37 \\ 9 \\ 10 \\ 29 \\ -23 \\ -29 \\ 28 \end{array}$ | 41<br>7<br>11<br>30<br>27<br>32<br>20 | 1 2 12<br>7 2 12<br>15 2 12<br>0 2 16<br>1 2 16<br>7 2 16<br>8 2 16 | $egin{array}{c} -20 \ -26 \ 29 \ -30 \ 17 \ 21 \ 20 \ \end{array}$ | 21<br>34<br>31<br>37<br>21<br>21<br>17 | 14 2 16<br>15 2 16<br>16 2 16<br>22 2 16<br>23 2 16<br>1 2 22<br>7 2 22 | $egin{array}{c} 16 \\ -21 \\ -13 \\ -15 \\ 14 \\ 25 \\ 38 \\ \end{array}$ | 14<br>20<br>13<br>14<br>14<br>20<br>39 |

#### DISCUSSION

The analogy between the orthorhombic structure of  $\mathrm{Nb_{12}O_{29}}$  and the one of  $\mathrm{Ti_2Nb_{10}O_{29}}$  reported by Wadsley 4 is almost complete, the interatomic distances of the former being at an average somewhat longer. Thus the deviations from the ideal structure of this type derived by Wadsley are the same for both compounds.

It is of special interest to compare the metal-metal distances for the octahedra, which are joined by sharing edges. This kind of connection of NbO<sub>6</sub>-octahedra is also present in the structure of niobium dioxide, recently studied by Marinder <sup>3</sup>. This structure is related to the rutile type, but represents a complicated superstructure of the latter. A main feature of the atomic arrangement of the dioxide is that the niobium atoms are not eqally spaced along the c axis, but form pairs (Nb-Nb distance equal to 2.80 Å) which are at a Nb-Nb distance of 3.10 Å to the adjacent metal atom doublets. The short intermetal distance has been discussed in terms of a metal-metal bond. In Nb<sub>12</sub>O<sub>29</sub>(o-rh) the niobium-niobium distances of octahedra joined by edges are, however, within the range 3.15-3.70 Å, in close agreement with the metal-metal distances of Ti<sub>2</sub>Nb<sub>10</sub>O<sub>29</sub>(o-rh) (3.21-3.60 Å). This indicates that no metal-metal bonds are present in Nb<sub>12</sub>O<sub>29</sub>(o-rh).

Most of the niobium-oxygen distances are about 1.9 Å, some, however, are markedly long. There seems to be a tendency toward tetrahedral instead of octahedral configuration of oxygen atoms around some of the niobium atoms (i.e.  $Nb_1$ ).

Wadsley <sup>4</sup> has shown that  $\mathrm{TiNb_2O_7(mon)^{17}}$  and  $\mathrm{Ti_2Nb_{10}O_{29}(mon)}$  are members of a homologous series  $\mathrm{Me_{3n}O_{8n-3}}$  with n=3 and n=4, respectively. For the orthorhombic version of the series only  $\mathrm{Ti_2Nb_{10}O_{29}(o\text{-rh})}$  is known. In the system  $\mathrm{Nb-O}$  no phase  $\mathrm{Nb_3O_7}$  corresponding to  $\mathrm{TiNb_2O_7}$  was found in samples prepared in the temperature range  $1050-1350^{\circ}\mathrm{C}$ . The existence of a monoclinic modification of  $\mathrm{Nb_{12}O_{29}}$  is discussed in the next section.

# NOTE ON THE CRYSTAL STRUCTURE OF Nb12O29(mon)

As mentioned above, the powder patterns of all  $NbO_{2.40}$  samples hitherto prepared show a great number of extra lines in addition to the reflexions belonging to the orthorhombic modification of  $Nb_{12}O_{29}$ . All attempts to sepa-

rate the two phases have been in vain and it has not been possible to find a single crystal of the extra phase. If, however, we suppose that its structure is isomorphous with that of Ti<sub>2</sub>Nb<sub>10</sub>O<sub>29</sub>(mon) reported by Wadsley 4, it is possible to index its powder pattern. The following data for the unit cell of Nb<sub>12</sub>O<sub>29</sub>(mon) were thus obtained:

$$a = (15.67 \pm 0.02) \text{ Å}$$
  
 $b = (3.835 \pm 0.002) \text{ Å}$   
 $c = (20.73 \pm 0.02) \text{ Å}$   
 $\beta = (112.93 \pm 0.02)^{\circ}$   
 $V = 1153 \text{ Å}^{3}$ .

With two formula units in the elementary cell the calculated density becomes

 $d_{\rm calc}=4.55~{
m g~cm^{-3}}$  (for  ${
m Nb_{12}O_{29}(o\text{-rh})}$   $d_{\rm calc}=4.54~{
m g~cm^{-3}}$ ). In Table 1 the powder patterns of the  ${
m NbO_{2.40}}$  sample consisting of both modifications of Nb<sub>12</sub>O<sub>29</sub> is given. The intensity values of the monoclinic modification were calculated assuming the atomic coordinates to be the same as those reported by Wadsley for  $Ti_2Nb_{10}O_{29}(mon)$ 4. The good agreement between the observed data and those thus calculated indicate that these atomic coordinates are essentially valid also for the niobium oxide. The idealized version of this structure is given in Fig. 3c.

Further attempts will be made to find a single crystal of Nb<sub>12</sub>O<sub>29</sub>(mon) in order to make possible the derivation of its structural details.

Acknowledgements. The author wishes to thank Professor Arne Magnéli, Dr. Georg Lundgren, Dr. Peder Kierkegaard, Fil.lic. Stig Åsbrink, Fil.lic. Sten Andersson and Fil.lic. Bengt-Olov Marinder for valuable help and discussions in connection with this work. The BESK and FACIT EDB computers were made available by kind permission of the Swedish Board for Computing Machinery.

This investigation forms part of a research programme supported by the Swedish Natural Science Research Council.

### REFERENCES

- 1. Andersson, G. and Magnéli, A. Acta Chem. Scand. 11 (1957) 1065.
- Norin, R. and Magnéli, A. Naturwiss. 47 (1960) 354.
   Marinder, B.-O. Arkiv Kemi 19 (1962) 435.
   Wadsley, A. D. Acta. Cryst. 14 (1961) 664.

- 5. Lu, C. S. Rev. Sci. Instr. 14 (1943) 331.
- 6. International Tables for X-ray Crystallography Vol. I, Birmingham 1952, p. 152.
- 7. Edstrand, M. International Union of Crystallography World List of Crystallographic Computer Programs, 1st Ed., 1962, p. 16 No. 6022.

  8. Asbrink, S., Blomquist, G. and Westman, S. Arkiv Kemi 14 (1959) 545.
- 9. Magnéli, A. Acta Cryst. 4 (1951) 447.
- Maghell, A. Acta Cryst. 4 (1951) 441.
   Vand, V., Eiland, P. F. and Pepinsky, R. Acta Cryst. 10 (1957) 303.
   Åsbrink, S. and Brändén, C.-I. International Union of Crystallography World List of Crystallographic Computer Programs, 1st Ed., 1962, p. 16, No. 6023.
   Thomas, L. H. and Umeda, K. J. Chem. Phys. 26 (1957) 293.
   Suzuki, T. Acta Cryst. 13 (1960) 279.
   Cruickshank, D. W. J. Computing Methods and the Phase Problems in X-ray Crystal Anglesis. Programs, 1961.

- Analysis, Pergamon Press 1961, p. 45.
- Liminga, R. and Olovsson, I. International Union of Crystallography World List of Crystollographic Computer Programs, 1st Ed., 1962, p. 16, No. 6015.
   Liminga, R. and Olovsson, I. International Union of Crystallography World List of
- Crystallographic Computer Programs, 1st Ed., 1962, p. 16, No. 6014.
- 17. Wadsley, A. D. Acta Cryst. 14 (1961) 660.

Received February 15, 1963.